

**LECTURE NOTES
ON
SWITCH GEAR AND PROTECTIVE
DEVICES**

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MODULE- I

Basic idea of Relay Protection

- Protective relay and relaying system detect abnormal condition like faults in electrical circuits and operate automatic switchgear to isolate the faulty equipment from the system as quickly as possible.
- The most severe electrical failures in power system are shunt faults which are increase the system current, reduction in voltage, power factor and frequency.

There are two groups of relaying equipment for protecting any equipments.

1. Primary relaying equipment
2. Back-up relaying equipment

→ Primary relaying is the first defence for protecting the equipments where as back up protection relaying works only when the primary relaying equipment fails which means back-up relaying is inherently slow in action. (The cause of primary relay

failures → Back up relay should not have anything common with primary relays.

(i) ✓ Circuit breaker

(ii) ✓ D.C tripping voltage supply.

(iv) Current or voltage supply to the relay.

Relay: A relay is an automatic device which senses an abnormal condition in an electric circuit and closes its contacts. These contacts in turn close the circuit breaker trip coil circuit, thereby it opens the circuit breaker ~~trip circuit~~ and the faulty part of the electric circuit is disconnected for

be rest of the healthy system.

Pick up level: - The value of actuating quantity which is on the threshold (border) above which relay operates ✓

operating time: - The time which

The elapse between the instant when the actuating quantity exceeds the pick up value to the instant when the relay contact close.

Reset time: - The time which elapse between the instant when the actuating quantity becomes less than the reset value to the instant when the relay contact returns to its normal position.

OR The time which the operating relay to ^{comes back to its initial position as a result of a} Reach: - A distance relay operates when

ever the impedance seen by the relay is less than a prescribed value. The impedance or the corresponding distance is known as the reach of the relay.

underreach: - The tendency of the relay to restrain at the set value or the impedance or impedance lower than the set value is known as under reach.

overreach: - The tendency of the relay to operate at impedance larger than the setting is known as overreach.

Relay burden: - It is the value of power consumed by the relay circuit at rated current or voltage and expressed in VA for ac and watt for d.c

Functional characteristic of protective relaying.

→ Reliability: - The relay should be reliable is the basic requirement.

→ Selectivity: - It is the basic requirement of the relay, in which it should be possible to select which part of the system is faulty and which is not and should isolate the faulty part of the system from unhealthy part.

- Discrimination

Unit protection: - This type of protection means the one in which the protection responds only to fault within its own zone, and does not make note

Non unit protection: - Non unit system protection is one which the selectivity is obtained by grading the time or current setting of the relay at different location,

Speed: - Speed is desirable characteristic of relay. It should neither be too slow which may result the damage of equipment nor should be too fast which may result

undesirable operation during transient faults.

Nature and cause of faults:-

- ① The nature of fault indicates any abnormal condition, between phase conductors & earth or between phase conductors.
- ② X fault always ~~causes~~ some effect on the ~~system~~
- ③ (a) Breakdown may occur at normal voltage on account (i) the deterioration of insulation level (ii) ~~deterioration~~ perching of birds (iii) accidental short circuiting by snakes. (iv) Kite strings
- (b) Breakdown may occur due to switching surges (i) surge caused by lightning.

* Pollution of insulator string which is commonly caused by deposited salt or cement dust which cause the insulation level will reduce.

* The insulation level of sheathed cable and armoured cable will decrease because of ageing

* Void formation in the insulating compound of underground cable due to unequal

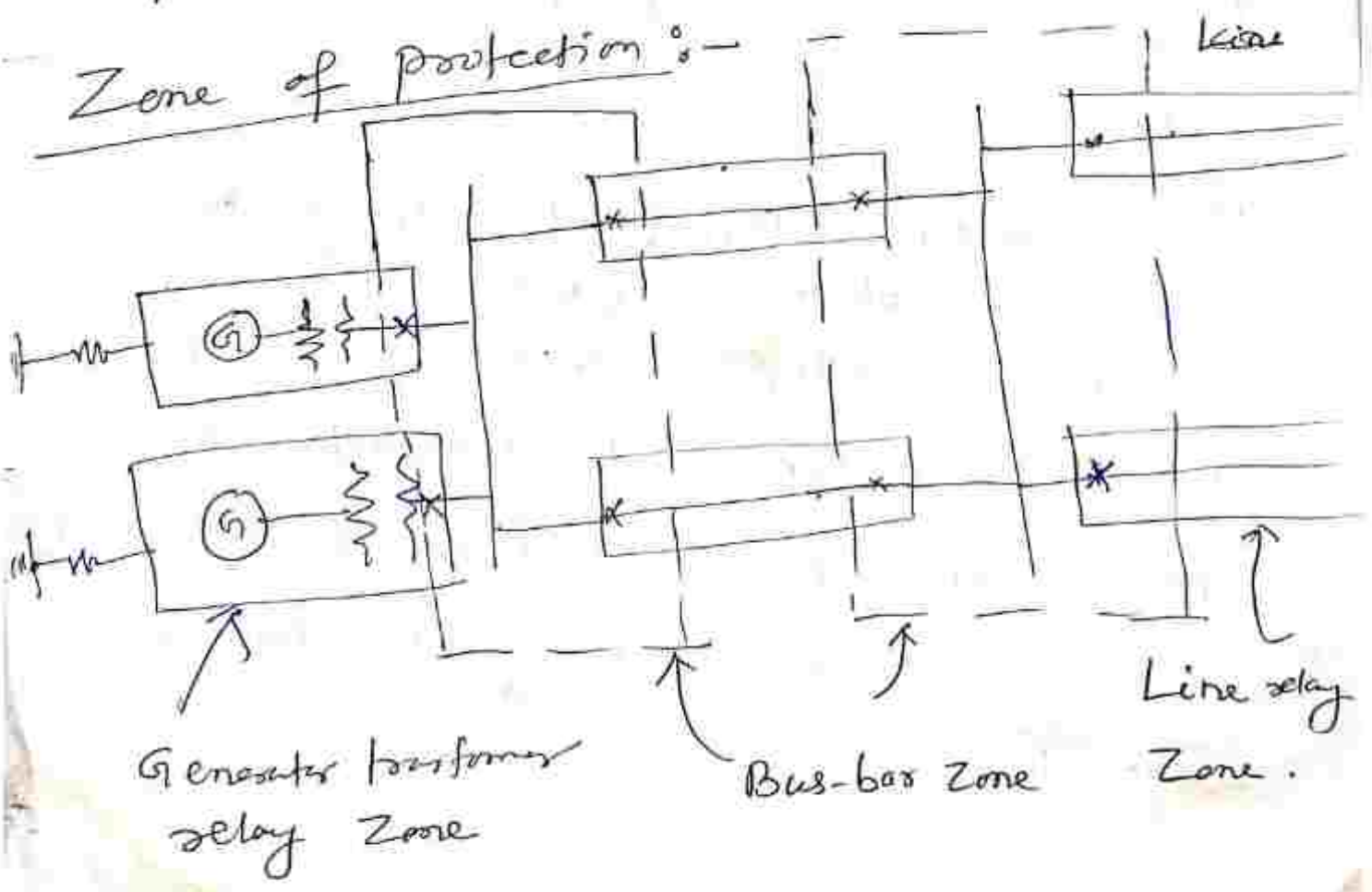
expansion and contraction caused by rise and fall of temperature is another cause of insulation failure.

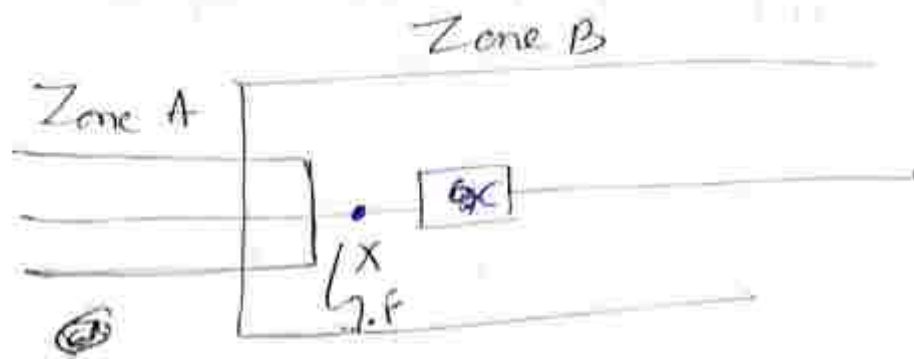
→ The line and apparatus insulation may be subjected to transient over-voltages because of the switching operations. The voltage level is very high, so requirement is high insulation level.

→ Lightning produce a very high voltage surges in power systems of the order of millions of volts and thus it is not feasible to provide an insulation which can withstand this abnormality.

→ The surge level with the velocity of light in the power system is limited by surge impedance.

Zone of protection :-

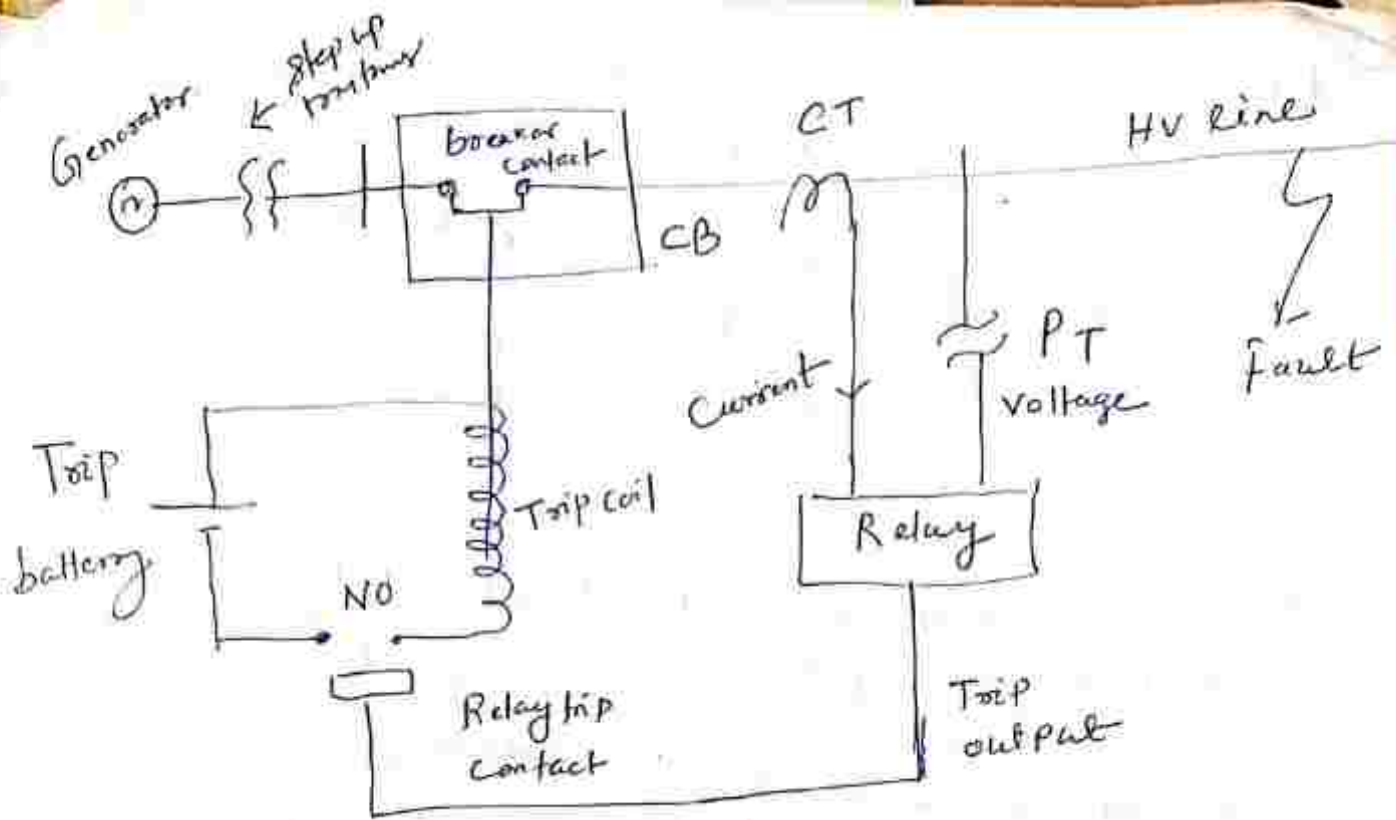




- ✓ (1) Fault will occur at X the CB of Zone B ~~and~~ including C will tripped, this does not intercept the flow of fault current from Zone A. The relaying equipment of Zone B must trip certain breakers in Zone A. For faults in Zone B to the right of breaker C, the operation of breaker in Zone A is not useful.

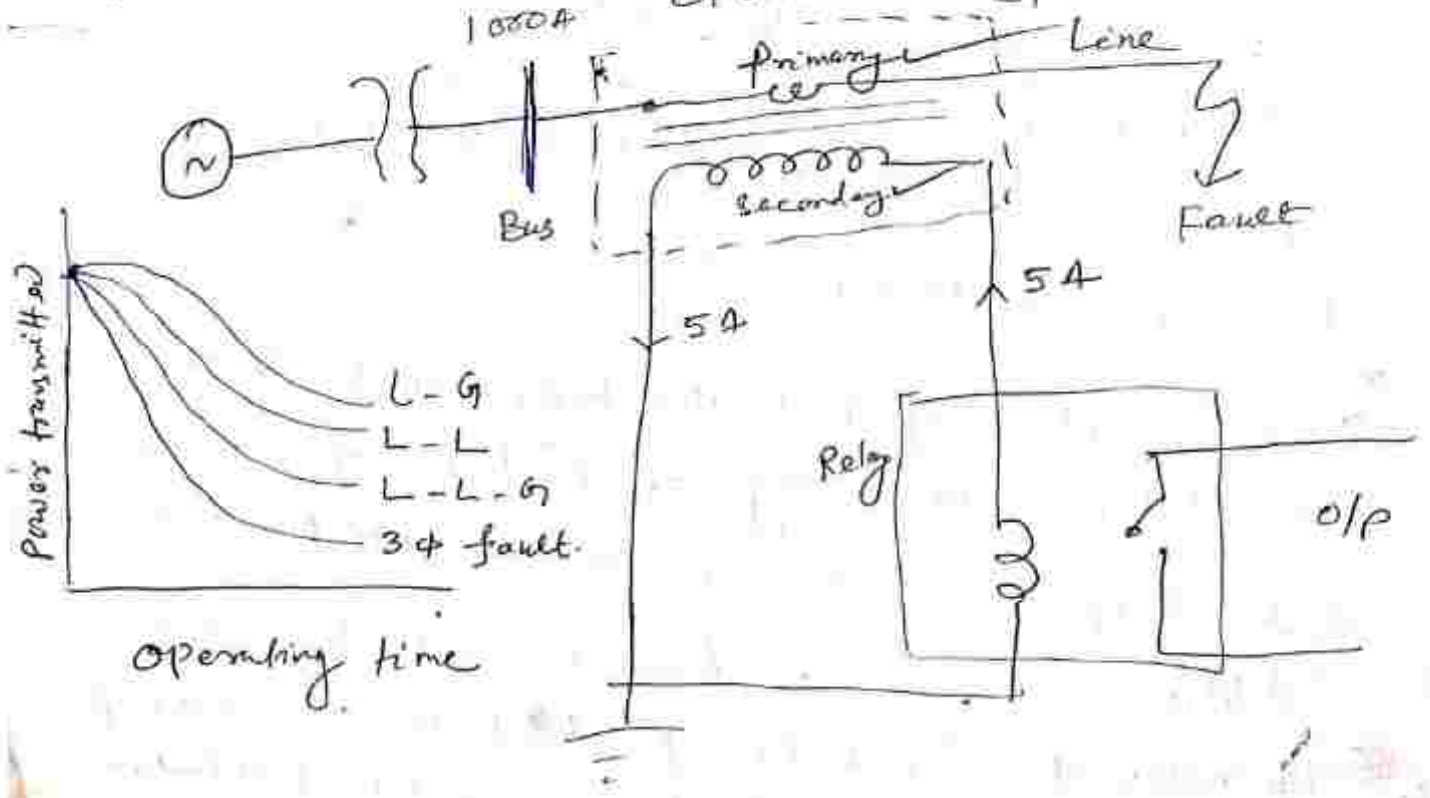
Basic principle of operation of protection system.

- (1) ✓ This type relay operate when current increases above a certain magnitude. This is called over current relay.
- (2) ✓ Another type relay operate when the ratio of V/I is less than a given value is known as under-impedance relay.

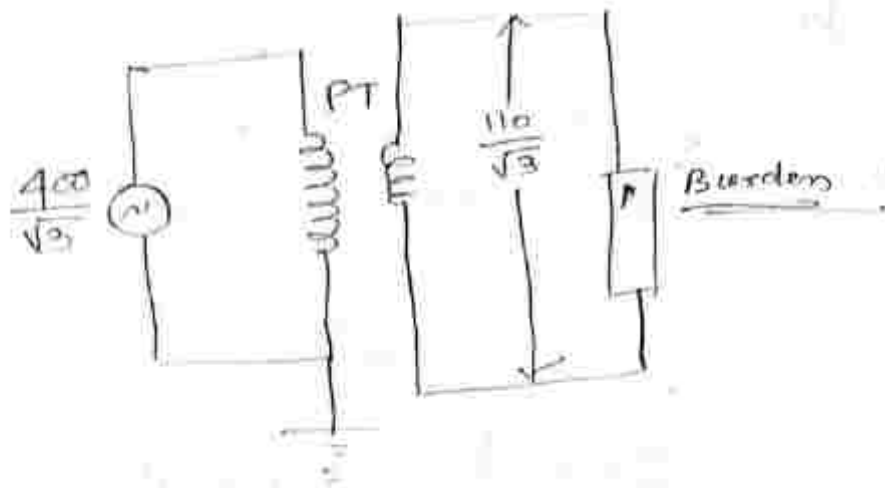


CT:- The standard secondary current ratings used in 5A and 1A. In practice, there is always some errors. This error is known as magnitude and phase angle (ratio error & phase angle error)

CT ratio = $\frac{1000A}{5A}$ CT



PT :-



- The CB is an electrically operated switch which is making as well as breaking the short circuit current. When the trip coil is energized it releases a latch, the energy stored in spring to bring about quick opening operation.
- The farthest point from the relay location and the reach point is termed as reach of the relay which is still inside the zone, is called reach point. The distance between the relay location and reach point is termed as the reach of the relay.

Primary and Backup protection:-

- When primary protection fails, due to failure of CT/PT or relay or failure of CB or D.C tripping voltage or moving mechanism. Therefore, we must have to insert second defence of back up protection. In case of primary protection fails, back up protection is required. Back up protection should not have anything common with primary protection.

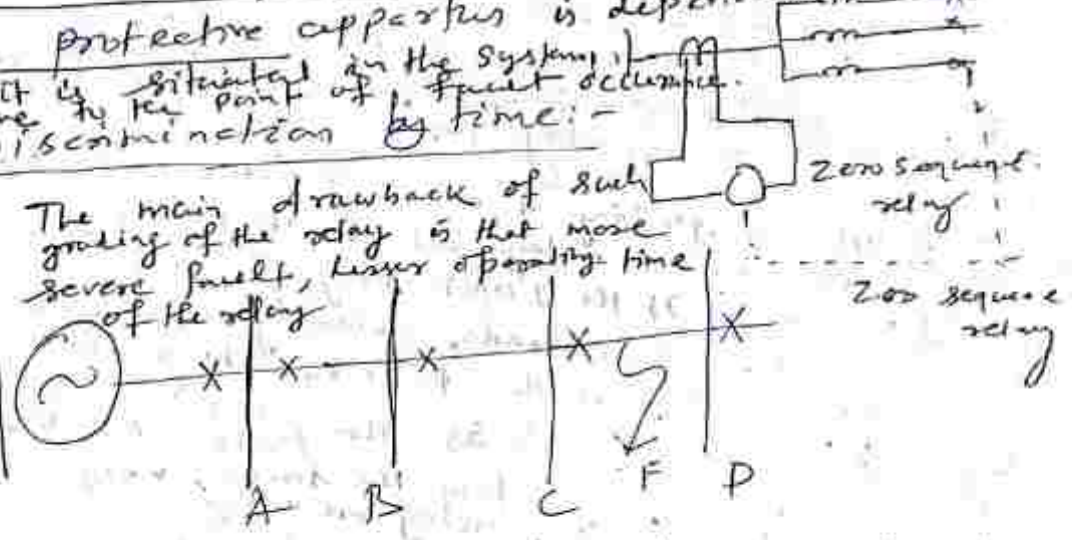
Back up protection must wait for the primary protection to operate. The operating time of the back up protection must be delayed by an appropriate amount ~~over~~ that primary protection's plus operating time of the primary circuit breakers.

Methods of Discrimination:

The objective to isolate the faulty system in a minimum time. There are various methods under this category are those in which the behaviour of the protective apparatus is dependent upon where it is situated in the system relative to the point of fault occurrence.

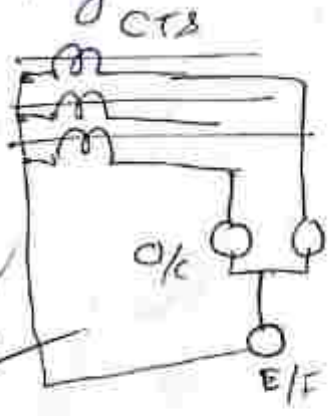
(a) Discrimination by time:

The main drawback of such grading of the relay is that more severe fault, lesser operating time of the relay



The circuit breaker is to trip nearest the fault prior to those farther off the point of fault by using time lag features. Suppose a fault in any any section of CD, the whole breaker's at A, B, C will trip, so the whole feeder ^{beyond A} becomes dead. So the requirement is that time lag to the CB at A, B, C and D

- ✓ A = 1.2 sec
- ✓ B = 0.8 sec
- ✓ C = 0.4 sec
- ✓ D = no time lag



Suppose fault occurs at CD section, the breaker at C will trip after a time of 0.4 sec. The feeder upto C will remain alive. ~~As above~~

(B) Discrimination by current magnitude - Current grading

This type of grading is done in a system where the fault current varies with the location of the fault.

The fault current increases as we go towards the source.

The pick up value of relay are set at the source, higher current towards the source, then the system is stable. In time-graded system, long time delay is required, that is the disadvantage point. It is difficult to

calculate the relay accuracy under transient condⁿ.

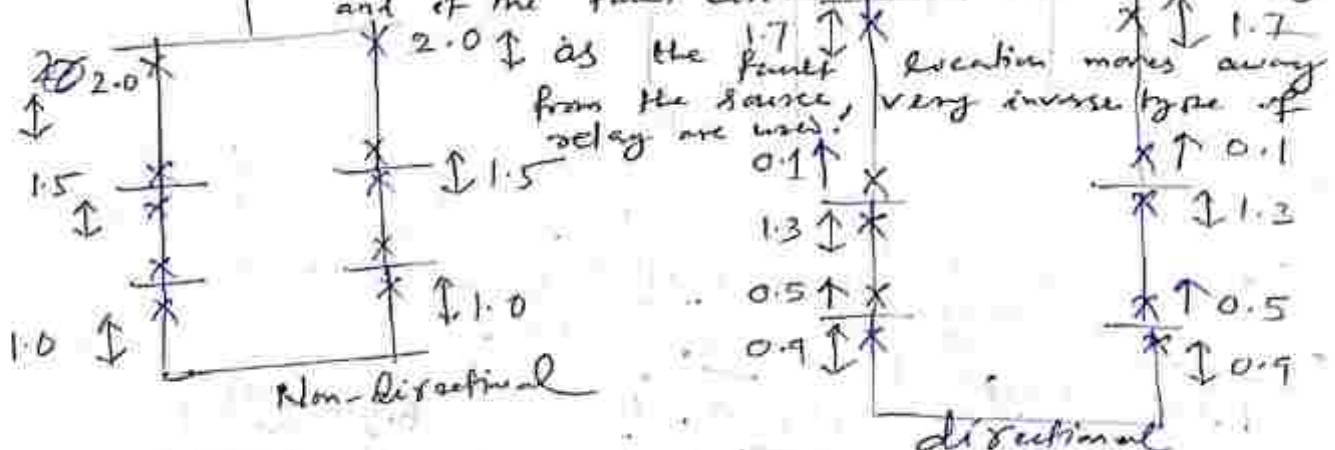
~~Both the pickup points are set up to pickup at the source. Higher current towards the source.~~

(C) Discrimination by time and direction

This type of grading is achieved with the help of inverse time overcurrent relay and almost widely used is the IDMT relay.



If the IDMT relay are slow at low value of overloads, extremely inverse relay are used and if the fault current reduces substantially



→ If we set non directional relay with same current setting but different time lags, the proper discrimination can not be obtained.

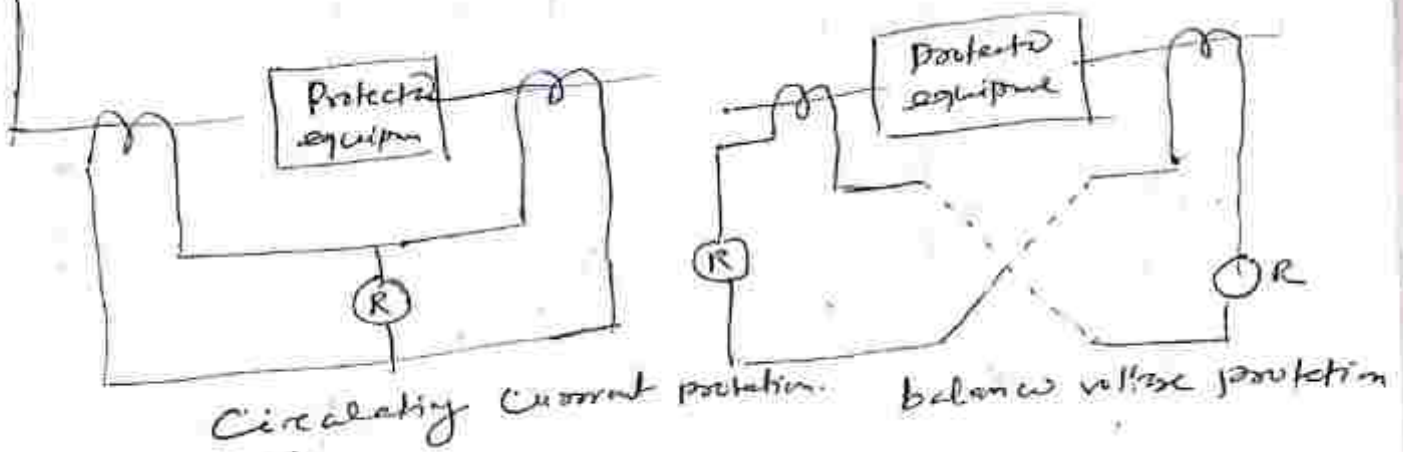
→ If we set directional features, the fault occurs at any section will be discriminated without loss of supply.

Discrimination by distance measurement

The faults nearer to the source have more severe takes longer time to clear if we have used time discrimination.

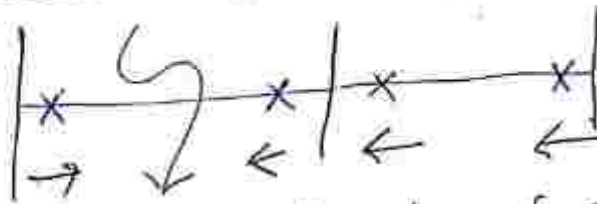
99 Combined time and distance protection gives the practical dimension of protection. unit protection is divided into two parts.

- (a) Circulating current principle
- (b) opposed voltage principle or balanced voltage principle.



→ In circulating current protection, the external fault does not disturb ~~and~~ whereas ~~of~~ if the fault within the protective equipment, the relay trips.

~~Power~~ - direction comparison discrimination ^{the CT secondary voltage will no longer balanced and current will flow in the relay which will trip the CB at that end.}



- ① power flows out at the other end, which means either load condⁿ or external fault condⁿ obtained tripping should be prevented
- ② power flows in, which may internal fault condⁿ and the breaker trip.

99 This case directional relay is used

Phase comparison discrimination:-

This is a power line carrier ~~CB~~ protection.

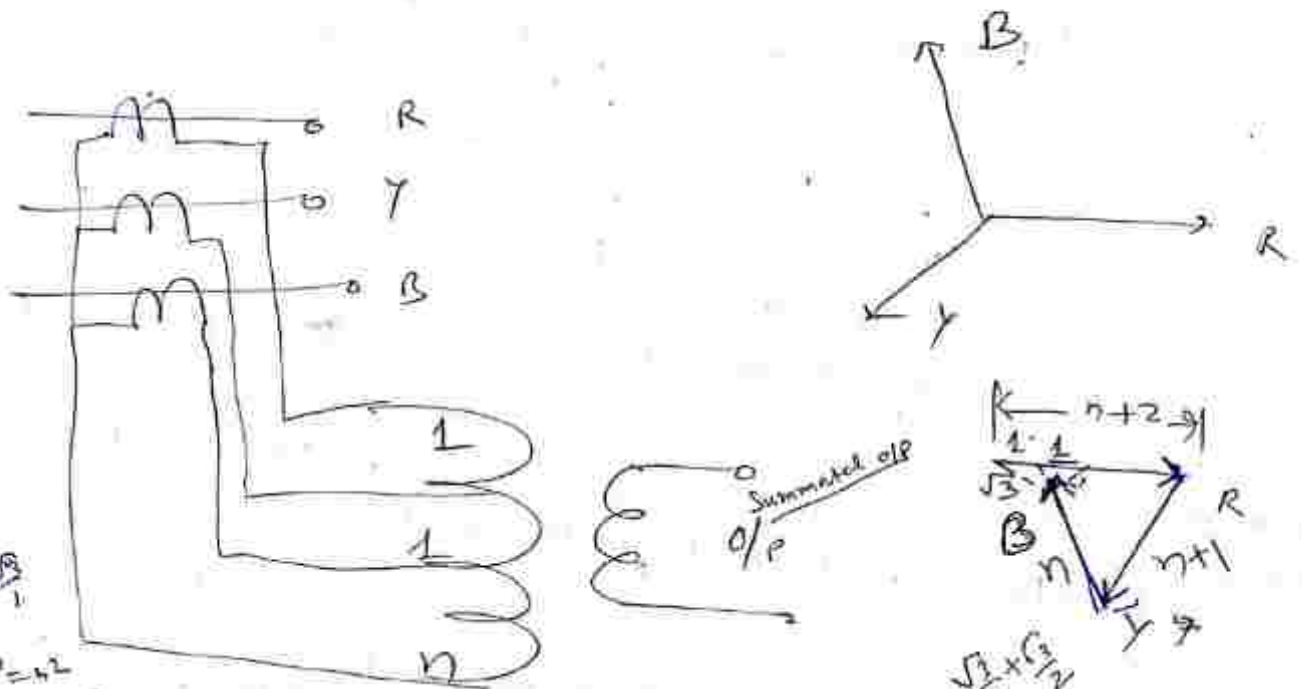
In this phase angle of current at both section will compared, whether the fault is internal or external. The phase angle information of primary current is transmitted by carrier line

Derivation of a single phase quantity from three phase quantity. —

✓ There are two commonly methods for deriving single phase quantity from a three phase system.

① Summation of transformer: —

→ The three CTs are connected to the primary winding of an auxiliary transformer. Each CT has different no. of turns.



$$\begin{aligned}
 P^2 + P^2 &= 4I^2 \\
 P^2 &= 4I^2 - 4I^2 \\
 &= \sqrt{2} - I^2 \\
 &= 2 - 1 \\
 &= 1.2/2 - 1 \\
 &= 0.21
 \end{aligned}$$

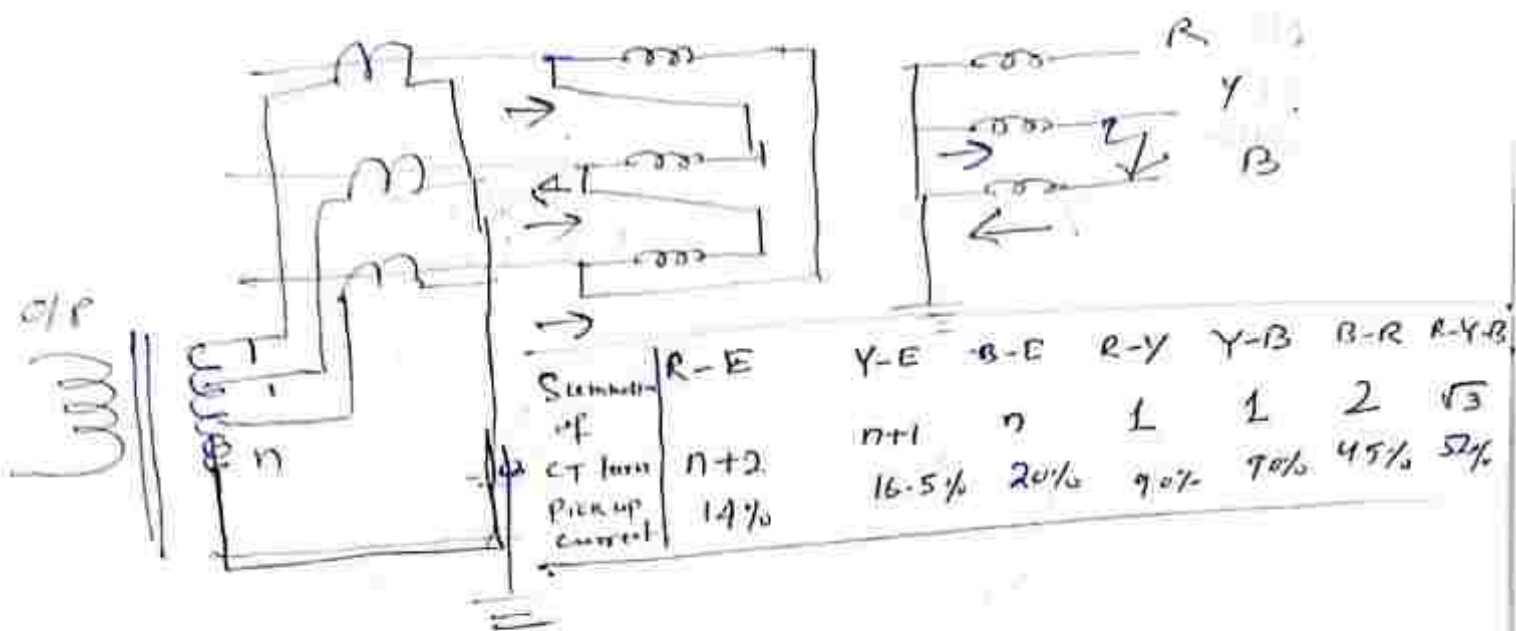
$$(n+2) I_R + (n+1) I_Y + n I_B$$

$$\begin{aligned}
 & \frac{\sqrt{3} + \sqrt{3}}{2} \\
 & \frac{2I}{\sqrt{3}}
 \end{aligned}$$

→ By this also control independently the o/p for earth fault and phase fault.

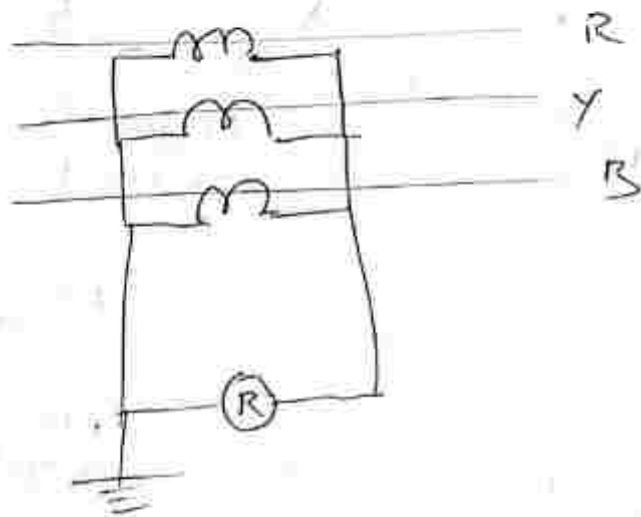
→ By this method pick up setting can be expressed in terms of n and 1 .

→ If there is phase to phase fault on the star side of delta/star transformer, zero o/p will occur at the meter. though fault condition



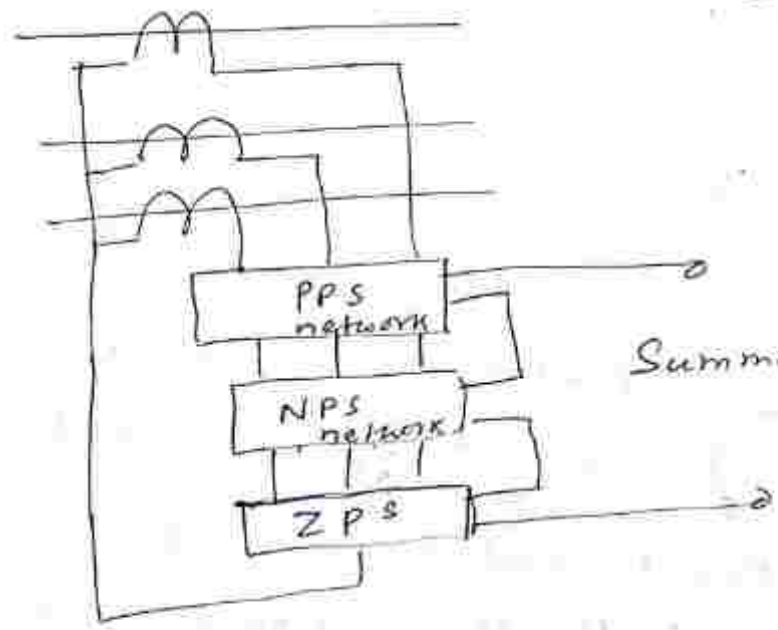
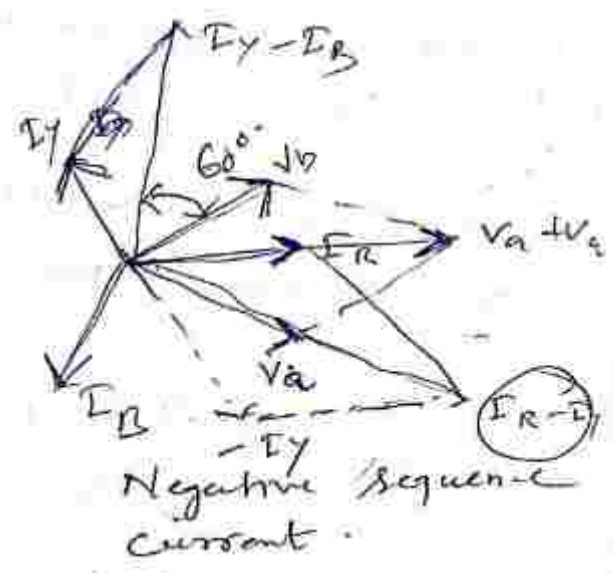
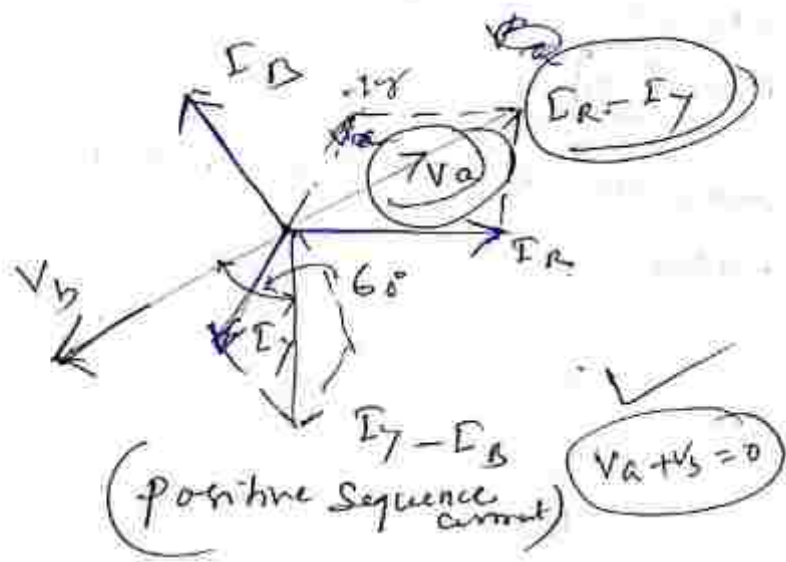
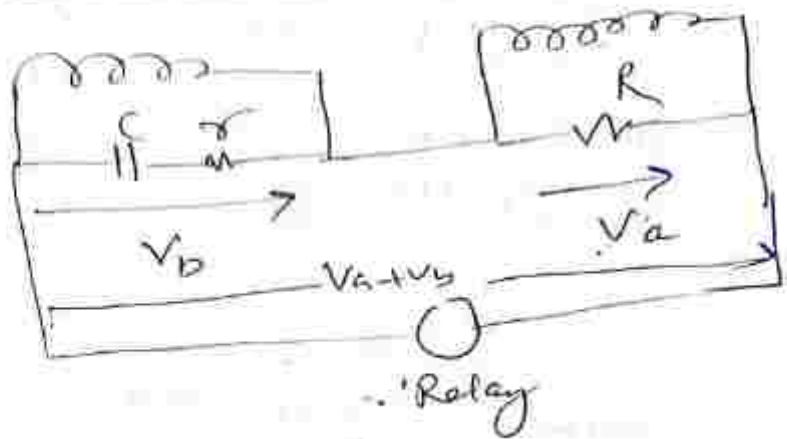
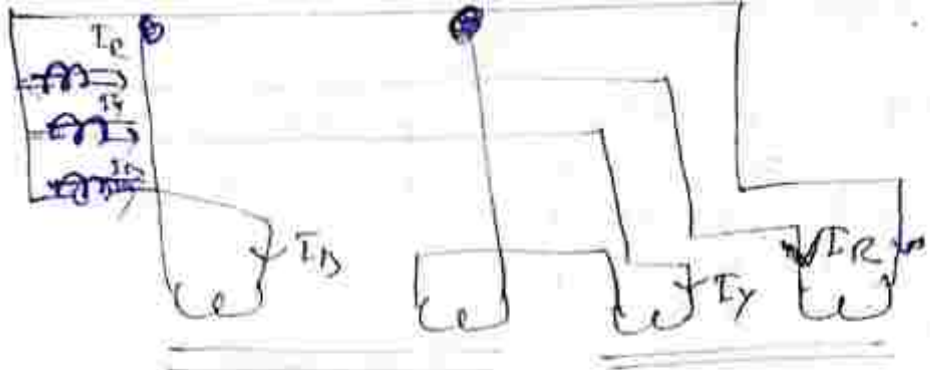
✓ Sequence network : - Zero sequence and negative sequence network are always used
Power System Protection

→ Zero sequence network are extensively used for earth fault protection.



→ When single or double earth fault occurs, the sequence of current flows through the relay.

→ For unbalanced condition or unsymmetrical fault, negative phase sequence network are used.



(Positive phase shifting PPS)

(NPS) Negative phase shifting

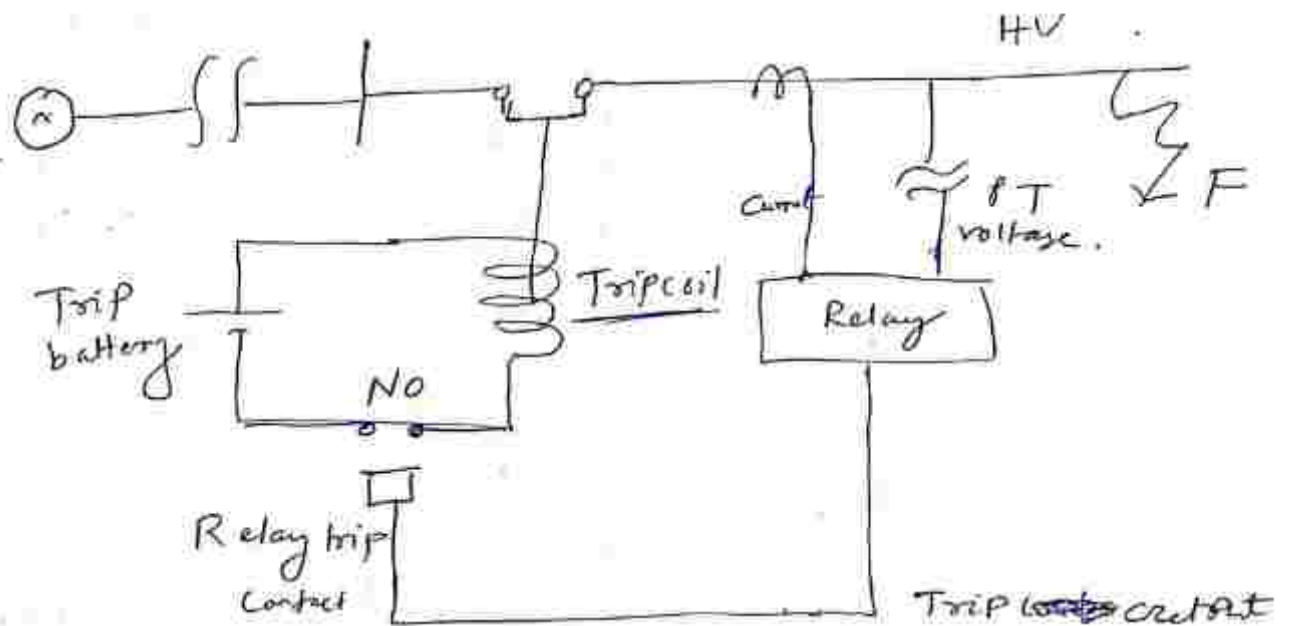
Summated output

Components of Relay protection

(1) Relay: — The main functions of a protective relay is to isolate a faulty section with the least interruption. The basic function of relay is design to detect and to measure abnormal conditions and close the contact in the tripping circuit.

(2) Circuit breaker: —

- Circuit breakers of various types are installed in all power circuits to open and close them under normal load conditions.
- CB are operated either manually or automatically.
- When tripping is required a trip coil is energized, which the energy will be released by trip coil. The trip battery supplies energy to the trip coil for this operation.
- The relay usually it contact directly.



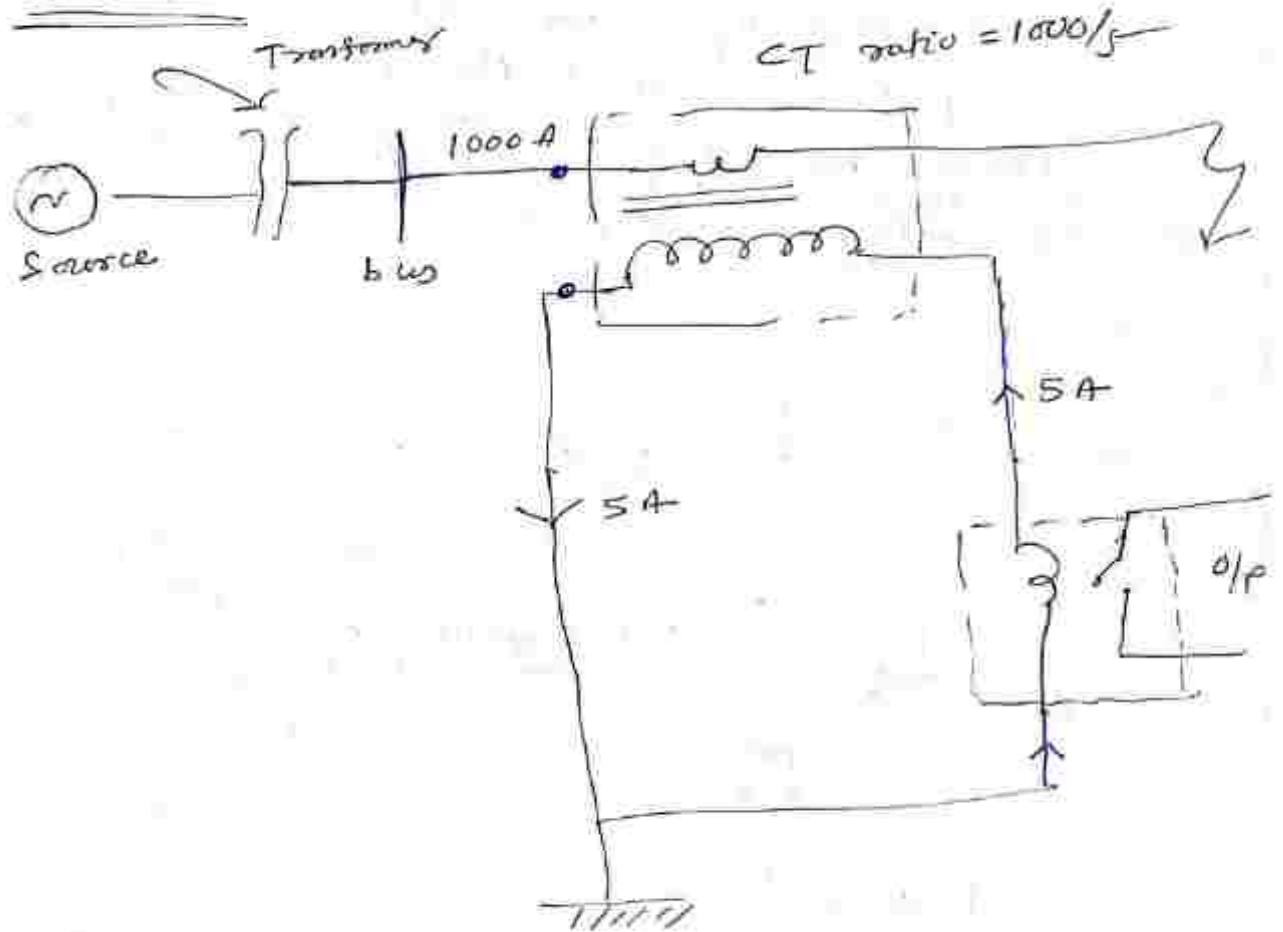
→ Tripping and other auxiliary supply

→ In power system two kinds auxiliary supply
d.c or a.c.

→ All d.c auxiliary supply circuit
must have their insulation resistance
maintained adequate level.

→ A.c auxiliary supply for the protective
relay scheme is mainly derived from
CTs. Under fault conditions, the amount
of current passes through the CT will always
be sufficiently to reliably trip the CB.

→ CT

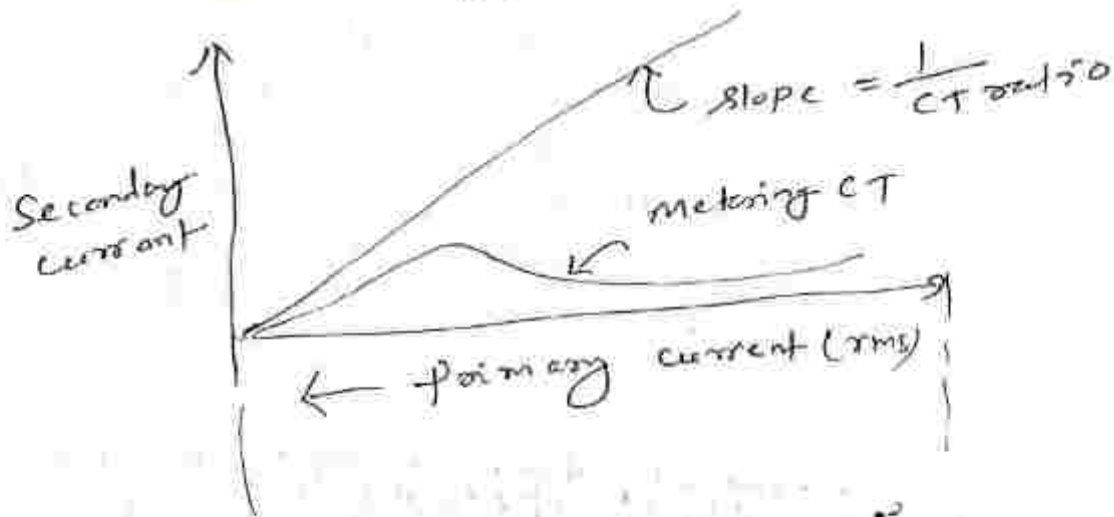
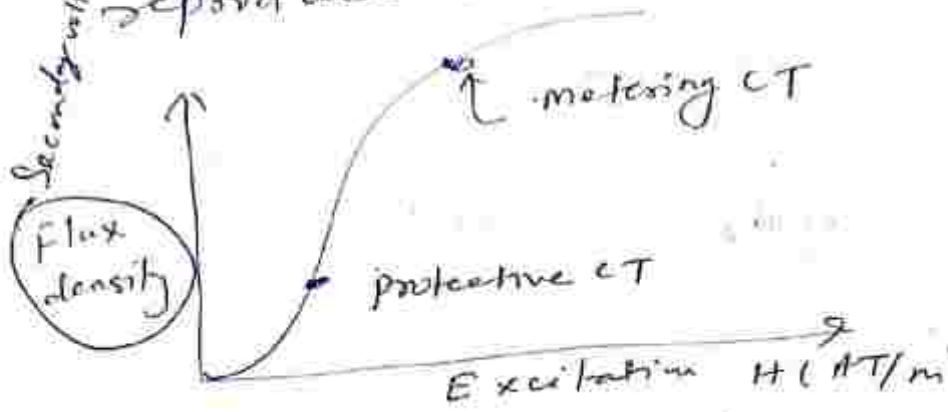


→ The standard secondary current rating
of CT are 5A & 1A.

→ In practice, there is always some errors.
These errors are known as ratio errors and
phase angle error.

→ A metering CT is so designed that it will saturate and it prevent from damage due to excessive current.

→ protective CT is designed to faithfully reproduce largest fault current



PT

Relay Classification:- According to the protective scheme,

Relay may be divided into main, auxiliary and signal relays.

✓ Main relay:- The main relay which responds to any change in actuating quantity, current, voltage & power.

✓ Auxiliary relay:- To perform some auxiliary function, the auxiliary relay ^{which} ^{are} controlled by other relay.

- to perform
- (a) time delay
 - (b) increasing no. of contact
 - (c) increase the making or breaking capacity of the contact.
 - (d) passing signal to other relay
 - (e) tripping of ckt breaker
 - (f) energizing a signal or an alarm.

✓ Signal relay:- ^{signal relay function to register the operation of some relay by flag indication.} ^{It indicates flag indication.}

(b) It can be actuate audible alarm ext.

Over relay:- Relay which responds to the actuating quantity when it exceeds a pre-determined value are over relays and of ~~type~~

Under relay:- when the actuating quantity drops below a predetermined value, they known as under relay

MODULE- II

Basic principle of relay:-

The electromagnetic relay are two types
(A) electromagnetic attraction (B) electromagnetic induction.

→ The armature is attracted to the pole of an electromagnet in electromagnetic attraction type relay.

→ The relay can be operated both d.c as well as a.c quantity.

→ With d.c supply, the torque is constant and if the force exceeds a predetermined value relay operates.

$$F \propto I^2$$

$$F = k' I^2$$

$$\text{Let } I = I_m \sin \omega t$$

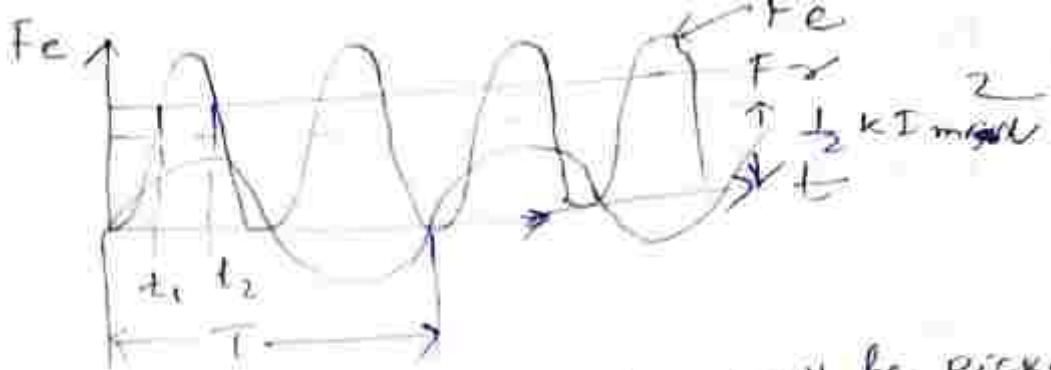
$$F = k' (I_m^2 \sin^2 \omega t)$$

$$= k' I_m^2 \left(\frac{1 - \cos 2\omega t}{2} \right)$$

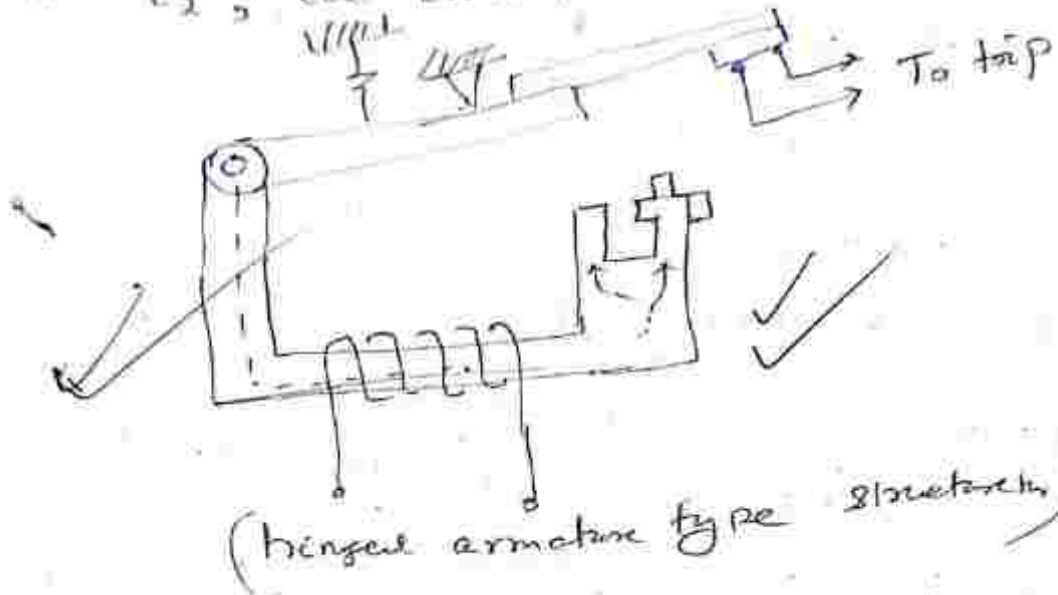
$$F = \frac{1}{2} k' I_m^2 - \frac{1}{2} k' I_m^2 \cos 2\omega t$$

The force has two component, one constant and other is function time i.e pulsating double frequency. The armature of the relay vibrates at double frequency. It will damage the relay contact.

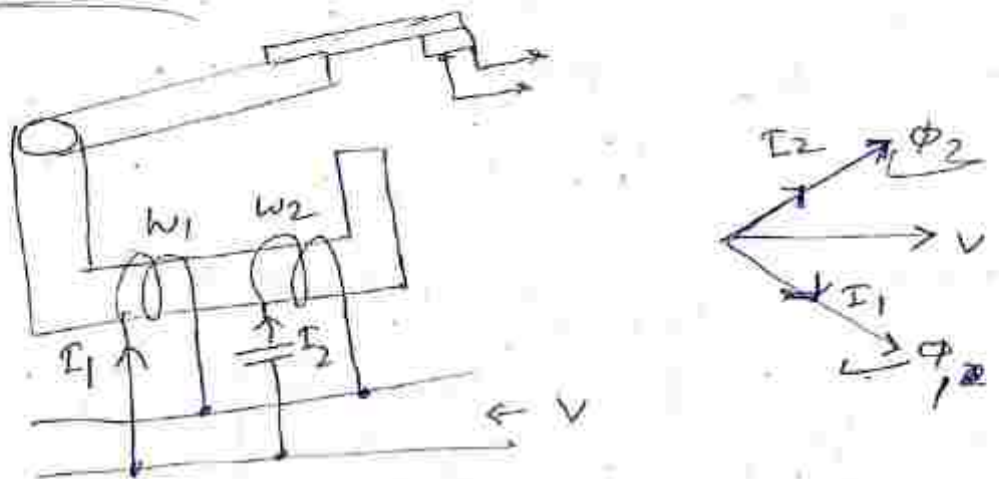
→ To overcome these difficulties, the two fluxes producing the force are displaced in time phase or phase shifting network ~~connected~~ or ~~connected~~ shading ring on the pole of the magnet.



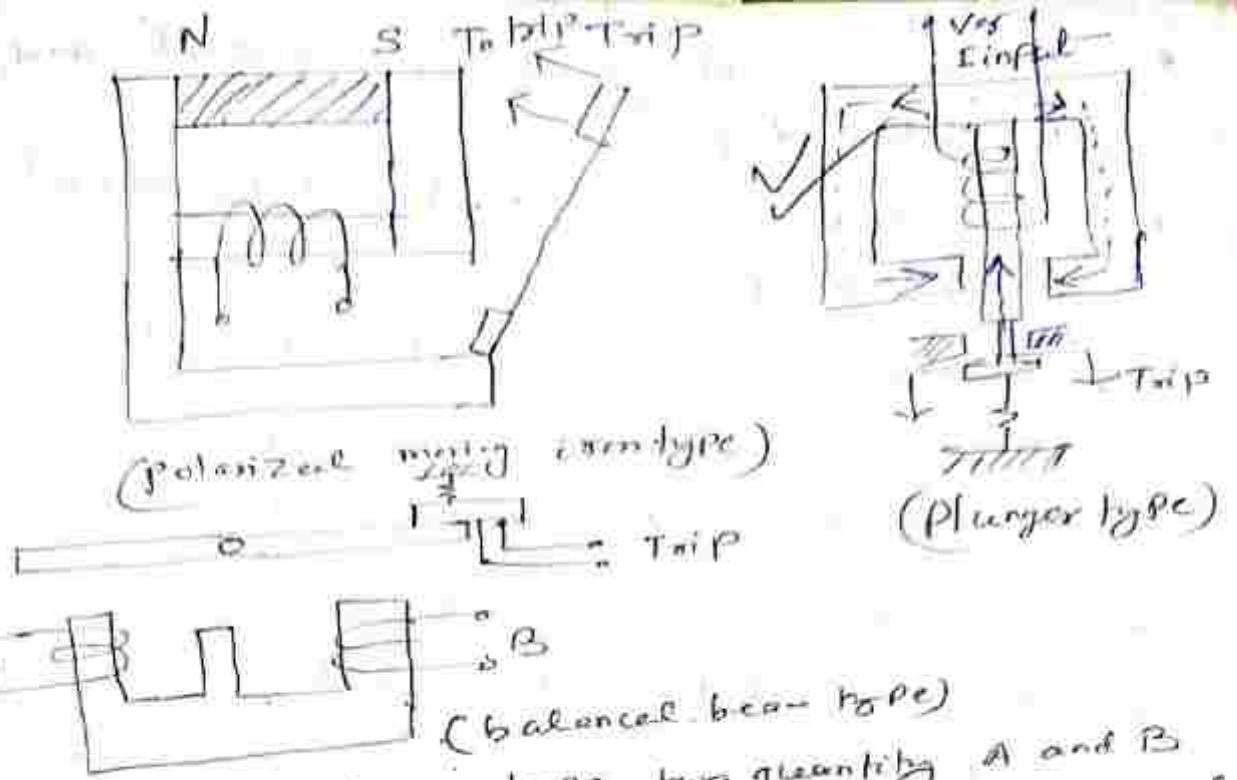
At time t_1 , the relay armature will be picked up.
 At " t_2 , the armature drops off at t_2 .



The flux through the shading pole lags behind unshaded pole.



→ Hinged armature type relay are used auxiliary relay e.g. tripping relay. The sensitivity of this relay can be increased for dc operation by addition of permanent magnet. This is known as polarized moving iron relay.



→ In balanced beam type two quantities A and B are compared. Actually $|A|^2$ and $|B|^2$ are compared because electromagnetic force are proportional to $(\text{ampere turn})^2$. It has low ratio reset/operating current. It is set for fast operation, there is a tendency to overshoot on transient condn.

Induction relay:-

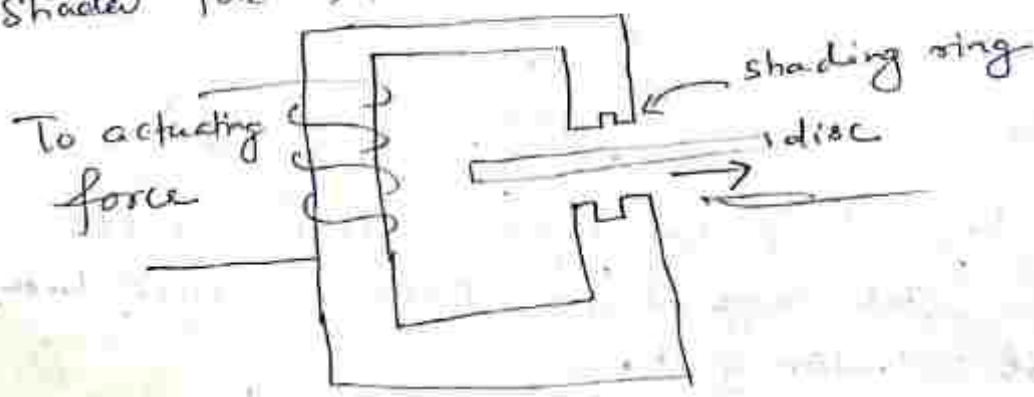
① This type of relay based on electromagnetic induction principle. These relay can be used on a.c. Depending on rotor, it is divided two type

- ⊕ (a) induction disc type
- ⊕ (b) induction cup type

→ In induction disc type relay, disc is ~~fixed~~ movable but moving contact of relay is fixed

→ There are two type of structure is available

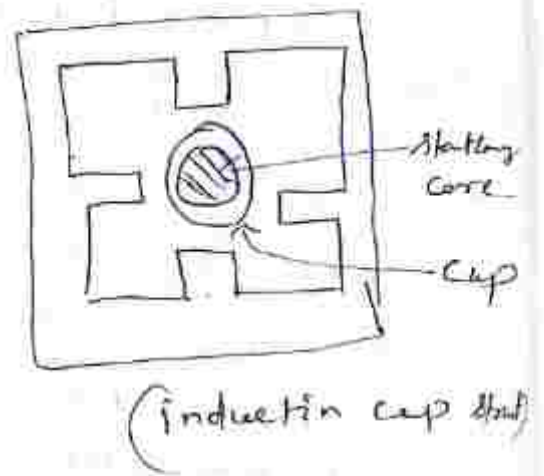
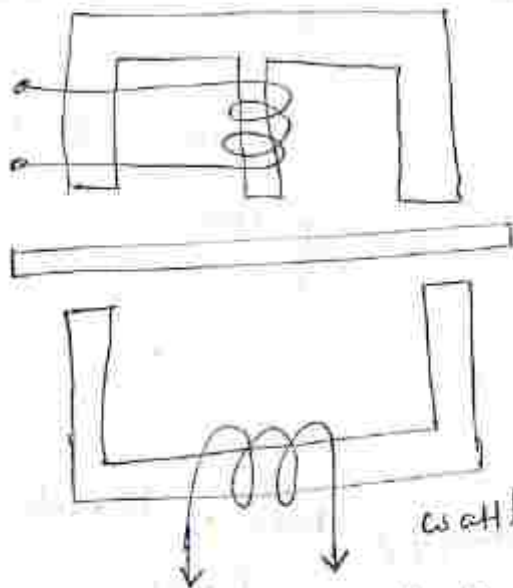
- ⊕ (a) Shaded pole structure (b) the weather vane structure.



- The disc is placed between shaded and unshaded pole of the relay.
- The system current is fed to the operating coil of the relay.
- The air gap flux is split into two out of phase components.
- The shading ring is made up of copper.
- The disc is normally made off aluminium, because it have low inertia and less deflecting torque.

~~Torque equation of induction relay~~

Watt hour meter structure :



- The construction of this structure is exactly identical to watt hour meter.
 - It has two coils on two different magnetic circuit.
- #### Induction Cup Relay

- It has four or more electromagnets
- A stationary iron core is placed between these electromagnets.

→ The rotor is a hollow cylindrical cup which is free to rotate in gap.

→ When electromagnet is energized, they induce voltages in the rotor cup and eddy current will induced. This eddy current interact with other pole.

→ The induction cup type relay are more sensitive than induction disc type relay.

→ The ratio of reset to pick up is high in induction relay as compared to armature relay.

→ The ratio between 95% to 100%.

Theory of induction relay torque: -

Two fluxes displaced in space and time phase are required.

$$\phi_1 = \phi_m \sin \omega t$$

$$\phi_2 = \phi_m' \sin(\omega t + \theta)$$

ϕ_1 is produced by the shaded pole

ϕ_2 is the flux produced by unshaded pole

The shaded pole flux lags an angle θ by the unshaded pole. The flux ϕ_1 & ϕ_2 induced an emf e_1 and e_2 .

$$e_1 \propto \frac{d\phi_1}{dt} \propto \phi_m \omega \cos \omega t$$

$$e_2 \propto \phi_m' \omega \cos(\omega t + \theta)$$

The voltage will circulate the eddy current in the disc of the relay.

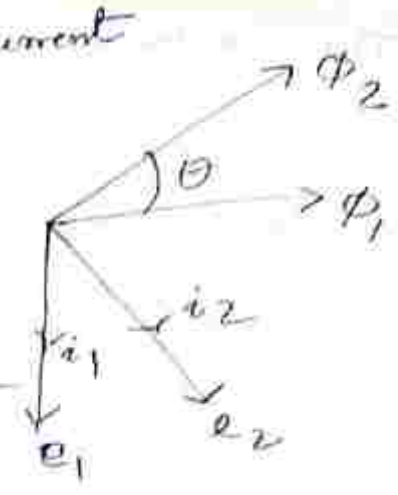
$$e_1 \propto e_1$$

$$e_1 \propto \phi_m \omega \cos \omega t$$

$$e_2 = \phi_m' \omega \cos(\omega t + \theta)$$

Flux ϕ_1 will interact with eddy current i_2 and ϕ_2 will interact with i_1 .

ϕ_2 leads ϕ_1 , the torque due to ϕ_2 and i_1 will be act as positive & ϕ_1 & i_2 will be negative



$$T \propto \phi_2 i_1 - \phi_1 i_2$$

$$\propto \phi_m \sin(\omega t + \theta) \cdot \phi_m \omega \cos \omega t - \phi_m \sin \omega t \cdot \phi_m \omega \cos \omega t$$

$$\propto \phi_m \phi_m' \sin(\omega t + \theta) \omega \cos \omega t - \phi_m \phi_m' \omega \sin \omega t \cos(\omega t + \theta)$$

$$\propto \phi_m \phi_m' \omega (\sin(\omega t + \theta - \omega t))$$

$$\propto \phi_m \phi_m' \omega \sin \theta$$

→ The torque is maximum when $\theta = 90^\circ$, if we maintain $\theta = 90^\circ$, no possibility of vibration

→ while we have doing different current setting, the no. of turns are changed

→ Higher the current setting required smaller of turns.

→ The higher the time multiplier setting greater the operating time.

→ The relay operating time depends upon between the moving contact & fixed contact of the relay.

Relay design & construction

- 1 → (a) ✓ Selection of the operating characteristic
- (b) ✓ Selection of paper construction
- (c) Selection of paper construction
- (d) ✓ Design of the contact movement from the point of view of utmost reliability.

① → The operating characteristic of the relay must be same abnormal operating characteristic.

② The most important characteristic ~~of~~ ~~are~~ for construction are reliability, simple circuit design.

Construction :- (a) contact (b) bearing (c) terminations
Electromechanical design (d) terminations & housing.

✓ Selection of contact material :-

- 1 → nature of current to be interrupted
- 2 → ~~voltage~~ bouncing & making operation of contact.
- 3 → The magnitude of current to be interrupted.
- 4 → Frequency of operation.
- 5 → The actual speed of contact to make or break.
- 6 → contact shape
- 7 → contact closing force.

On the basis of practical experience the following are some of the rules recommended in the design of contact system of a relay.

- (a) To avoid arcing
- (b) To reduce contact resistance by increase pressure.
- (c) To maintain accuracy, so the relay should provide maximum torque/weight ratio.

(d)

Bearing

- (i) Single ball bearing
- (ii) multi-ball bearing
- (iii) Pivot & jewel bearing
- (iv) Knife edge bearing.

Electromechanical design: - It relates the mechanical features of core, yoke and the armature. The reluctance of the magnetic path is kept to a minimum. The relay coil usually limited to 5A and the voltage to 220V, but still the insulation for the relay coil is designed to withstand 4 kV.

Termination & housing

- (1) The base of armature is done with a spring. The spring is insulated by moulded blocks. These moulded block

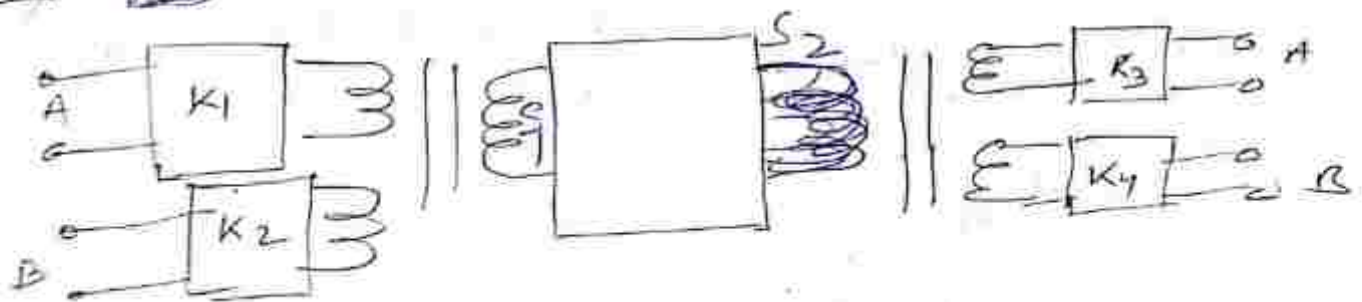
Generation equation of comparator:

→ Amplitude & phase is two quantity require for setting the point. The comparator decides the operating characteristic of the relay.

Let S_1 & S_2 be two input signals such that when the phase relationship is a magnitude relationship always predetermined condition, tripping is initiated.



→ The input signal has derived from voltage transformer and current transformer and some mixing circuit



$$\overline{S_1} = K_1 \overline{A} + K_2 \overline{B}$$

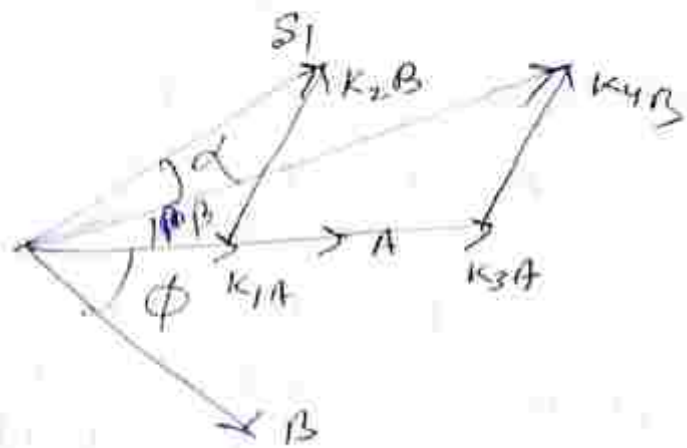
$$\overline{S_2} = K_3 \overline{A} + K_4 \overline{B}$$

A & B are primary system quantity, K_1 and K_3 are the scalar constant and K_2 and K_4 are the complex number with θ_2 and θ_4 as angles (vectors).

Let the vector A be the reference vector and B lags behind A by an angle ϕ . Then equation can be rewritten as:

$$S_1 = k_1 |A| + k_2 |B| \left\{ \cos(\theta_2 - \phi) + j \sin(\theta_2 - \phi) \right\}$$

$$S_2 = k_3 |A| + k_4 |B| \left\{ \cos(\theta_4 - \phi) + j \sin(\theta_4 - \phi) \right\}$$



If the operating criterion is such that $|S_1| \geq |S_2|$ then at the threshold operation, $|S_1| = |S_2|$ ✓

$$\{k_1 A + k_2 B \cos(\theta_2 - \phi)\}^2 + \{k_2 B \sin(\theta_2 - \phi)\}^2$$

$$= (k_3 A)^2 + \{k_4 B \cos(\theta_4 - \phi)\}^2 + \{k_4 B \sin(\theta_4 - \phi)\}^2$$

$$\begin{aligned} & \cancel{(k_1^2 - k_3^2) A^2 + k_2^2 B^2 \cos^2(\theta_2 - \phi) + k_2^2 B^2 \sin^2(\theta_2 - \phi)} \\ & \quad - \cancel{k_4^2 B^2 \cos^2(\theta_4 - \phi) + k_4^2 B^2 \sin^2(\theta_4 - \phi)} \end{aligned}$$

= 0

$$\cancel{(k_1^2 - k_3^2) A^2 +}$$

$$\begin{aligned} & (k_1 - k_3)^2 A^2 + \{k_2 B (\cos \theta_2 \cos \phi + \sin \theta_2 \sin \phi)\}^2 \\ & + \{k_2 B (\sin \theta_2 \cos \phi - \cos \theta_2 \sin \phi)\}^2 \end{aligned}$$

$$- \{k_4 B (\cos \theta_4 \cos \phi + \sin \theta_4 \sin \phi)\}^2 - \{k_4 B (\sin \theta_4 \cos \phi - \cos \theta_4 \sin \phi)\}^2$$

$$\begin{aligned}
& (k_1 - k_3) |A|^2 + k_2^2 B^2 \cos^2 \theta_2 \cdot \cos^2 \phi + k_2^2 B^2 \sin^2 \theta_2 \sin^2 \phi \\
& + 2 k_2 B \cos \theta_2 \cdot \cos \phi \cdot \sin \theta_2 \cdot \sin \phi \\
& + k_2^2 B^2 \sin^2 \theta_2 \cdot \cos^2 \phi - k_2^2 B^2 \cos^2 \theta_2 \cdot \sin^2 \phi \\
& - 2 k_2 B \sin \theta_2 \cdot \cos \phi \cdot \cos \theta_2 \cdot \sin \phi \\
& - k_4^2 B^2 \cos^2 \theta_4 \cdot \cos^2 \phi - k_4^2 B^2 \sin^2 \theta_4 \cdot \sin^2 \phi \\
& - 2 k_4 B \cos \theta_4 \cdot \cos \phi \cdot \sin \theta_4 \cdot \sin \phi \\
& - k_4^2 B^2 \sin^2 \theta_4 \cdot \cos^2 \phi + k_4^2 B^2 \cos^2 \theta_4 \cdot \sin^2 \phi \\
& + 2 k_4 B \sin \theta_4 \cdot \cos \phi \cdot \cos \theta_4 \cdot \sin \phi
\end{aligned}$$

$$\Rightarrow (k_1 - k_3) |A|^2 + k_2^2 |B|^2 \cos^2 (\theta_2 - \phi) + k_2^2 |B|^2 \sin^2 (\theta_2 - \phi) - k_4^2 |B|^2 \cos^2 (\theta_4 - \phi) - k_4^2 |B|^2 \sin^2 (\theta_4 - \phi)$$

New

$$\begin{aligned}
& \left\{ k_1 |A| + k_2 |B| \cos (\theta_2 - \phi) \right\}^2 + \left\{ k_2 |B| \sin (\theta_2 - \phi) \right\}^2 \\
& = \left\{ k_3 |A| + k_4 |B| \cos (\theta_4 - \phi) \right\}^2 + \left\{ k_4 |B| \sin (\theta_4 - \phi) \right\}^2
\end{aligned}$$

$$\begin{aligned}
& (k_1^2 - k_3^2) |A|^2 + 2 |A| |B| \left\{ k_1 k_2 \cos (\theta_2 - \phi) - k_3 k_4 \cos (\theta_4 - \phi) \right\} \\
& + k_2^2 |B|^2 \cos^2 (\theta_2 - \phi) - k_4^2 |B|^2 \cos^2 (\theta_4 - \phi) \\
& + k_2^2 |B|^2 \sin^2 (\theta_2 - \phi) - k_4^2 |B|^2 \sin^2 (\theta_4 - \phi) = 0
\end{aligned}$$

$$(k_1^2 - k_3^2) |A|^2 + 2 |A| |B| \left\{ k_1 k_2 \cos (\theta_2 - \phi) - k_3 k_4 \cos (\theta_4 - \phi) \right\} + (k_2^2 - k_4^2) |B|^2 = 0$$

Dividing by $(k_2^2 - k_4^2) |A|^2$

$$\frac{k_1^2 - k_3^2}{k_2^2 - k_4^2} + \left| \frac{B}{A} \right|^2 + 2 \left| \frac{B}{A} \right| \left\{ \frac{k_1 k_2 \cos(\alpha_2 - \phi) - k_3 k_4 \cos(\alpha_4 - \phi)}{k_1^2 - k_4^2} \right\}$$

$$= 0$$

$$\left| \frac{B}{A} \right|^2 + 2 \left| \frac{B}{A} \right| \left\{ \frac{k_1 k_2 \cos \alpha_2 \cdot \cos \phi + k_3 k_4 \sin \alpha_2 \cdot \sin \phi}{k_1^2 - k_4^2} - \frac{k_3 k_4 \cos \alpha_4 \cdot \cos \phi - k_1 k_2 \sin \alpha_4 \cdot \sin \phi}{k_2^2 - k_4^2} \right\}$$

$$\left| \frac{B}{A} \right|^2 + 2 \left| \frac{B}{A} \right| \left\{ \frac{(k_1 k_2 \cos \alpha_2 - k_3 k_4 \cos \alpha_4) \cos \phi + (k_1 k_2 \sin \alpha_2 - k_3 k_4 \sin \alpha_4) \sin \phi}{k_1^2 - k_4^2} + \frac{k_1^2 - k_3^2}{k_2^2 - k_4^2} \right\} = 0$$

$$\Rightarrow \left| \frac{B}{A} \right|^2 + \left\{ 2 \left| \frac{B}{A} \right| [a_0 \cos \phi + b_0 \sin \phi] + c_0 \right\} = 0$$

$$a_0 = \frac{k_1 k_2 \cos \alpha_2 - k_3 k_4 \cos \alpha_4}{k_2^2 - k_4^2}$$

$$b_0 = \frac{k_1 k_2 \sin \alpha_2 - k_3 k_4 \sin \alpha_4}{k_2^2 - k_4^2}$$

$$c_0 = \frac{k_1^2 - k_3^2}{k_2^2 - k_4^2}$$

$$\delta = \frac{2}{|k_1 k_2|} \cos^2 \alpha_2 + \frac{2}{k_3 k_4} \cos^2 \alpha_4 + 2 k_1 k_2 k_3 k_4 \cos \alpha_2 \cos \alpha_4$$

$$+ k_1 k_2 \sin^2 \alpha_2 + k_3 k_4 \sin^2 \alpha_4$$

$$+ 2 k_1 k_2 \sin \alpha_2 \sin \alpha_4$$

$$\left(\frac{B}{A} \right) + A (A_0 \cos \phi + B_0 \sin \phi) \neq C_0 = (A_0 \cos \phi + B_0 \sin \phi)$$

$$r = \sqrt{C_0^2 - a_0^2 - b_0^2}$$

$$\left(\frac{B}{A} \right) \cos \phi$$

$$\left(\frac{B}{A} \right) \sin \phi$$

$$\begin{aligned} x &= r \cos \phi \\ y &= r \sin \phi \end{aligned}$$

$$k_1 - k_3$$

$$\left(\frac{B}{A} \right) \cos \phi = 2x$$

$$2 \left(\frac{B}{A} \right) \cos \phi = 2x$$

$$2 \left(\frac{B}{A} \right) \sin \phi = 2y$$

$$x^2 + y^2 + 2a_0 x + 2b_0 y + c_0 = 0$$

$$x^2 + y^2 + 2a_0 x + 2b_0 y + c_0 = 0$$

$$r = \sqrt{C_0 - a_0^2 - b_0^2}$$

$$r = \sqrt{C_0 - a_0^2 - b_0^2}$$

$$C_0 = \sqrt{a_0^2 + b_0^2}$$

$$\begin{aligned} & (x - a_0) \\ & + (y - b_0) \\ & + - r - r \end{aligned}$$

$$\delta = \sqrt{c_0^2 - a_0^2 - b_0^2}$$

$$= \left(\frac{k_1^2 - k_3^2}{k_2^2 - k_4^2} \right)^2 - \left(k_1 k_2 \sin^2 \theta_2 + k_3 k_4 \cos^2 \theta_2 - 2 k_1 k_2 k_3 k_4 \cos^2 \theta_2 \cos^2 \theta_2 \right)$$

$$= \left(\frac{k_1^2 - k_3^2}{k_2^2 - k_4^2} \right)^2 - \left((k_1 k_2 \sin^2 \theta_2)^2 + (k_3 k_4 \cos^2 \theta_2)^2 + 2 k_1 k_2 \sin \theta_2 \cdot k_3 k_4 \cos \theta_2 \right)$$

$$= \left(\frac{k_1^2 - k_3^2}{k_2^2 - k_4^2} \right)^2 - \left(k_1 k_2 \cos^2 \theta_2 - k_3 k_4 \cos^2 \theta_2 + 2 k_1 k_2 k_3 k_4 \cos^2 \theta_2 \cdot \cos^2 \theta_2 \right)$$

$$= \left(\frac{k_1^2 - k_3^2}{k_2^2 - k_4^2} \right)^2 - \left(k_1 k_2 \sin^2 \theta_2 + k_3 k_4 \cos^2 \theta_2 + 2 k_1 k_2 k_3 k_4 \sin^2 \theta_2 \cdot \cos^2 \theta_2 \right)$$

$$= \left(\frac{k_1^2 - k_3^2}{k_2^2 - k_4^2} \right)^2 - \left(k_1 k_2 - k_3 k_4 + 2 k_1 k_2 k_3 k_4 \sin^2 \theta_2 \cdot \cos^2 \theta_2 \right)$$

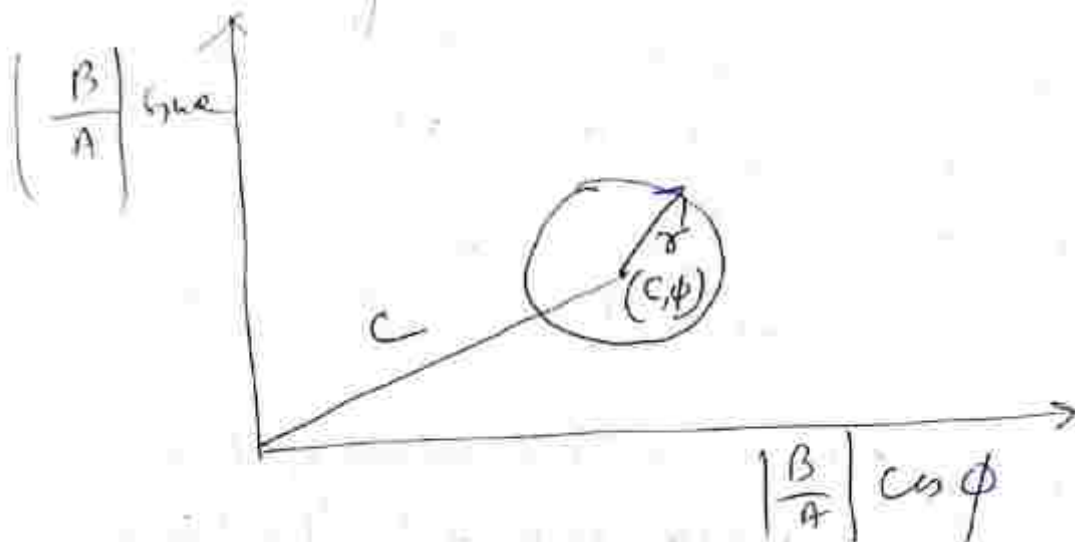
$$\delta = \sqrt{c_0^2 - a_0^2 - b_0^2}$$

$$= \sqrt{\frac{k_1^2 |k_4|^2 + |k_2|^2 k_3^2 - 2 |k_1| |k_2| |k_3| |k_4| \cos(\theta_2 - \theta_2)}{k_1^2 - k_4^2}}$$

$$C = \sqrt{a_0^2 + b_0^2}$$

$$= \sqrt{k_1^2 k_2^2 + k_3^2 k_4^2 - 2 k_1 k_2 k_3 k_4 \cos(\theta_2 - \theta_4)}$$

$$|k_2| - |k_4|$$

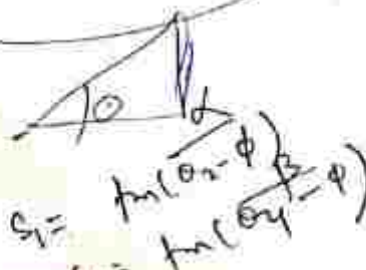


(Threshold ch. of Amplitude comparator)

Analysis for phase comparator :-

Here the inputs S_1 & S_2 stated their phase relation $S_1 = |S_1| \angle \alpha$, $S_2 = |S_2| \angle \beta$ with respect to reference axis. The scalar product of these two vector quantities is maximum when they are in phase and positive torque will be obtained when $\alpha - \beta = \pm \pi/2$

$$\vec{A} \cdot \vec{B} = AB \cos \theta$$



$$S_1 = \tan(\alpha - \phi)$$

$$S_2 = \tan(\beta - \phi)$$

$$\tan(\alpha - \beta) = \pm \infty$$

$$\frac{\tan \alpha - \tan \beta}{1 + \tan \alpha \cdot \tan \beta} = \pm \infty$$

$$1 + \tan \alpha \cdot \tan \beta = 0$$

$$\frac{1 + \frac{|k_2||B|\sin(\theta_2 - \phi)}{|k_1||A| + |k_2||B|\cos(\theta_2 - \phi)}}{\times \frac{|k_4||B|\sin(\theta_4 - \phi)}{|k_3||A| + |k_4||B|\cos(\theta_4 - \phi)}} = 0$$

$$\Rightarrow \left\{ \frac{|k_1||A| + |k_2||B|\cos(\theta_2 - \phi)}{|k_2||B|\sin(\theta_2 - \phi)} \right\} \left\{ \frac{|k_3||A| + |k_4||B|\cos(\theta_4 - \phi)}{|k_4||B|\sin(\theta_4 - \phi)} \right\} = 0$$

$$\Rightarrow k_1 k_3 |A|^2 + k_1 |k_4| |A| |B| \cos(\theta_4 - \phi) + |k_2| |k_3| |A| |B| \cos(\theta_2 - \phi) + |k_2| |k_4| |B|^2 \cos(\theta_2 - \phi) \cos(\theta_4 - \phi) + |k_2| |k_4| |B|^2 \sin(\theta_2 - \phi) \sin(\theta_4 - \phi) = 0$$

Dividing the equations by $\frac{|k_2||k_4||A|^2 \cos(\theta_2 - \theta_4)}{\text{we get}}$

$$\frac{|B|^2}{|A|^2} + \frac{|B|}{|A|} \left\{ \frac{(|k_1||k_4| \cos \theta_4 + |k_2||k_3| \cos \theta_2) \cos \phi + (|k_1||k_4| \sin \theta_4 + |k_2||k_3| \sin \theta_2) \sin \phi}{(|k_2||k_4| \cos(\theta_2 - \theta_4))} \right\}$$

$$+ \frac{k_1 k_3}{(|k_2||k_4| \cos(\theta_2 - \theta_4))} = 0$$

$$\text{or } \frac{|B|^2}{|A|^2} + \frac{|B|}{|A|} \left\{ A_0' \cos \phi + B_0' \sin \phi \right\} + C_0' = 0$$

$$A_0' = \frac{(|k_1||k_4| \cos \theta_4 + |k_2||k_3| \cos \theta_2)}{(|k_2||k_4| \cos(\theta_2 - \theta_4))}$$

$$B_0' = \frac{(|k_1||k_4| \sin \theta_4 + |k_2||k_3| \sin \theta_2)}{(|k_2||k_4| \cos(\theta_2 - \theta_4))}$$

$$C_0' = \frac{k_1 k_3}{(|k_2||k_4| \cos(\theta_2 - \theta_4))}$$

Solⁿ:
Solved

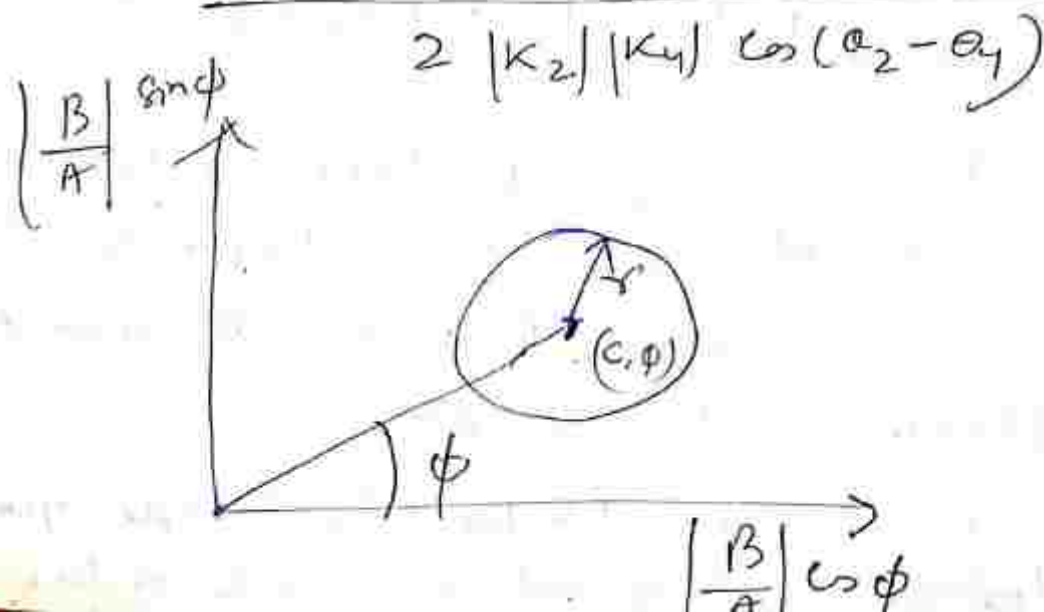
$$\begin{aligned} \sin \alpha \cdot \sin \phi &= \frac{\cos(\alpha - \phi) - \cos(\alpha + \phi)}{2} \\ &= \frac{\cos(\alpha_2 - \phi - \phi_1 + \phi) - \cos(\alpha_2 - \phi - \phi_1 + \phi)}{2} \\ &= \frac{2 \cos(\alpha_2 - \phi_1)}{2} \\ &= \cos(\alpha_2 - \phi_1) \end{aligned}$$

The above equation represents a circle with radius.

$$r = \frac{\sqrt{|k_1|^2 |k_4|^2 + |k_2|^2 |k_3|^2 - 2|k_1| |k_3| |k_4| \cos(\alpha_2 - \alpha_4)}}{2 |k_2| |k_4| \cos(\alpha_2 - \alpha_4)}$$

The co-ordinate of the centre (c, ϕ) , where

$$c = \frac{|k_1|^2 |k_4|^2 + |k_2|^2 |k_3|^2 + 2|k_1| |k_2| |k_3| |k_4| \cos(\alpha_2 - \alpha_4)}{2 |k_2| |k_4| \cos(\alpha_2 - \alpha_4)}$$



General Equation for Electromagnetic Relay

The equation of the relay characteristic Φ at the threshold condition of operation under steady state condition, it will be treated as circle on a complex plane.

The equation can be represented in general form

$$K|A|^2 - \frac{K'|B|^2}{\text{Current}} + \Phi|A||B| \cos(\phi - \theta) - K'' = 0$$

$$\frac{K|A|^2}{-2A|B|C \cos(\phi - \theta)} + \frac{K''}{+2A|B|K_3 \cos(\phi - \theta)}$$

Positive quantity
involves torque

$|A|$ & $|B|$ — Two quantities being compared ✓

ϕ = electrical angle between A & B

θ = Relay characteristic angle

K & K' — Scalar constant

K'' — Mechanical Restraining torque constant

✓ A is the ~~voltage~~ current & B is the voltage

$$K|I|^2 - K'|V|^2 + |V||I| \cos(\phi - \theta) - K'' = 0$$

Current winding produce a torque KI^2 and potential winding a torque $K'V^2$.

The interaction of voltage & current produce a torque $V I \cos(\phi - \theta)$

K'' is ~~some~~ finite only single quantity relay, where it is used as level

indicator, θ is negligible small.
 so $k'' = 0$

Divide by $k' |I|^2$ in equation.

$$\frac{k}{k'} - \left| \frac{V}{I} \right|^2 + \left| \frac{V}{I} \right| \frac{\cos(\phi - \theta)}{k'} = 0$$

$$\left| \frac{V}{I} \right|^2 - \left| \frac{V}{I} \right| \frac{\cos(\phi - \theta)}{k'} + \left| \frac{1}{2k'} \right|^2 = \frac{k}{k'}$$

$$\therefore = \left| \frac{k}{k'} \right| + \left| \frac{1}{2k'} \right|^2$$

~~$$\sigma = \sqrt{\left| \frac{1}{2k'} \right|^2 + \left| \frac{V}{I} \right| \frac{\cos(\phi - \theta)}{k'}}$$~~

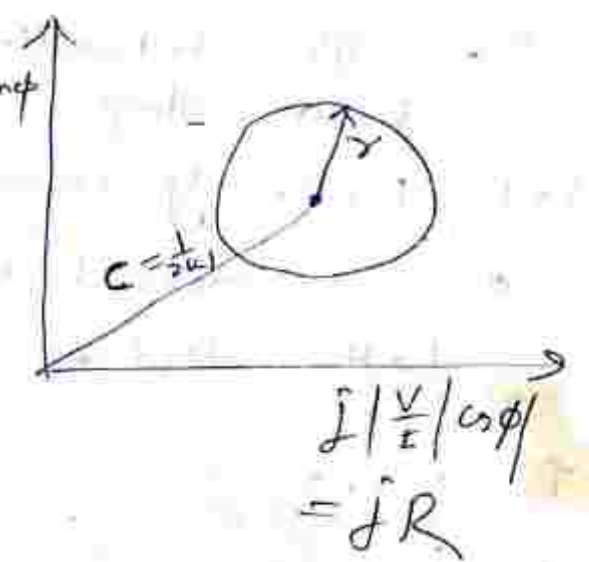
$$\sigma^2 = \frac{k}{k'} + \left| \frac{1}{2k'} \right|^2$$

$$= \frac{k}{k'} + \frac{1}{4k'^2} = \frac{k \cdot 4k'^2 + 1}{4k'^2}$$

$$\sigma = \frac{\sqrt{1 + 4k k'^2}}{2k'}$$

$$c = \sqrt{x^2 + y^2}$$

$$c = \frac{1}{2k'} = \int X$$



Over current relay :-

(A) Depending the time of operation the relay are categorized (i) Instantaneous over current relay (ii) Inverse time over current relay (iii) Inverse definite minimum time (iv) Very inverse relay (v) Extremely inverse.

(i) Instantaneous over current relay

- It has no time delay operation.
- The time of operation is approximately 0.1 sec.
- The characteristic is achieved by hinged type relay.

(ii) Inverse-time current relay:-

- operating time reduces as actuating quantity increases.
- This characteristics can be obtained with induction type relay by using suitable core.

(iii) Inverse definite minimum type current relay

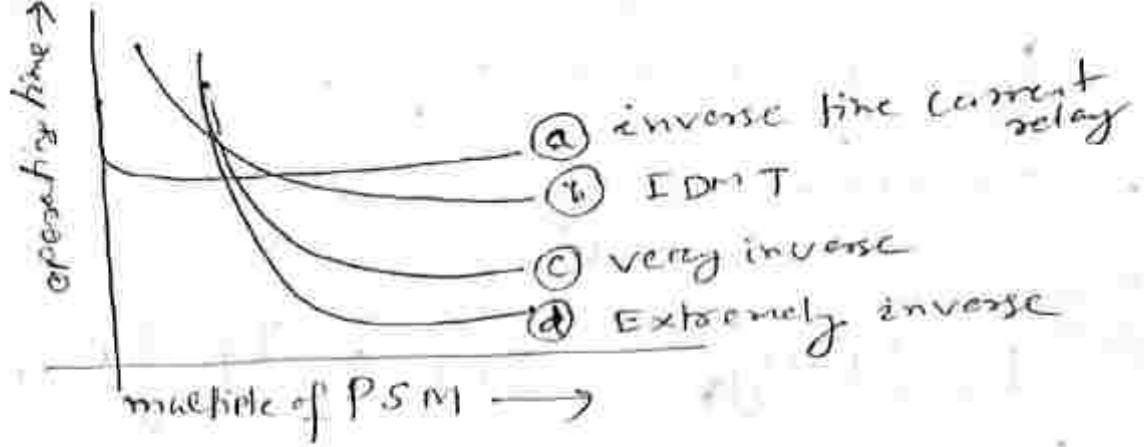
- The operating time is approximately inversely proportional to the fault current.

(iv) very inverse relay:-

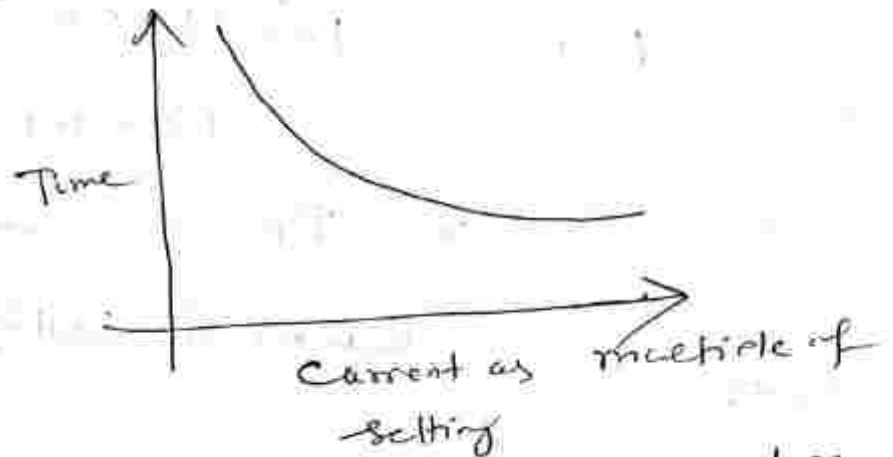
- The saturation of core occurs at a latter stage.

(v) Extremely inverse

- It is one in which the saturation occurs at a latter stage.



Time current characteristics



- ✓ Pick up adjustment is by coils (induction type relay)
- ✓ Ampere turn at pick up are same for each tap.

~~at different gaps~~

For a given multiple of pick up, the ampere turn and hence the torque are same.

- ✓ multiple of pick up should not less than 1.5.

- ✓ Inverse time current relay are non directional relay. They are use in feeders transmission line, transformer machine.

I_f = fault current

$$CT \text{ ratio} = \frac{x}{y}$$

$$I_R \text{ (Relay Current)} = \frac{I_f \times y}{x}$$

(iii) Current setting multiplier (PSM)

$$PSM = \frac{\text{fault current in relay}}{\text{pick up value.}} = \frac{I_R}{I_p}$$

Current setting \times rated secondary current

$$\frac{\frac{I_f \times y}{x}}{\frac{I_p}{100} \times 100}$$

$$= \frac{I_R \checkmark}{\frac{I_p}{100} \times 100}$$

I_p = Per unit current setting of the relay

$$\frac{I_p}{100} \times y = \frac{I_R \times 100}{I_p \times y} = \frac{I_f \times y}{x \times I_p \times y} = \frac{I_f \times 100}{x \times I_p \times y}$$

Problem : - An IDMT type overcurrent relay

is used to protect feeder through 500/1 CT. The relay has PS of 125% and TMS = 0.3. Find the time of operation of the said relay if a fault current of 5000 A flows through the feeder.

PSM : 2 3 5 8 10 15

Time for unity TMS : 10 6 4.5 3.2 3 2.5

(100% current = 2A)

$$\text{Relay current } I_R = \frac{I_f}{\text{CT ratio}} = \frac{5000}{500} = 10\text{A}$$

Pick up value of relay = Current setting \times ratio
 secondary current of CT

$$= \frac{125}{100} \times 1 = 1.25\text{A}$$

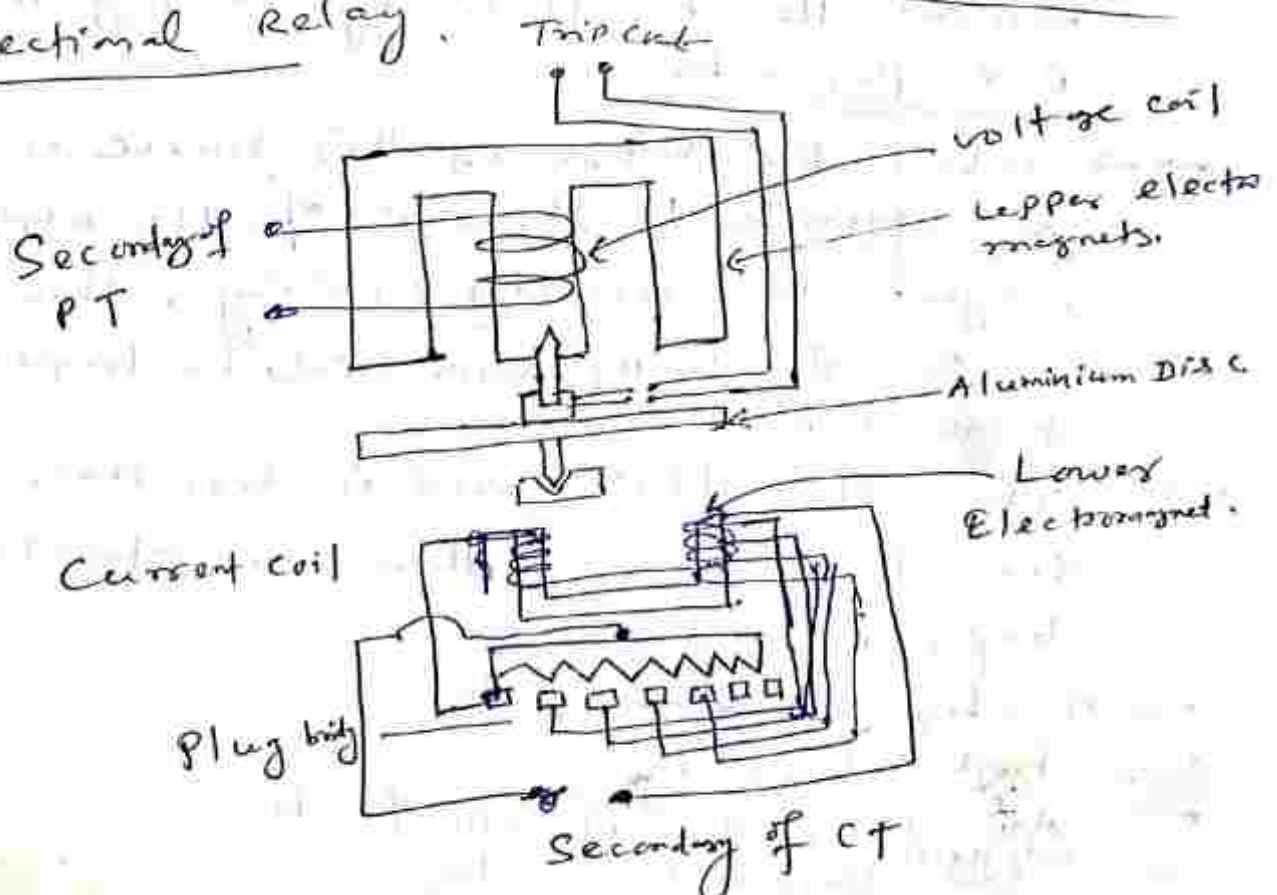
Plug setting multiplier PSM = $\frac{\text{Fault current of relay}}{\text{Pickup value of relay}}$

$$= \frac{10}{1.25} = 8$$

for given PSM = 8, time of 3.2 sec.

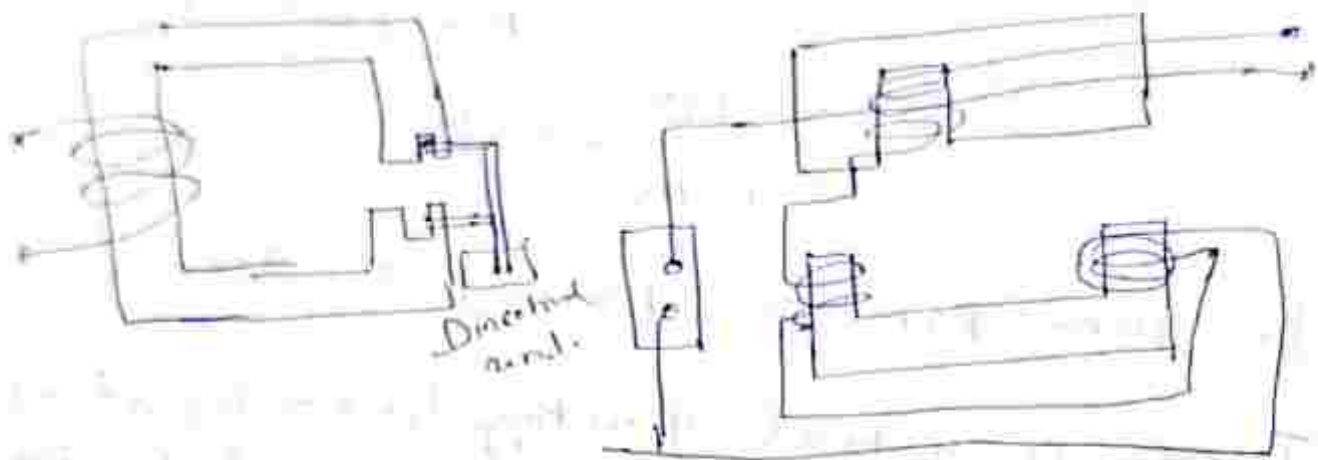
Time \Rightarrow actual operating time = 3.2 \times time multiplier setting
 $= 3.2 \times 0.3 = 0.96\text{ sec.}$

Directional Relay



Direction Relay

- In ring or loop system as well as ring main system, the gradual overcurrent protection cannot give proper protection.
- The directional features achieved by induction disc type overcurrent relay with split phase magnet in addition with directional unit. The directional unit consists of resistance & capacitance.



- The directional unit controls the angle between the two fluxes by varying the R-X parameter.
- when the voltage of this source is equal & opposite to the o/p of the upper magnet of secondary winding, there is no current in the lower coil, no torque is produced.
- If it opposes and is less than the secondary output, there is an opposing torque.
- → It has high speed operation.
- High sensitivity.
- At low voltage it will operate ^{adequately} thermal time taking.

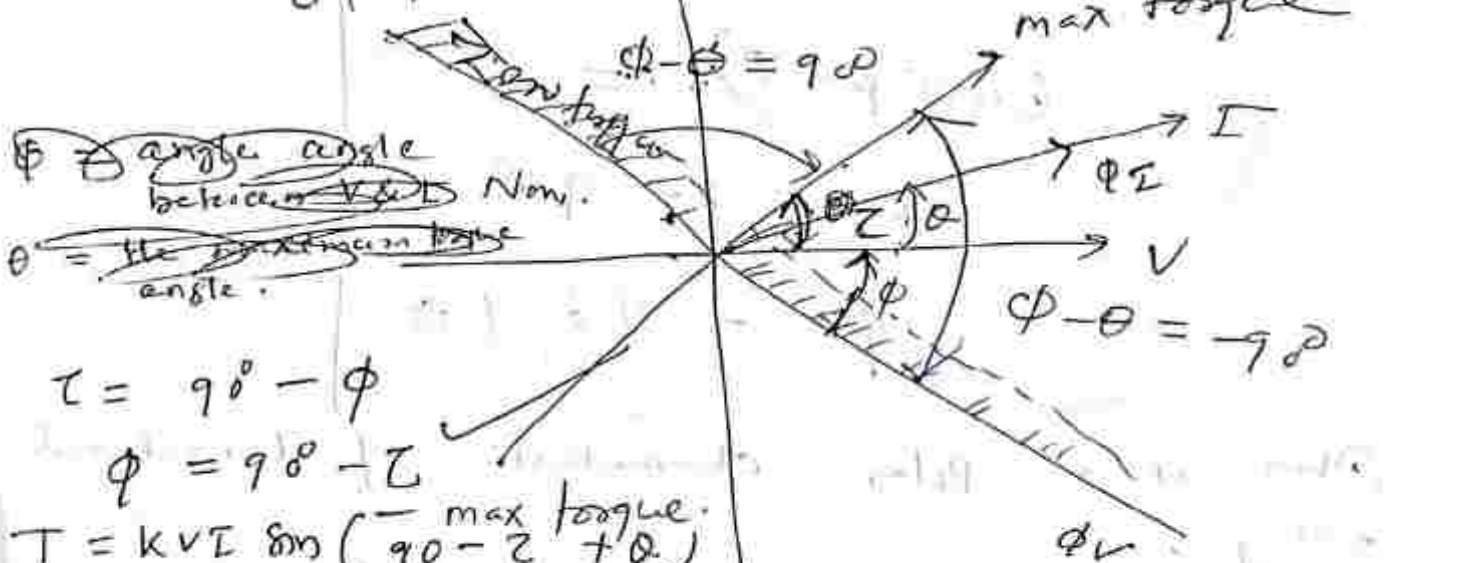
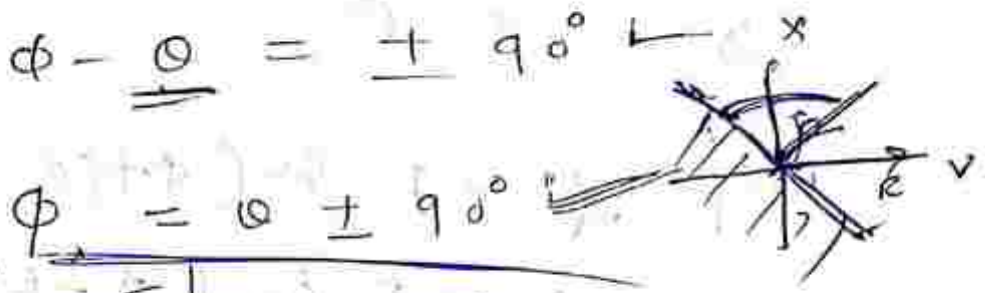
Single Phase Directional Relay

The modification of general equation $k|A|^2 & k'|B|^2$ is eliminated. considering voltage current directional relay

$$V I \cos(\phi - \theta) - k'' = 0$$

The spring constant k'' has no function.

$T \propto d\phi \propto \sin(\phi + \theta)$
 $T = k V I \sin(\phi + \theta)$
 $\phi + \theta = 90^\circ$
 Zero torque $\sin(\phi + \theta) = 0$
 $\phi + \theta = 0^\circ$ or 180°
 0 Torque.



$\tau = 90^\circ - \phi$
 $\phi = 90^\circ - \tau$
 $T = k V I \sin(90 - \tau + \theta)$
 $= k V I \cos(\theta - \tau)$
 When $\theta = \phi$ max. torque occurs. In a voltage current directional relay θ will not 90° . If the impedance angle of potential coil is λ .

$$\begin{cases} \theta = 90 - \lambda \\ \theta + \lambda = 90 \end{cases} \quad \begin{cases} V I \cos(\theta - \tau) \\ = 0 \\ \theta - \tau = 90 \end{cases}$$

$\phi_v =$ main flux due to voltage coil $\theta = \tau + 90^\circ$
 $\phi_i =$ flux due to current coil

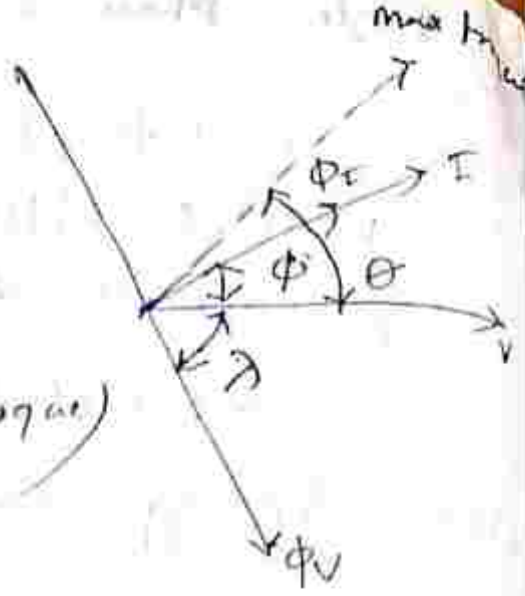
$$\underline{\text{Torque}} \propto \Phi_v \Phi_t \sin(\lambda + \phi)$$

$$T \propto k V I \sin(\lambda + \phi)$$

when $\lambda + \phi = 90^\circ$ (max. torque)

$$\theta = 90^\circ - \lambda$$

$$\lambda = 90^\circ - \theta$$



$$T \propto V I \sin(\phi + 90^\circ - \theta)$$

$$\propto V I \cos(\phi - \theta)$$

$$\cos(\phi - \theta) = 0$$

$$\phi - \theta = 90^\circ$$

$$\phi = 90^\circ + \theta$$

This is a polar characteristic of directional relay.

If the current phasor crosses the dotted line the opposing torque exceeds the spring torque and hence the relay operates.

$$\left\{ \begin{array}{l} \theta + \phi = 90^\circ \\ \phi = 90^\circ + \theta \end{array} \right.$$

$\phi = 90^\circ + \theta$
 $\theta = 90^\circ - \phi$

Distance relay

The distance relay has classified (i) Impedance relays (ii) reactance relays (iii) mho relays.

Impedance relay:-

This is a device which measures distance by comparing the fault current I with the voltage V across the fault loop. The amplitude comparator and balanced beam structure is most common.

The equation of amplitude comparator

$$\underbrace{(K_1^2 - K_3^2)}_{K_1} |A|^2 + 2|A||B| \left\{ K_1 K_3 \cos(\theta_2 - \phi) - K_3 K_4 \cos(\theta_4 - \phi) \right\} + \underbrace{(K_2^2 - K_4^2)}_{K_2} |B|^2 = 0$$

$$T = K_1 I^2 - K_2 V^2$$

operating torque is produced by current coil and restraining torque produced by voltage coil. So impedance relay is voltage restrained over current relay.

For proper operation of the relay, the operating torque should be greater than the restraining torque.

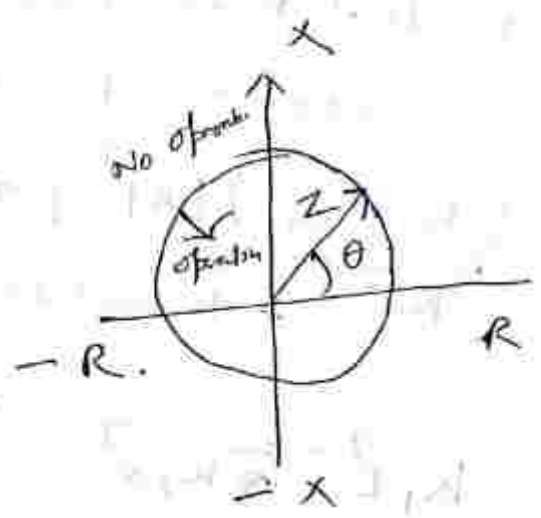
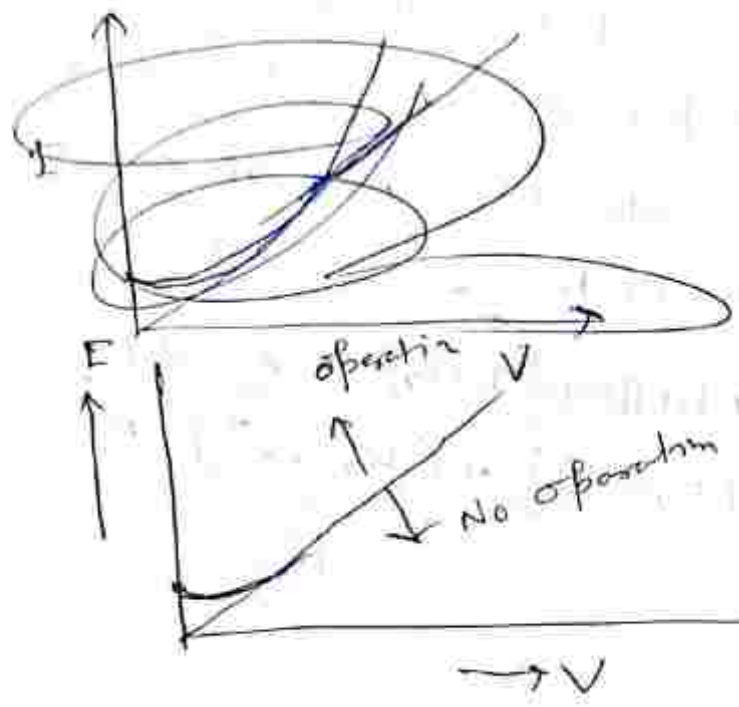
$$K_1 I^2 > K_2 V^2$$

$$\frac{V^2}{I^2} < \frac{K_1}{K_2}$$

$$Z < \sqrt{\frac{K_1}{K_2}}$$

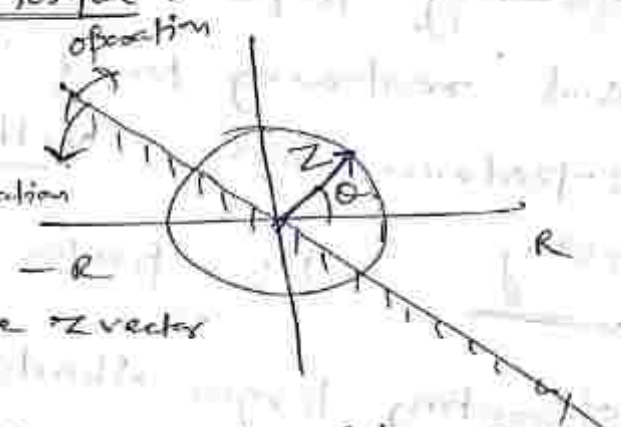
$$Z < \text{constant (design impedance)}$$

This means that the impedance relay will operate only if the impedance seen by the relay is less than a preselected value. At threshold condition

$$Z = \sqrt{\frac{K_1}{K_2}}$$


The initial bend in the characteristics is due to the presence of spring torque.

In case two were in phase, the Z vector coincides with +R axis. When current lags the voltage by 180°, the Z vector coincides with -R axis.



When I lags behind V, the Z vector lies in the upper semicircle. This relay is non-directional.

These relays may use balance beam structure or induction cup structure.

Reactance relay:- In this relay the operating torque is obtained by current and restraining torque due to current-voltage directional element, so, a reactance relay is an overcurrent with directional restraint. The directional element is so designed that its maximum torque angle is 90° i.e. $\theta = 90^\circ$

$$T = K_1 I^2 - K_3 V I \cos(\phi - \theta)$$

$$= K_1 I^2 - K_3 V I \cos(\phi - 90^\circ)$$

$$= K_1 I^2 - K_3 V I \sin \theta$$

For the operation of the relay

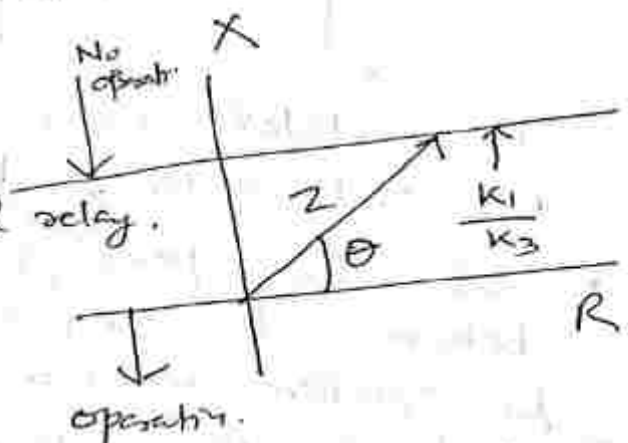
$$K_1 I^2 > K_3 V I \sin \theta$$

$$\frac{V I}{I^2} \sin \theta < \frac{K_1}{K_3}$$

$$Z \sin \theta < \frac{K_1}{K_3}$$

$$X < \frac{K_1}{K_3}$$

It is a non-directional relay.



Mho relay: - In this relay the operating torque

is obtained by the $V-I$ element and restraining torque due to the voltage element. This means

a mho relay is a voltage restrained directional relay. Mho relay is high speed relay & known as admittance relay.

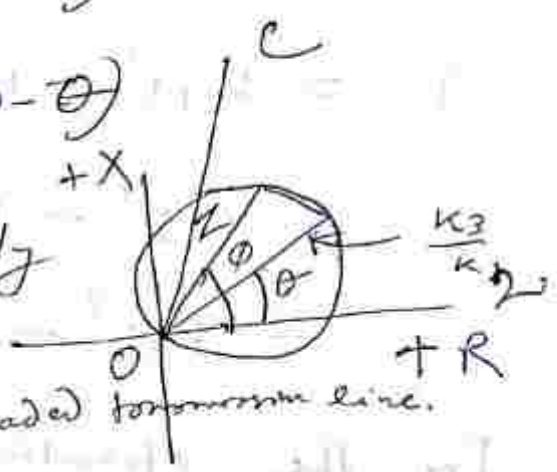
$$T = K_3 V I \cos(\phi - \theta) - K_2 V$$

For the relay operates $K_3 V I \cos(\phi - \theta) > K_2 V$

$$\frac{V^2}{V I} < \frac{K_3}{K_2} \cos(\phi - \theta)$$

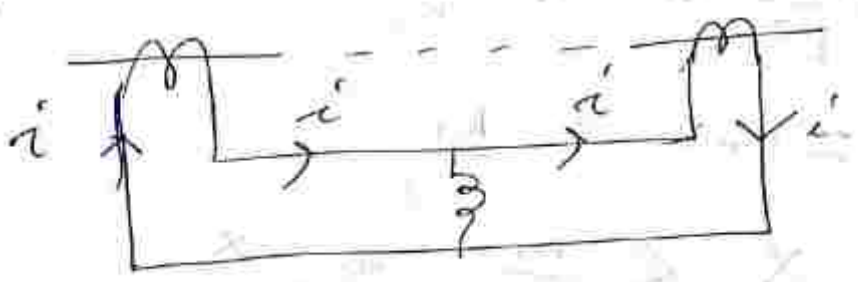
$$Z < \frac{K_3}{K_2} \cos(\phi - \theta)$$

* This relay is inherently directional.



* Mho relay is suitable for long EHV/UHV heavily loaded transmission line. Differential relay.

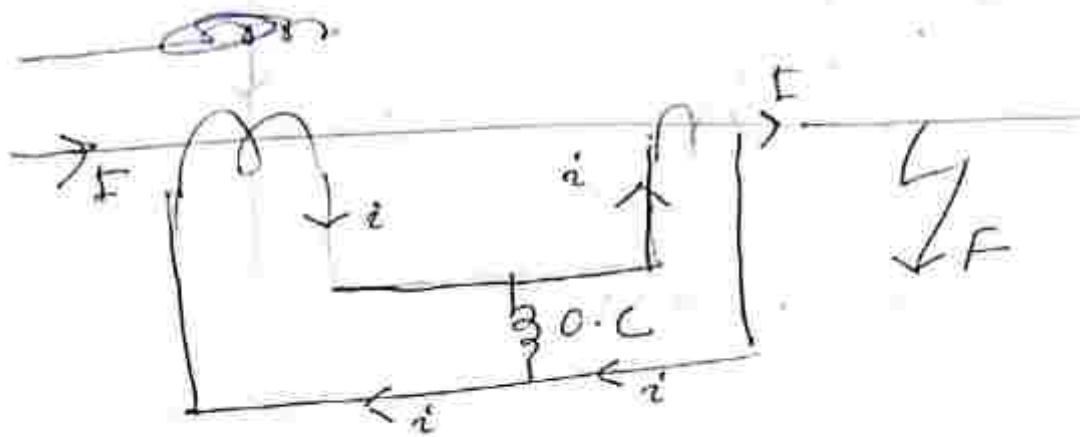
- The vector difference of two vectors similar quantity when exceeds a predetermined value, relay operates



The dotted line represents (a) transformers, an alternator, bus.

- If the operating coil is not connected between the equipotential point, there will be difference current through the operating coil of the relay and this may result in maloperation of the relay.

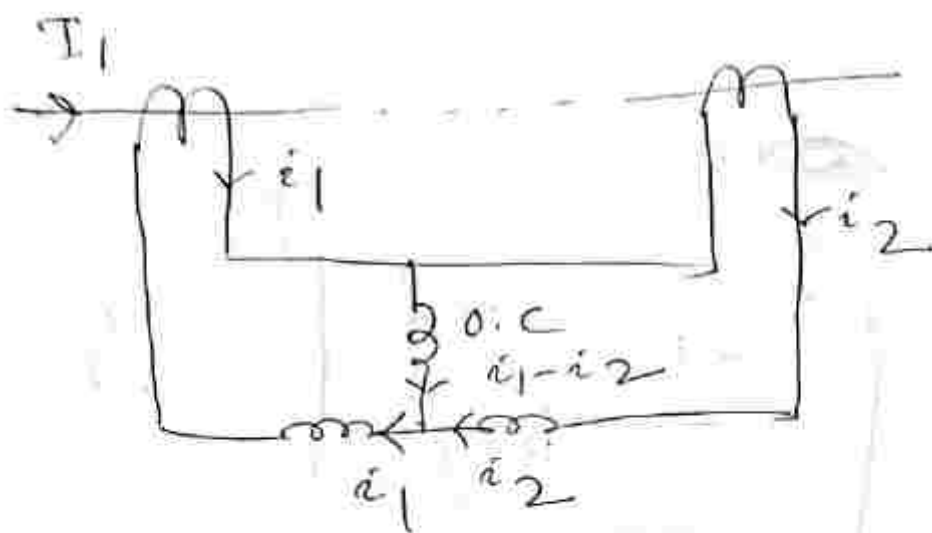
if the burden of the two CT is unequal, the heavily loaded CT will saturate during through fault. Causing different characteristics of the two CT. So that, there is dissimilarity in the characteristics of the two CT's which results in misoperation of the relay.



The desirable feature of this relay is that when there is a fault in the outside, relay does not operate. If the two CT are identical and playing the same secondary current, for interfault situation, the relay coil operate. The form of protection is known as merge-price protection.

Under transient condition, the CT do not transform their current accurately. Two CT under normal condition differ their magnetic properties slightly in terms of different residual magnetism or unequal burden on the two CTs. In the result, one CT will saturate earlier or during short circuit.

This case is validated with transformer. The
 Merz-price protection is modified
 by biasing the relay. This is known as
 biased differential protection or percentage
 differential protection is used.



The relay consist of operating coil and restraining
 coil. The operating coil is connected to
 mid point of restraining coil. ~~But~~ but
 owing to the dissimilarities in CTs, the
 differential current through the operating
 coil is $(i_1 - i_2)$ and equivalent current
 in the restraining coil is $(i_1 + i_2) / 2$

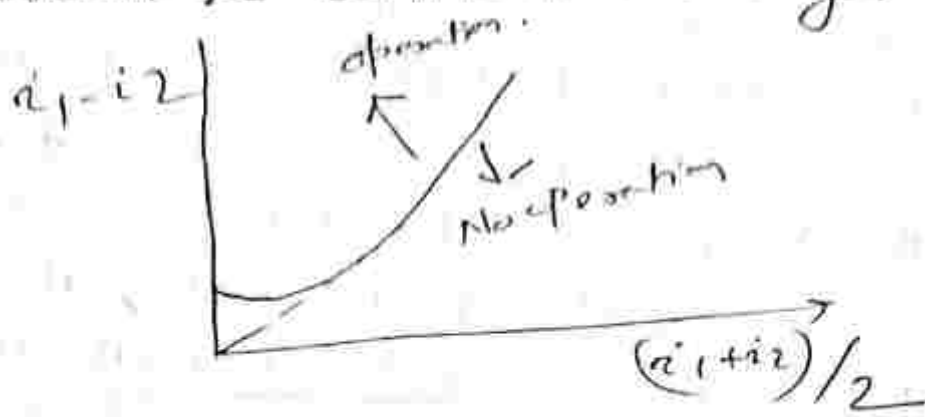
Operating coil torque $T_o \propto (i_1 - i_2) n_o$

Restraining coil torque $T_r \propto \frac{(i_1 + i_2) n_r}{2}$

At balance $\frac{(i_1 + i_2) n_r}{2} = (i_1 - i_2) n_o$

$$\frac{n_r}{n_o} = \frac{i_1 - i_2}{(i_1 + i_2) / 2}$$

The ratio of differential operating current to the average restraining current is a fixed percentage. This is why it is known as percentage differential relay.



Feeder protection

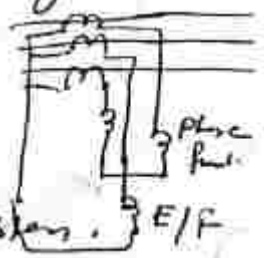
- ① Overcurrent protection → backup
- ② Distance protection → primary
- ③ Pilot relaying protection

In a distribution circuit ~~relay~~ non-directional relay is used,

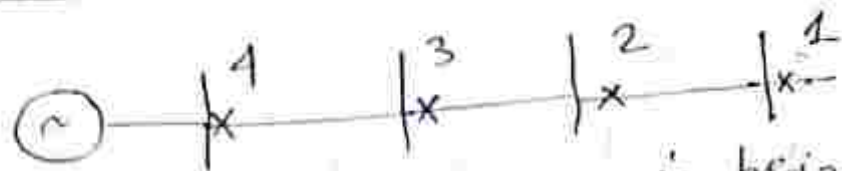
Two phase and one earth fault relay are required for complete protection of the ^{three phase} ~~system~~ _{area}
Overcurrent protection is used for phase and ground fault on station serving distribution cells
Overcurrent protection used as backup protection

The discrimination using overcurrent protection is used in the following way. 3PEN

- ① Time graded system
- ② Current graded system
- ③ Time current graded system. } E/F



Time graded system: -



This is a radial feeder line is being fed from one source. The time of the relay is so adjusted that the relay farthest from the source will have minimum time of operation. Near the source, the operating time increases.

The main disadvantage point is that the fault current does not vary much with the location of fault and inverse characteristics does not apply. Time graded system is normally employed for backup protection in large transmission system.

Current graded system: - This type of grading

is done on a system where the fault current varies appreciable with the location of the fault. The current nearer to the source is highest. ~~More relay can~~ The set up value of the relay is highest, so that long time required for operation of the relay. In this system it is very difficult to determine the magnitude of current under fault condition.

Time & Current grading system

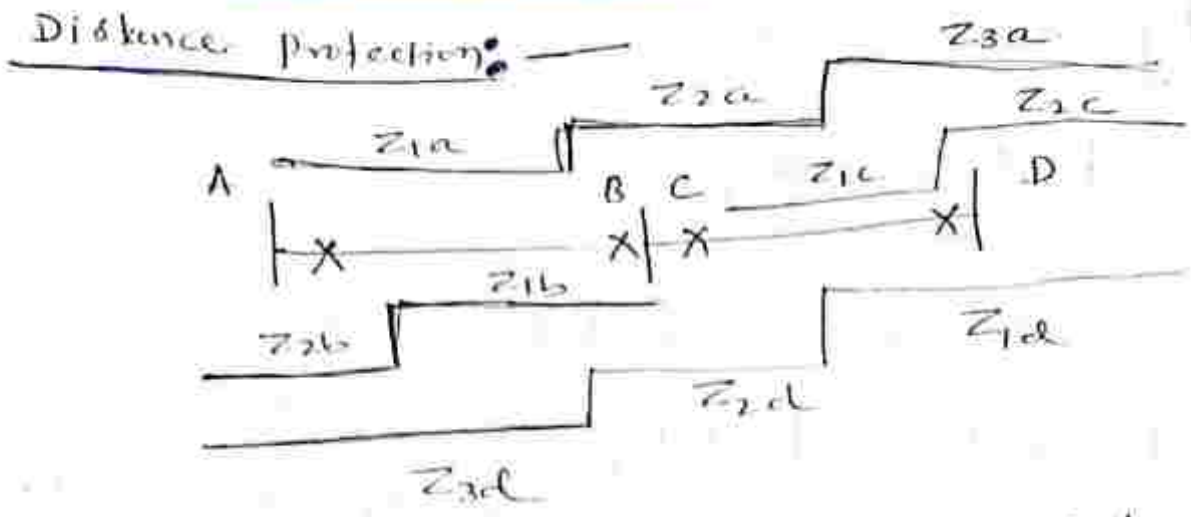
→ This type of grading is achieved with the help of inverse time over current relay and the most widely used. It EDMT relays are ~~not~~ slow at low values of current

extremely inverse relay are used.

Selection of Time Setting

In case of radial distribution line, the pick up value of relay is adjusted such that it will trip for all values of short circuit and it also provide for back up protection for adjoining line. The set up value of relay is equal to the current at the farthest end. Suppose B & fault, under ~~minimum~~^{maximum} generation gives the ~~minimum~~^{maximum} fault current and line to line fault under minimum generation gives minimum fault current. The relay must be ~~be~~ adjusted between these two extreme limits. The current setting of the relay farthest from the source should be minimum. According to Indian standard specification, the operating value should exceed 1.3 times the setting.

Min Short circuit current $> 1.3 \text{ Setting}$.



This protection scheme is divided into 3 Zones. AB & CD are the two line sections. The three zones are Z_{1a} , Z_{2a} , Z_{3a} . Z_{1a} covers 80% of the line AB and it is a high speed zone. No intentional time lag is provided for this zone.

Speed Zone at A covers remaining 20% length of the line AB and 20% of line CD. If fault will occur in this section relay at A will operate when the time elapsed corresponds to the ordinate Z_{2a} . The main idea of the second zone is to provide protection for the remaining 20% section of the line AB. In case of an arcing fault in section AB which adds to the impedance of the line as seen by the relay at A, the relay A will see the 2nd zone of protection. The operating time of 2nd zone is normally about 0.2 to 0.5 sec. The third zone at A provide back up protection for faults in the line CD, in some cases.

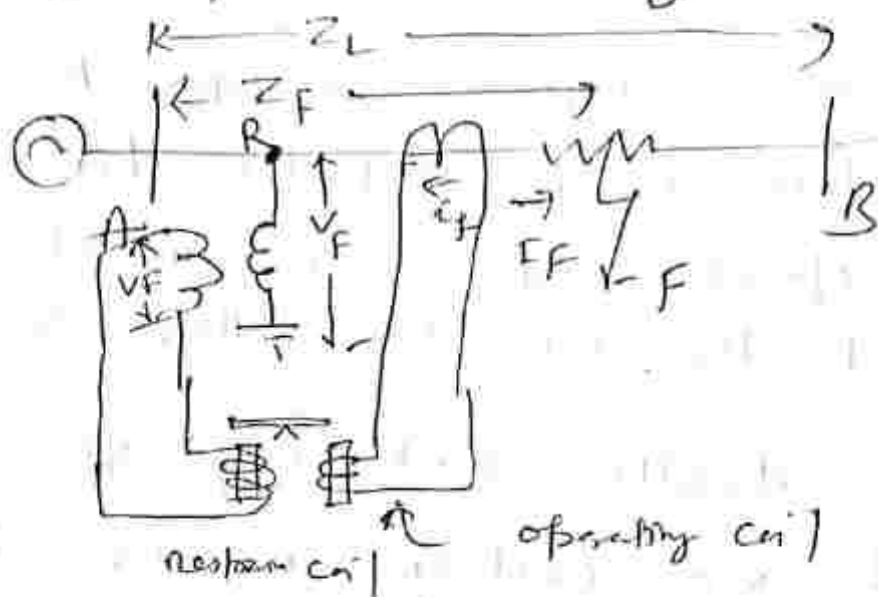
The relay at C fails to operate then the relay A will provide back up protection.

Distance Protection : —

The action depends on upon the distance of the feeding point to the fault. The time of operation of such protection is a function of the ratio of voltage & current. It is a double actuating quantity relay with one coil is energised by voltage and other coil by current. The current element produces positive value torque and ~~negative~~ voltage element produces negative value of torque. The relay operates only $\frac{V}{I}$ ratio falls below a predetermined value. The V/I ratio measured the location of CT & PT. Near the fault nearer to PT, voltage decreases and fault farthest from the CT, voltage increase. So, we maintain constant V/I ratio ~~for~~ measured from the relay location. Distance protection is a non-unit type protection.

Distance protection is a primary and back up protection. For higher clearing fault, distance relay used.

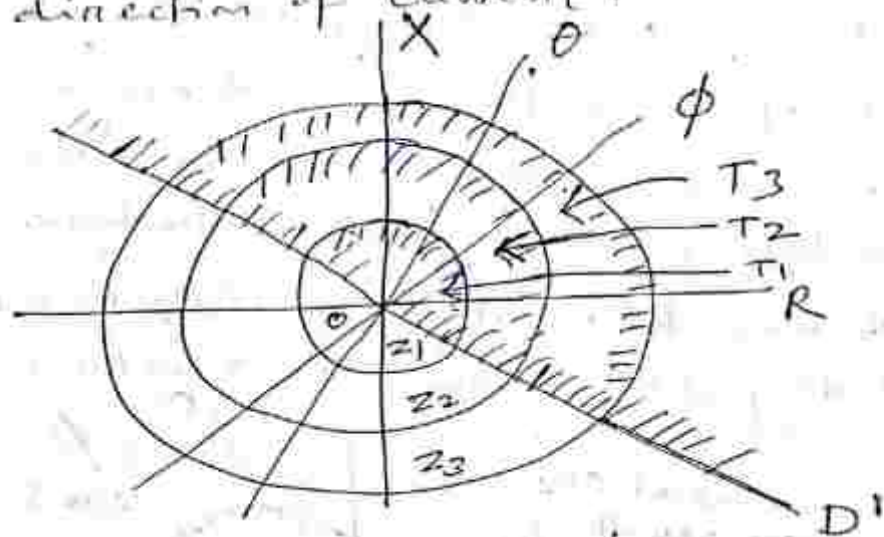
Principle of distance relay operates



The analysis of distance relay is governed by the ratio of voltage to current at the relay location. V_F / I_F . R is the point where relay connected and the two coils of the relay operating and restraining coils receive current I_F and V_F proportional to the fault current I_F . Below a particular value of $Z = V/I$ the relay operates.

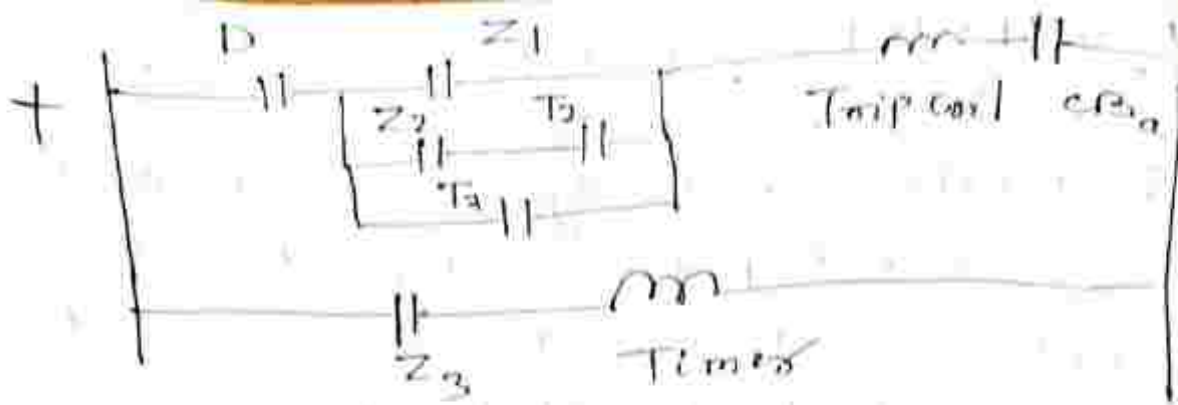
Distance Protection by Impedance Relay

Impedance is directly proportional to the length of line. Impedance relay which measures impedance can be used to recognize a fault condition and operate. It has no directional features and it will operate irrespective of the direction of current.



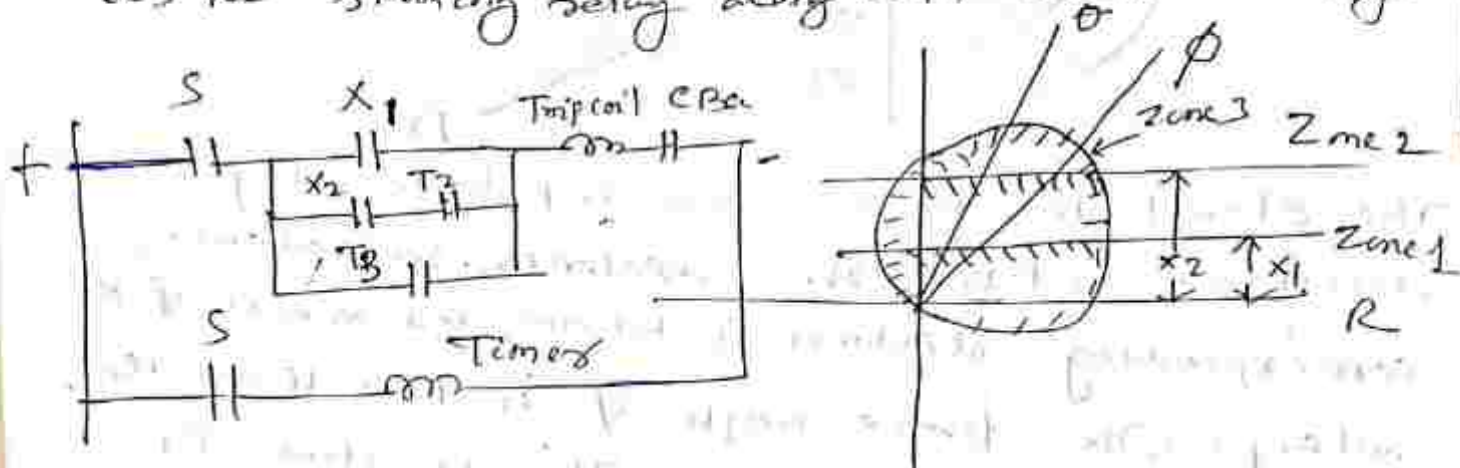
The characteristic for a 3 zone impedance relay with directional unit D' . The ~~distance~~ impedance corresponding distance is known as reach of the relay. The torque angle ϕ is less than the impedance angle θ . This is done in order to reduce the effect of ~~arc~~ ^{arc} resistance of the relay.

- The element Z_3 of Zone 3 controls the timer.
- The Zone 1 element operates without any intentional time delay, but still it has some finite time of operation T_1 , whereas Z_2 & Z_3 operates with a time delay of T_2 and T_3 respectively.



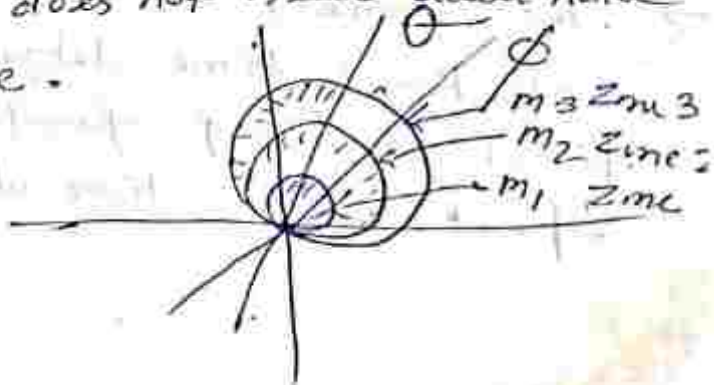
Distance protection by reactance relays

This type of relay responds only to the reactance component of the impedance. A reactance relay is a non-directional relay and the directional unit of the type used along the impedance relay can not be used. A mho relay is used as the starting relay along with reactance relay.

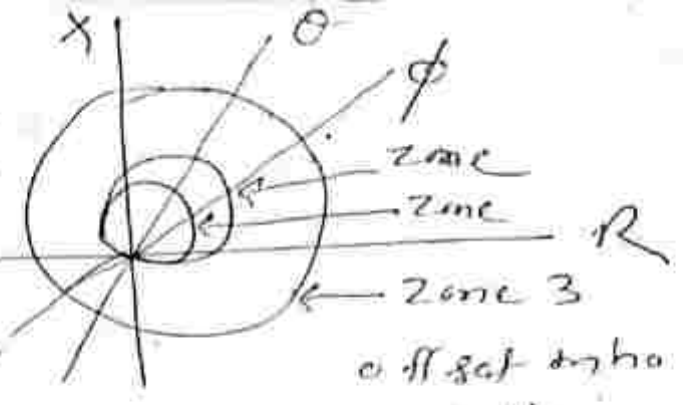


In case fault takes place 1st zone, all the three unit X_1 , X_2 and S block. The operation of X_1 takes less time, the contact X_1 is closed.

Mho relay :- Mho relay, inherently being a direction relay, does not need additional unit for the purpose.



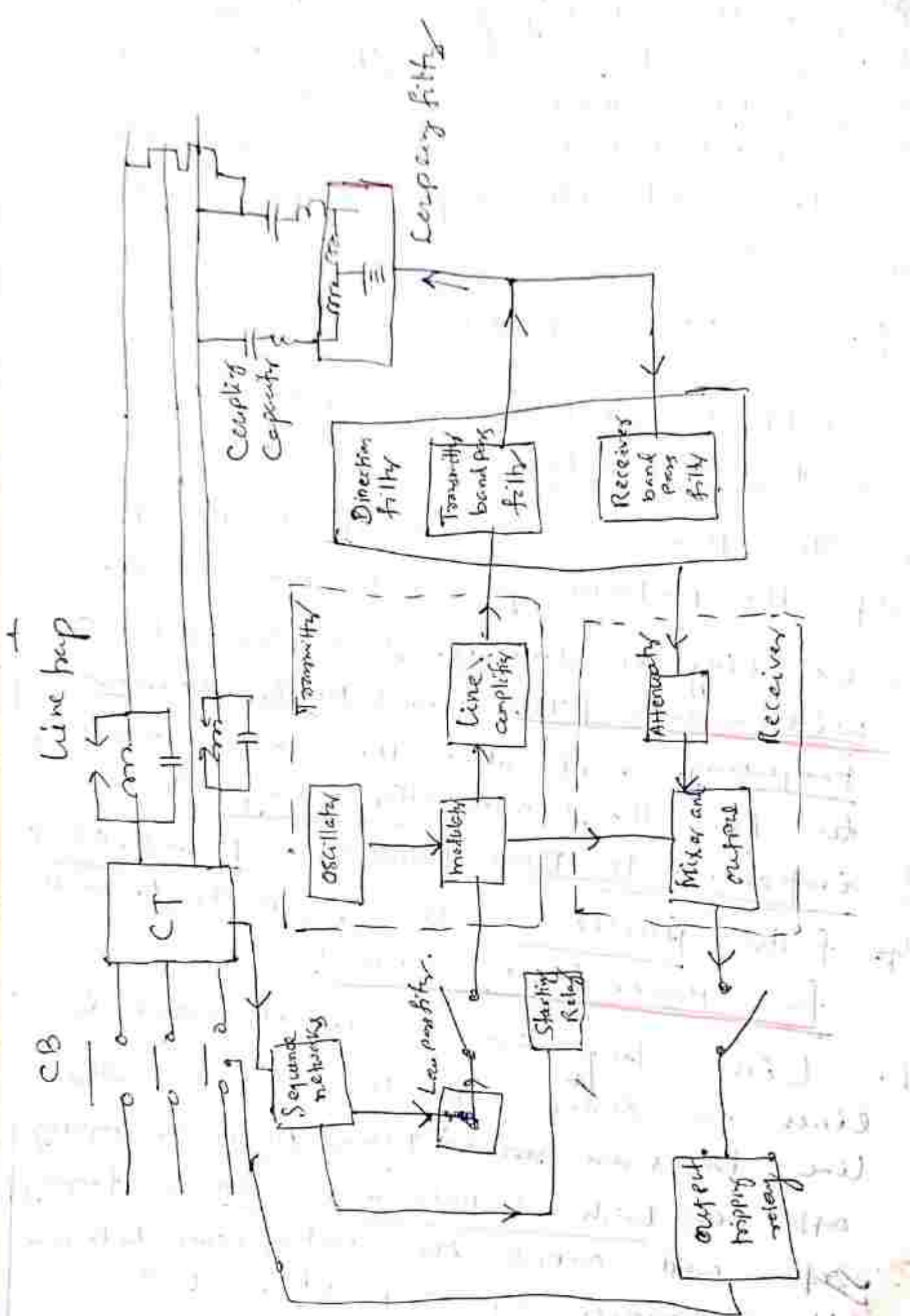
Zone 3 mho unit which act as blasting relay or for controlling the timer can also be replaced by an offset mho unit which has advantages under closed loop fault relay conditions.



offset mho relay

Pilot wire protection

1. Pilot wire protection is usually limited to 100 to 10 miles.
2. The prime consideration is the coupling of the protective gear to the power line.
3. Coupling is done through a series L-C wide-band filter tuned to the carrier frequency. It allows the carrier frequency to pass through and offer a very high impedance to power frequency. Parallel L-C filters provide a drainage path to earth for power frequency current.
4. Line traps are provided at overhead lines in series with the phases. The line traps are ~~provided~~ tuned to power frequency after a high impedance to carrier frequency. It will avoid the interference between the carrier signals of adjacent line.



CB

line pair

Coupling Capacitor

Coupling filter

Direction filter

Transmitting band pass filter

Receiving band pass filter

Oscillator

Line amplifier

Modulator

Attenuator

Receiver

Mixer and output

Starting Relay

output tripping relay

Sequence network

Low pass filter

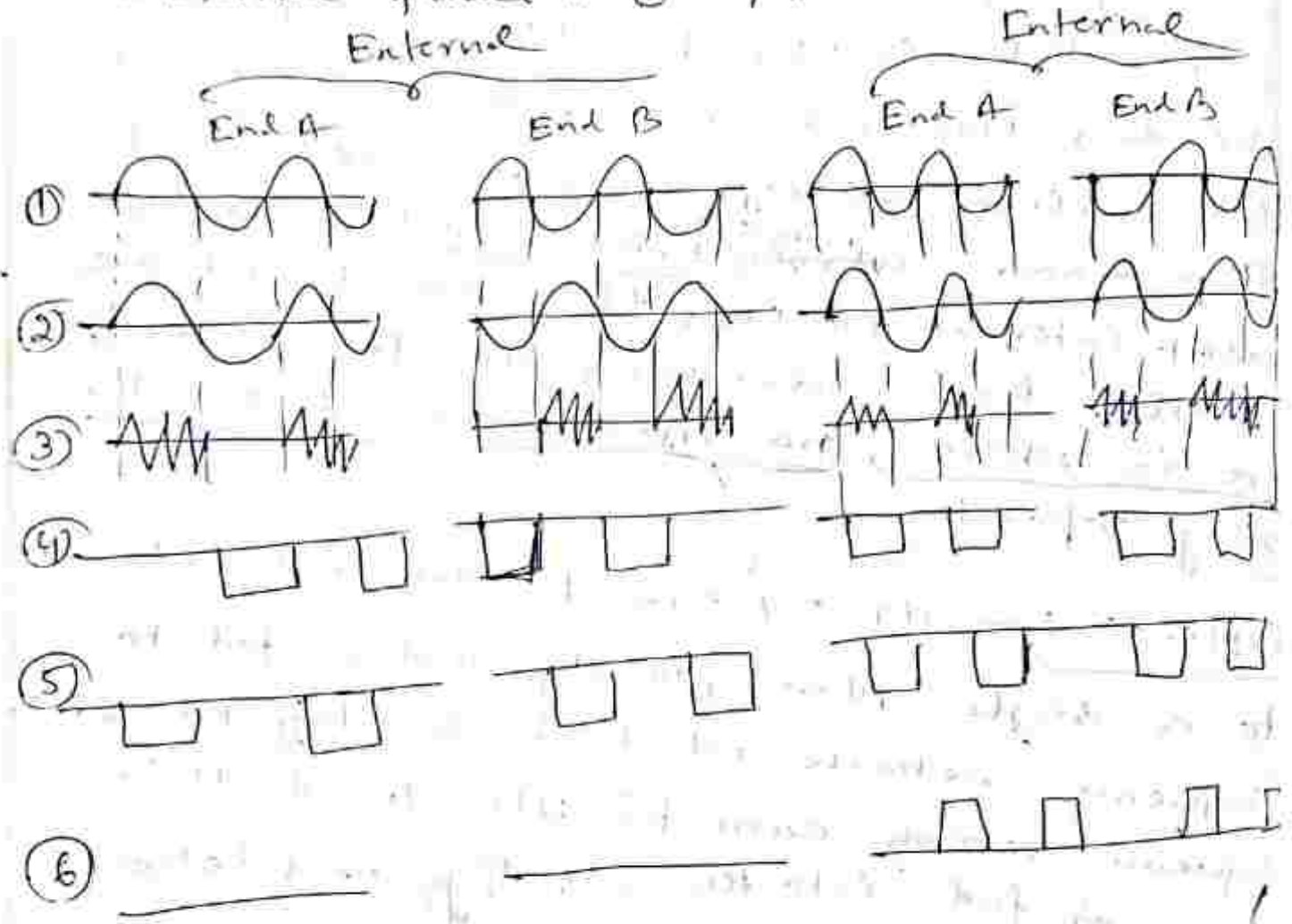
The signal is generated by transmitter consist of oscillator and amplifier with frequency 50 to 500 kHz.

Phase comparison scheme:-

The phase comparison block ^{scheme} will operate ~~the~~ relay whenever the carrier current signals are displaced in time. Under relay operation no signal is transmitted at both ends. For phase comparison scheme, the line CTs are so connected that their secondary currents are 180° out of phase under ~~internal~~ ^{normal} / external faults. Under ~~internal~~ ^{normal} / external faults under internal fault, the current at one end reverses, the two currents are in phase, no signal received and the relay operates.

Explanation:- (1) 3 ϕ currents are reduced to a single phase quantity and is fed to sequence network which is sensitive to negative sequence network current. The o/p of this network is fed into the ~~starting modulator~~ transmitter through a low pass filter. This 50 Hz modulator fed into the transmitter modulator ~~through~~ low pass filter. The o/p of the modulator is partly fed to the next and partly amplified by amplifier.

and feed to the line through band pass filter and coupling equipment. The transmitted signal enters the receiver circuit through receiver band pass filter. It is then attenuated and passed into the mixer circuit. This mixture circuit receives two signals, one from the local circuit and another from the end circuit. The phase relation of these signals is so arranged that it is 180° for normal operation of the system or external fault. 0° for internal fault.



- 1:- Primary current
- 2:- Secondary current
3. Transmitted signal
4. Received "
5. Locally derived signal
6. O/P.

MODULE- III

Generator protection

✓ Stator fault :- Phase to phase fault

(2) Phase to ground fault

(3) Inter-term fault

The phase to phase and interterm fault are less common are compared to the phase to ground fault.

✓ Rotor fault (1) ground fault or short cut between between the term of the field winding, cause severe mechanical and thermal stresses acting upon the winding insulation as

Abnormal running condn

(1) Unbalanced loading

(2) overloading

(3) overspeed

(4) overvoltage

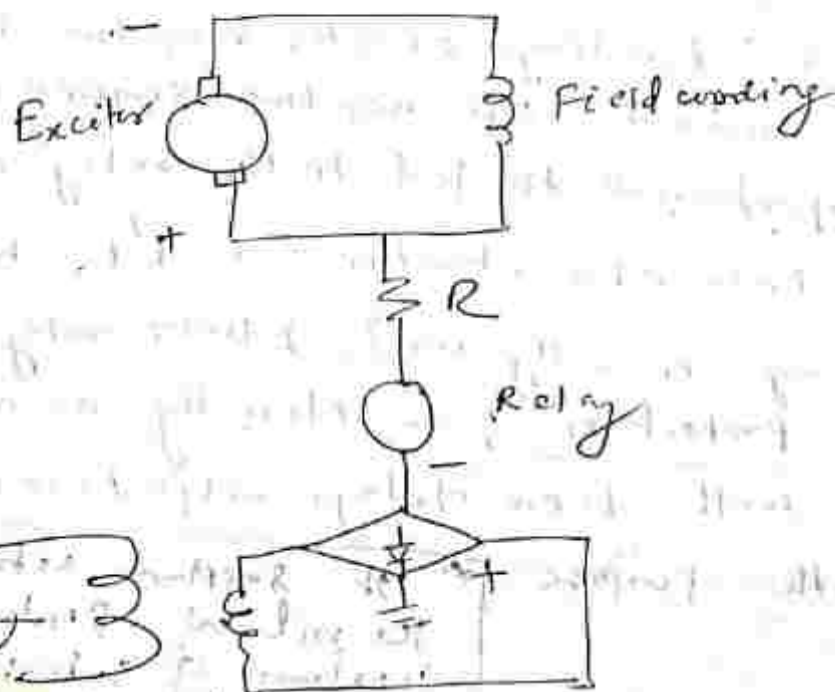
(5) failure of prime mover :-

(6) Loss of excitation

faulty operation of the voltage regulator.

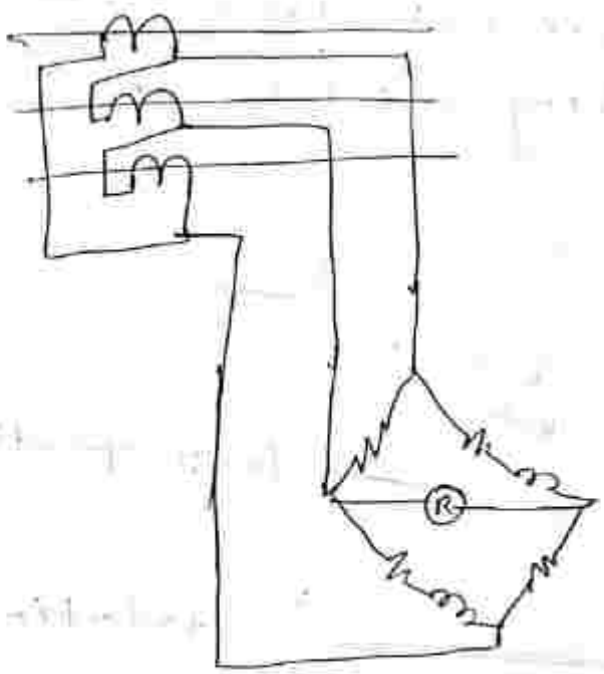
induction generator.

Rotor protection :-



Small power supply is connected to the positive pole of the field circuit. A fault detecting relay and a high resistance to limit the current are connected in series with this circuit. A fault occurs at any point on the field circuit will pass a current through the relay to cause relay operation. The earth fault relay coils are instantaneous and are connected to alarm circuit for indication.

Unbalanced Loading



Negative sequence relay

Unbalanced loading creates negative phase sequence current. The negative sequence current is proportional to feed to the relay with inverse square law characteristic, i.e. $I^2 t = K$ or $t = \frac{1}{I^2}$

The relay normally used IDMT relay.

Overload Protection :- Normally an overcurrent relay with time delay adjustment should serve the purpose

It supplies active power to the grid w/ operating heavy pf impedance of Inductor generally shift into Earth ground.

overspeed protection: — wattmetric relay is used.

The speed goes up whenever there is sudden loss of load.

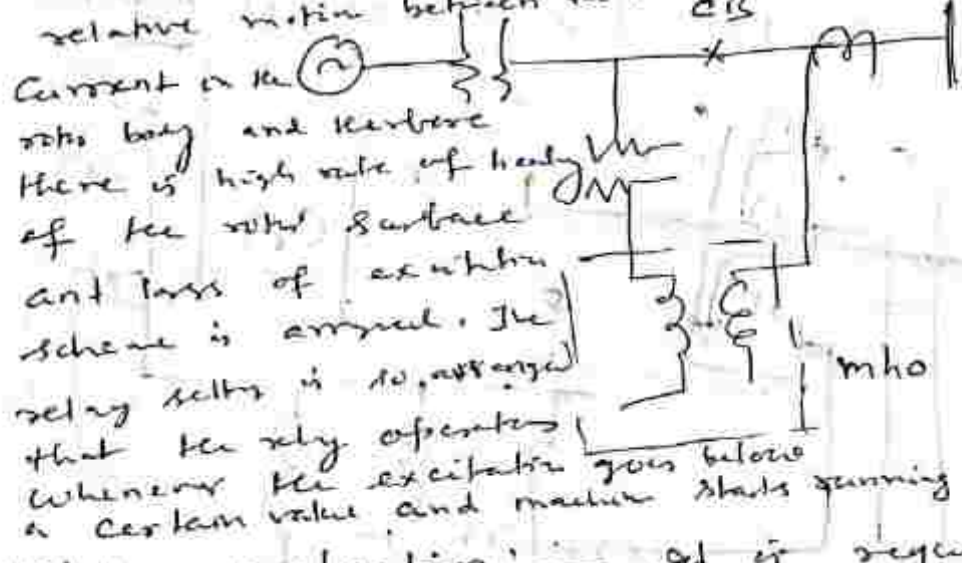
overvoltage protection: — a.c. overvoltage relay

is used which pick up voltage 110% of the normal value. The operation of the relay introduce resistance in the generator or exciter field circuit and if overvoltage persists.

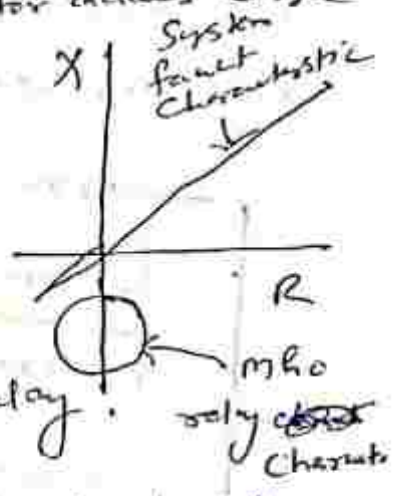
Failure of prime mover: — The wattmetric relay with directional characteristic is used.

Class of excitation: — off set mho relay is used for this case. A very large alternator

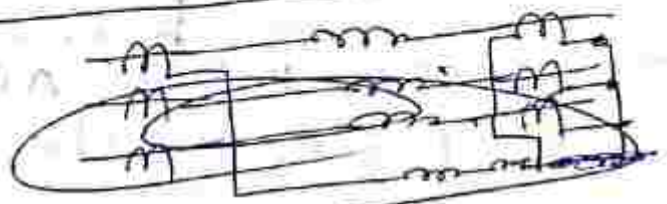
can not be allowed to run asynchronously for long as the relative motion between the stator field and rotor induces large



Current in the rotor bars and kerbars there is high rate of heating of the rotor surface and loss of excitation scheme is arranged. The relay setting is so arranged that the relay operates whenever the excitation goes below a certain value and machine starts running asynchronously.

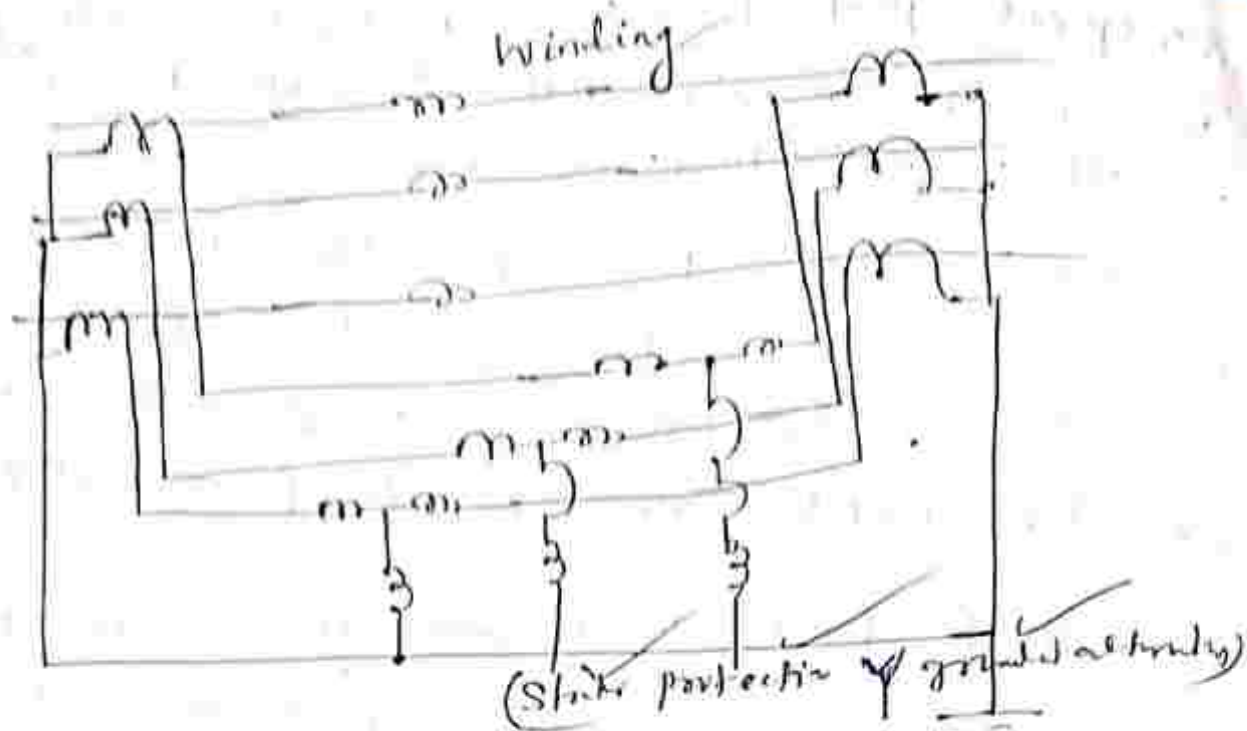


Stator protection: — It is required differential protection above 10 MVA



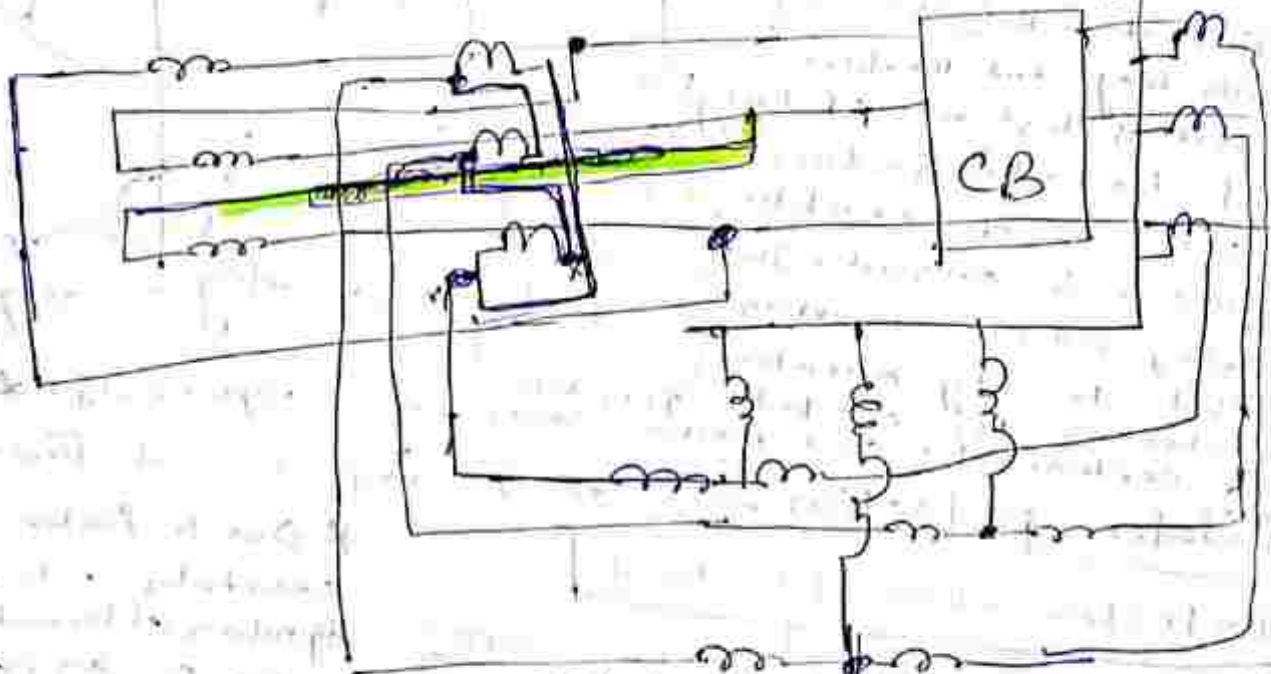
* Due to failure of excitation, the synchronous alternator now works as an induction generator and draws large reactive power from the grid, off course when a asynchronous

under normal operating condition alternator is connected to the grid it supplies active power to the system in addition to its power and pf. is lagging and impedance of the system is in first quadrant.



The percentage differential relay. It can be seen that for an external fault, the relay does not operate, and for internal fault it does operate.

In case the generator Δ connected, gives the scheme of percentage differential protection.

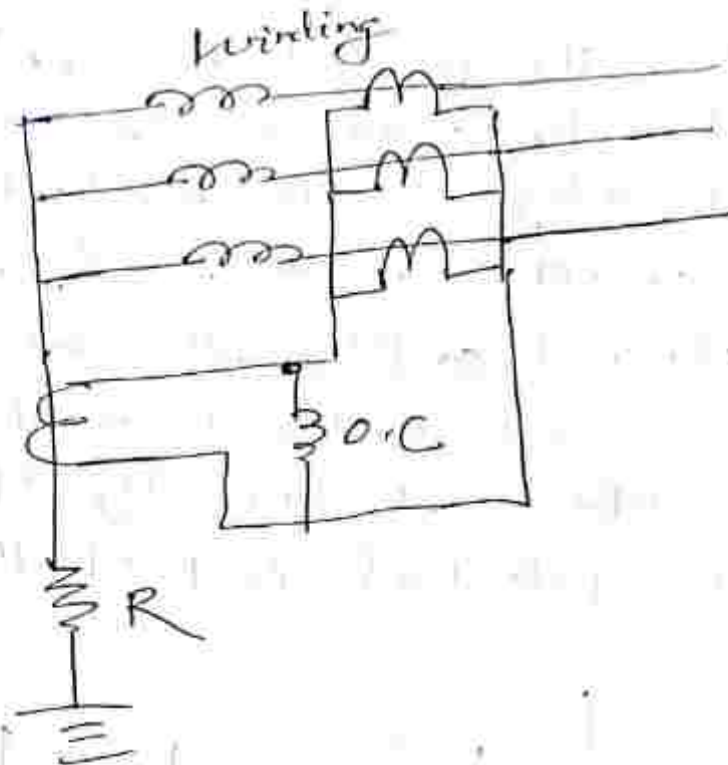


(Stator Protection Δ Connected) actually

Restricted Earth fault protection :-

If the stator part is not available because it is made inside the generator and it is grounded through some low-

impedance, Percentage differential relaying for ground faults only can be provided. This is known as restricted earth fault protection is used.



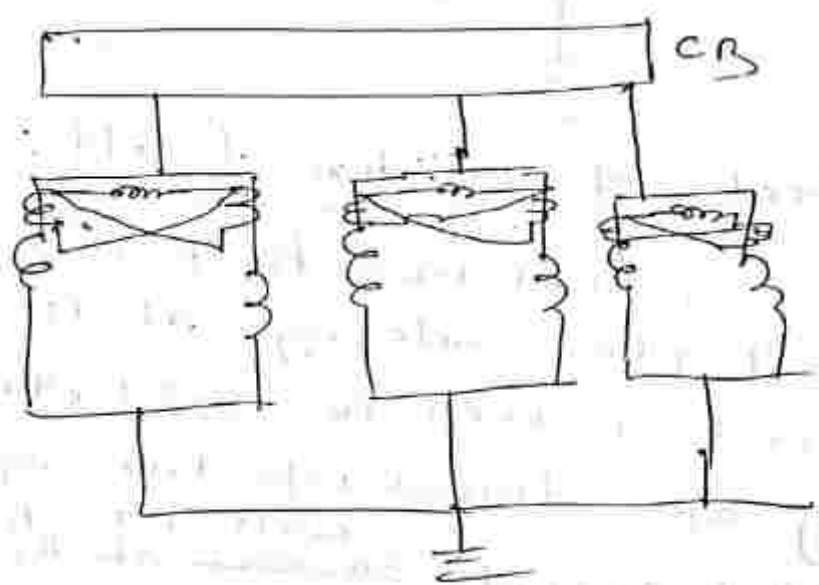
Protection of inter turn fault: -

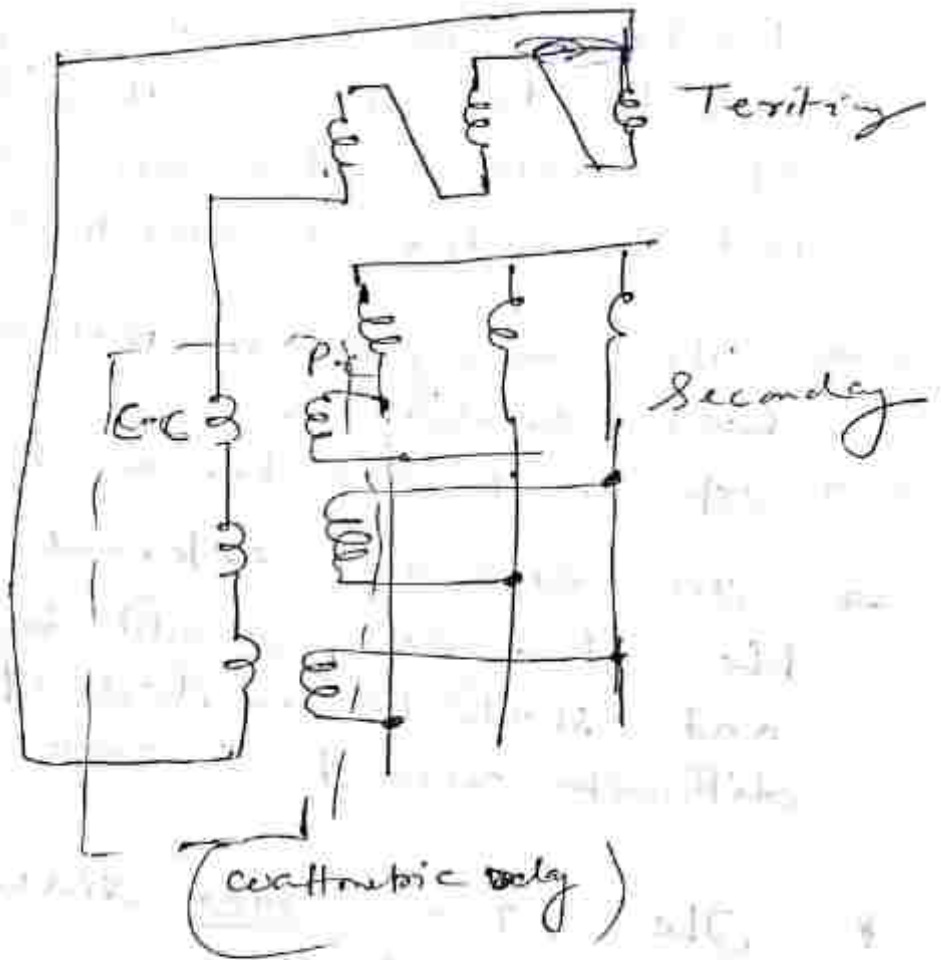
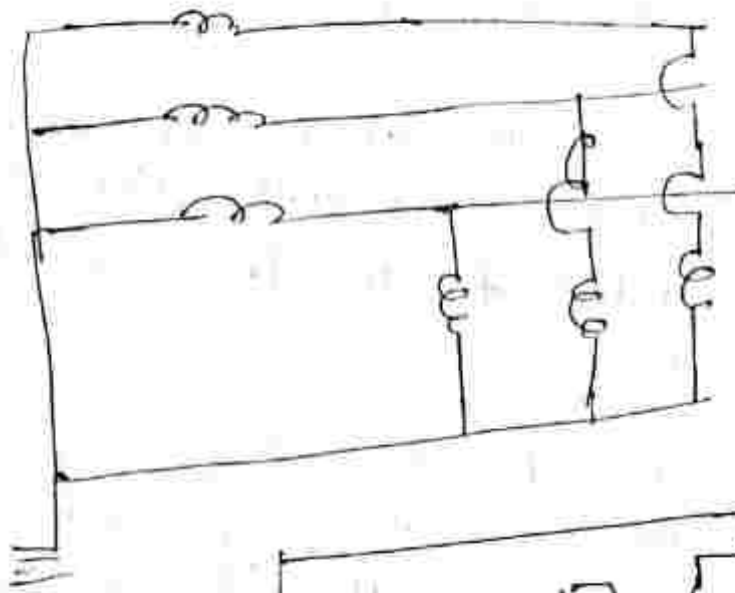
The method used for protection is known as split phase relaying. If the number of circuit is even for split phase protection, they are divided into two equal groups of parallel circuits ^{with CT for each group} ~~in each of the two groups~~.

If the no. of is odd, the no. of CTs in each of the two groups will not be equal and the CT must have different primary current ratings so that under normal condⁿ their secondary current will be equal.

For protection of inter-turn fault

winding having one CRT per phase, one of the methods suggested uses a five limb V.T with tertiary winding. The tertiary winding along with secondary winding with metric relay is used. The H.V winding is connected ^{between} the neutral and line terminal of the alternator. The voltage across the tertiary winding is the residual voltage which is normal condition is zero and some voltage under abnormal condⁿ. The residual voltage circulates current in the current coil of the relay ~~and~~ secondary of the transformer feeds the potential coil of the relay element.



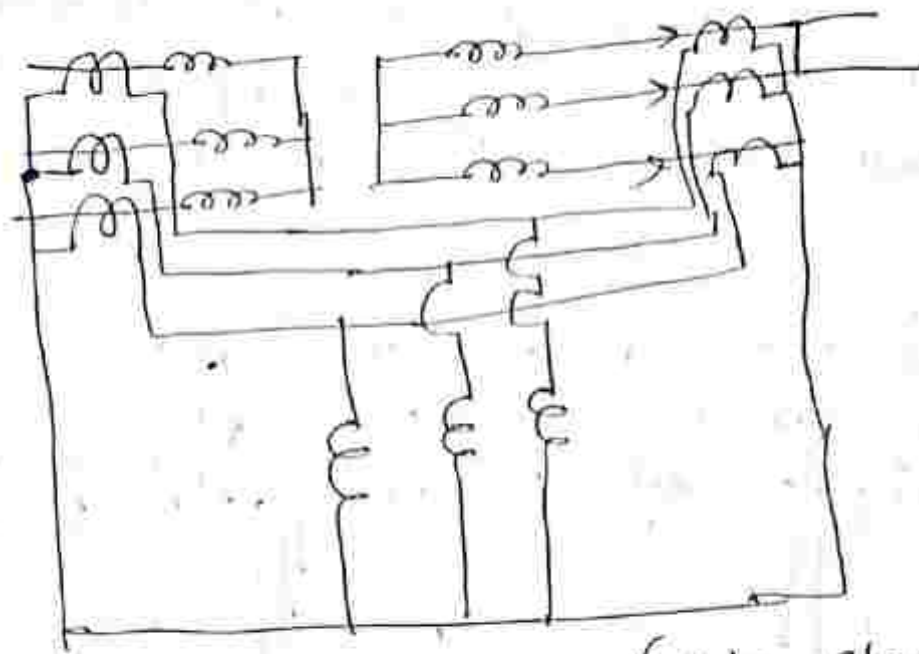


This diagram illustrates a transformer with a tertiary winding. The primary winding is connected to a source. The secondary winding is connected to a load consisting of a capacitor (C) and an inductor (L) in series. The tertiary winding is connected to a load consisting of a resistor (R) and an inductor (L) in series. The transformer core is represented by a rectangular loop. Labels 'Tertiary' and 'Secondary' are written next to their respective windings. A note '(capacitive only)' is written below the secondary winding.

Protection of Transformer:-

- For protection of transformer under short circuit and overloading, percentage differential protection, is recommended for transformer rated for more than 1 MVA.
- The primary and secondary current of a transformer are normally different. These currents form each other by 30° . In case of winding star-delta connected, differential protection scheme is considered.
- The relay must not operate under normal load condition.
- It must operate on internal fault condⁿ.
- In case of external fault condition, the two CTs should be equal in magnitude and should be in phase opposition so that differential current is zero.

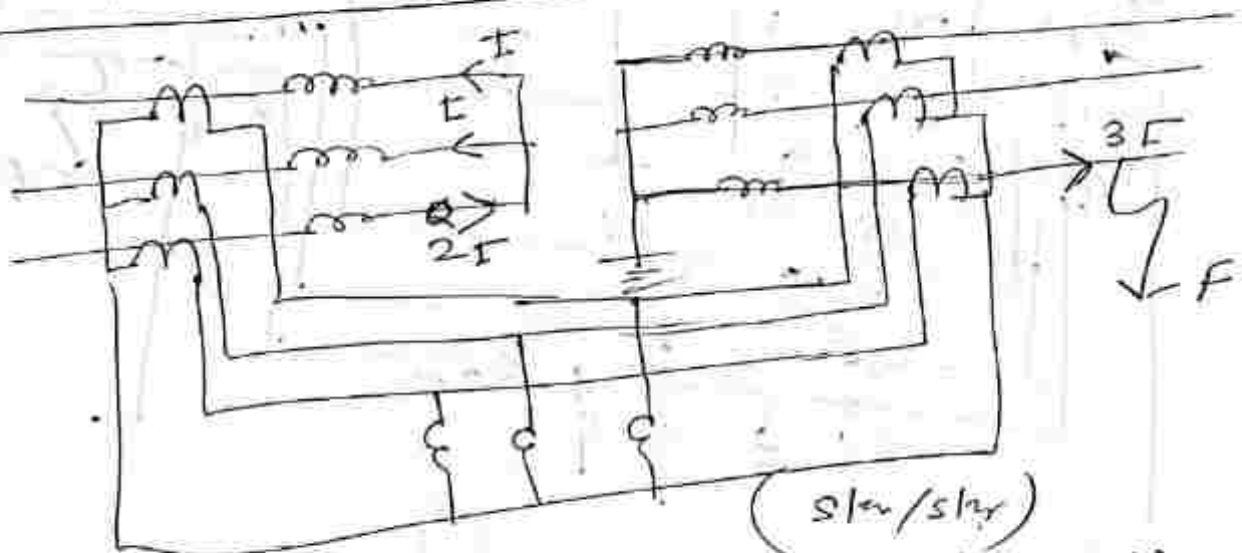
* The CT on star side of power transformer are in delta and on the delta side they are connected in star. The line current of star-delta power transformer will be displaced by 30° . In order to reduce the phase displacement, requirement is that to be connected by such fashion



(Star-Star) transformer

→ In this case star point of both transformer is ungrounded. When line to ground fault occurs, no extra fault current can flow. For external fault there will be no current through the operating coil. The relay will not operate.

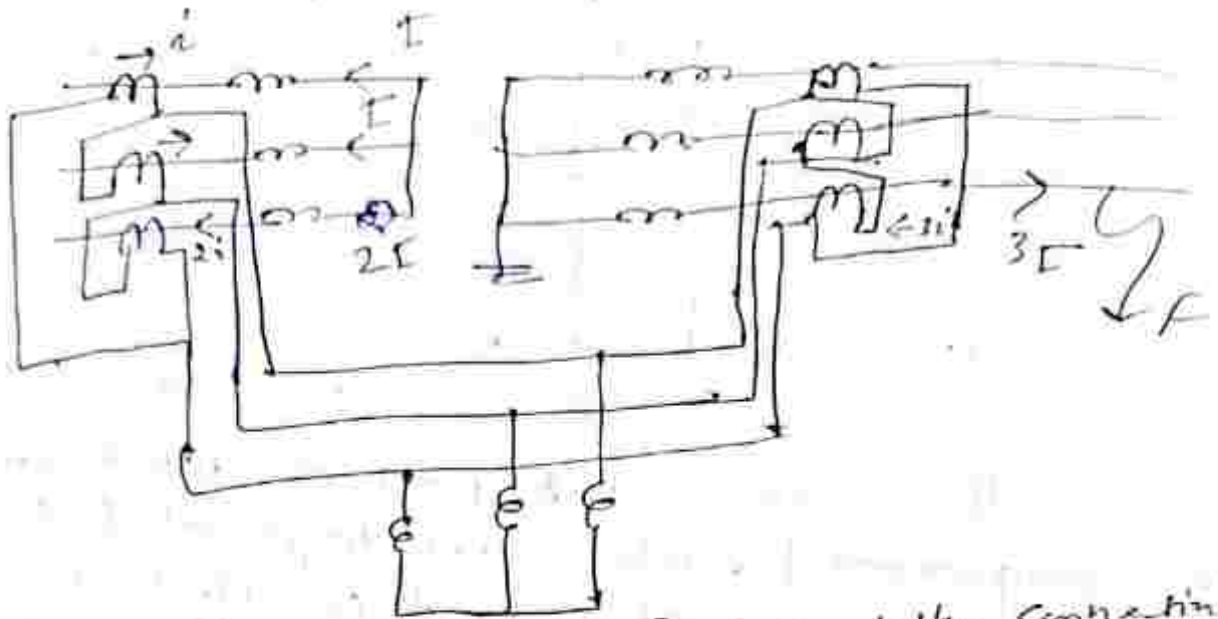
Star point is grounded :-



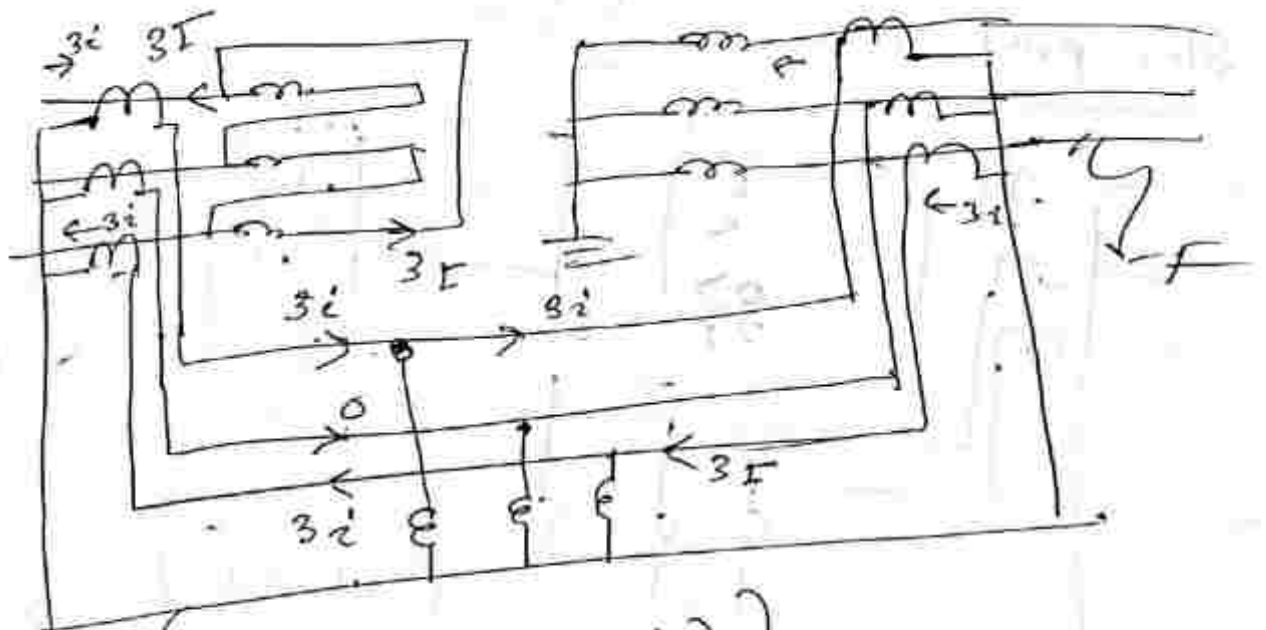
(Star/Star)

Assume that the unity transformation ratio, if the fault current on the secondary side is $3I$, only $2I$ current will be supplied by the primary. This type of connection is known as zero sequence current generator.

on case of through fault, the current circulate through the operating coil of the relay and relay will operate which is not desirable.



(Star/Star grounded CT, delta connection)
 In the case of external fault, the relay do not operate.

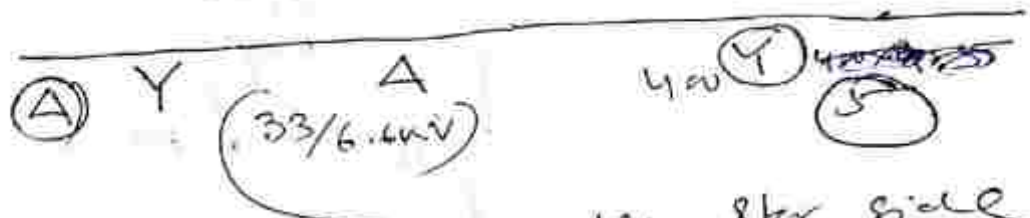


(Delta/Star grounded)

Problem :-

A 3 phase transformer rated $\underline{33\text{ kV}/6.6\text{ kV}}$ is connected star/delta and the protecting current transformers on the low voltage side have a ratio of $400/5$. Determine the ratio of current transformers on HV side.

Solⁿ :- Low voltage side is delta, the CT on that side will be star.



The line current on the star side of the power transformer.

$$\frac{E_1}{I_2} = k \quad \therefore E_1 = I_2 \times k$$

$$= 400 \times \frac{6.6}{33}$$

$$= 80 \text{ Amp.}$$

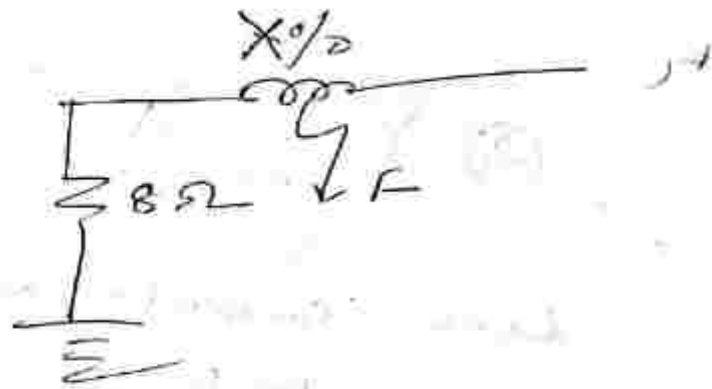
The CT on the star side is delta connected and the current required on relay side of CT is 5 amp. The current on the CT secondary is $5/\sqrt{3}$.

The CT ratio on the HT side is

$$\left(80 : \frac{5}{\sqrt{3}} \right)$$

A 6.6 kV, 5 MVA star connected alternator has a reactance 1.5 ohm/phase and negligible resistance. Most Z price protection scheme is used which operates when the out of balance current exceeds 25% of the full load current. The neutral of the generator through a resistance of 8 ohm. Determine the proportion of the winding which remains unprotected against earth fault. Show that alternator reactance can be ignored.

$$\frac{4.45 \times 10^2}{e}$$



The reactance of the winding of sequence of the current $\cdot X_n \times n^2$

The number of turns will be $\frac{xN}{100}$

The reactance of the unprotected winding will be $\frac{1.5 x^2 n^2}{100^2}$

The voltage of the unprotected portion = $3810 \times \frac{x}{100}$

The fault current = $3810 \times \frac{x}{100} \times \frac{1}{8}$ amp

$$\text{full load current} = \frac{5000}{\sqrt{3} \times 6.6} = 437.37 \text{ A}$$

∴ out of balance current required for the operation of the relay

$$437.37 \times 0.25 = 109.34 \text{ A}$$

$$\frac{3810 \text{ A}}{8 \omega} = 109.34$$

$$\omega = 22.95\%$$

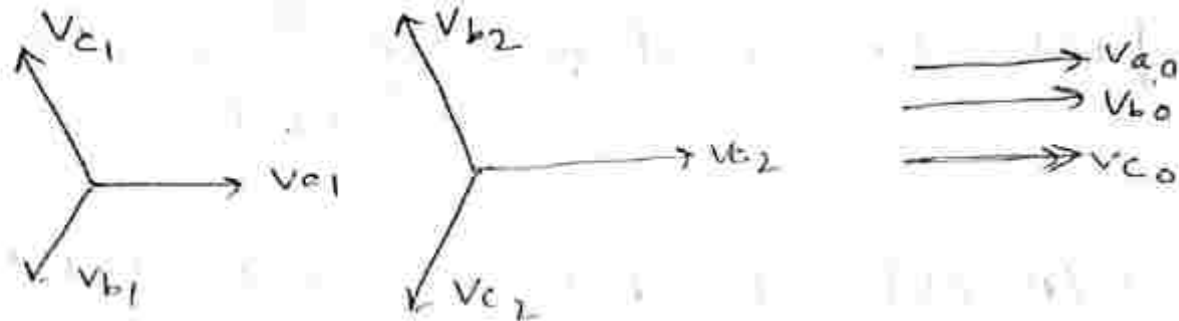
Symmetrical component and System

According to Fortescue's theorem, the three unbalanced vectors V_a , V_b and V_c can be replaced by three unbalanced vectors.

Positive sequence component: - It has three vectors equal in magnitude but displaced to in phase each other by 120° and has the phase sequence as the original vectors.

Negative sequence component: - Negative sequence component has three vectors equal in magnitude but it displaced from each other by 120° and phase sequence opposite to the original vectors.

③ Zero sequence component: - Zero sequence component which has three vectors of equal magnitude and also are in phase with each other



$$V_a = V_{a1} + V_{a2} + V_{a0}$$

$$V_b = V_{b1} + V_{b2} + V_{b0}$$

$$V_c = V_{c1} + V_{c2} + V_{c0}$$

$$\lambda = 1 \angle 120^\circ$$

$$\lambda^2 = 1 \angle -120^\circ$$

$$\lambda^3 = 1 \angle 0^\circ$$

$$\lambda^4 = \lambda \quad \lambda^2 + \lambda + 1 = 0$$

$$V_a = V_{a1} + V_{a2} + V_{a0}$$

$$V_b = \lambda^2 V_{a1} + \lambda V_{a2} + V_{a0}$$

$$V_c = \lambda V_{a1} + \lambda^2 V_{a2} + V_{a0}$$

$$I_a = I_{a1} + I_{a2} + I_{a0}$$

$$I_b = \lambda^2 I_{a1} + \lambda I_{a2} + I_{a0}$$

$$I_c = \lambda I_{a1} + \lambda^2 I_{a2} + I_{a0}$$

$$-V_a + \lambda V_b + \lambda^2 V_c = V_{a1} (1 + \lambda^3 + \lambda^3) + V_{a2} (1 + \lambda^2 + \lambda^4) + V_{a0} (1 + \lambda + \lambda^2)$$

$$= 3V_{a1} + V_{a2} (1 + \lambda^2 + \lambda) + 0$$

$$= 3V_{a1}$$

$$\therefore V_{a1} = \frac{1}{3} (V_a + \lambda V_b + \lambda^2 V_c)$$

$$V_a + \lambda^2 V_b + \lambda V_c = V_{a_1} (1 + \lambda + \lambda^2)$$

$$+ V_{a_0} (1 + \lambda^3 + \lambda^3) + V_{a_0} (1 + \lambda^2 + \lambda) = 3V_{a_0}$$

$$V_{a_0} = \frac{1}{3} (V_a + \lambda^2 V_b + \lambda V_c) \checkmark$$

$$V_a + V_b + V_c = V_{a_1} (1 + \lambda^2 + \lambda) + V_{a_2} (1 + \lambda + \lambda^2) + 3V_{a_0}$$

$$\underline{V_{a_0} = \frac{1}{3} (V_a + V_b + V_c)}$$

$$V_{a_1} = \frac{1}{3} (V_a + \lambda V_b + \lambda^2 V_c)$$

$$V_{a_2} = \frac{1}{3} (V_a + \lambda^2 V_b + \lambda V_c)$$

$$V_{a_0} = \frac{1}{3} (V_a + V_b + V_c)$$

$$I_{a_1} = \frac{1}{3} (I_a + \lambda I_b + \lambda^2 I_c)$$

$$I_{a_2} = \frac{1}{3} (I_a + \lambda^2 I_b + \lambda I_c)$$

$$I_{a_0} = \frac{1}{3} (I_a + I_b + I_c)$$

Average 3 phase power in terms of symmetrical component

$$P = V_a I_a \cos \phi_a + V_b I_b \cos \phi_b + V_c I_c \cos \phi_c$$

$$= V_a \cdot I_a + V_b I_b + V_c I_c$$

$$\begin{aligned} & (V_{a_1} + V_{a_2} + V_{a_0}) (I_{a_1} + I_{a_2} + I_{a_0}) \\ & + (\lambda^2 V_{a_1} + \lambda V_{a_2} + V_{a_0}) (\lambda^2 I_{a_1} + \lambda I_{a_2} + I_{a_0}) \\ & + (\lambda V_{a_1} + \lambda^2 V_{a_2} + V_{a_0}) (\lambda I_{a_1} + \lambda^2 I_{a_2} + I_{a_0}) \end{aligned}$$

$$\Rightarrow v_{a1} \epsilon_{a1} + v_{a1} \epsilon_{a2} + v_{a1} \epsilon_{a0} + v_{a2} \epsilon_{a1} + v_{a2} \epsilon_{a2} + v_{a2} \epsilon_{a0} \\ + v_{a0} \epsilon_{a1} + v_{a0} \epsilon_{a2} + v_{a0} \epsilon_{a0}$$

~~$$+ \lambda v_{a1} \epsilon_{a1} + \lambda v_{a1} \epsilon_{a2} + \lambda^2 v_{a1} \epsilon_{a0} + \lambda v_{a2} \epsilon_{a1} + \lambda v_{a2} \epsilon_{a2} \\ + \lambda v_{a2} \epsilon_{a0} + v_{a0} \epsilon_{a1}$$~~

~~$$+ \lambda^4 v_{a1} \epsilon_{a1} + \lambda^3 v_{a1} \epsilon_{a2} + v_{a0}$$~~

$$\lambda^4 v_{a1} \epsilon_{a1} + \lambda^3 v_{a1} \epsilon_{a2} + \lambda^2 v_{a1} \epsilon_{a0}$$

$$+ \lambda^3 v_{a2} \epsilon_{a1} + \lambda^2 v_{a2} \epsilon_{a2} +$$

Taking first terms on the R.H.S

$$(v_{a1} + v_{a2} + v_{a0}) (\epsilon_{a1} + \epsilon_{a2} + \epsilon_{a0}) \\ = v_{a1} \epsilon_{a1} + v_{a2} \epsilon_{a2} + v_{a0} \epsilon_{a0} + v_{a1} \epsilon_{a2} + v_{a1} \epsilon_{a0} \\ + v_{a2} \epsilon_{a1} + v_{a2} \epsilon_{a0} + v_{a0} \epsilon_{a1} + v_{a0} \epsilon_{a2}$$

2nd term

$$(\lambda^2 v_{a1} + \lambda v_{a2} + v_{a0}) (\lambda^2 \epsilon_{a1} + \lambda \epsilon_{a2} + \epsilon_{a0}) \\ = \lambda^2 v_{a1} \cdot \lambda^2 \epsilon_{a2} + \lambda^2 v_{a1} \cdot \lambda \epsilon_{a2} + \lambda^2 v_{a1} \cdot \epsilon_{a0} + \lambda v_{a2} \cdot \lambda \epsilon_{a2} + \lambda v_{a2} \cdot \epsilon_{a0} \\ + \lambda v_{a2} \cdot \lambda \epsilon_{a1} + v_{a0} \cdot \lambda \epsilon_{a2} + v_{a0} \epsilon_{a0}$$

$$\left[\begin{array}{l} \lambda^2 v_{a1} \cdot \lambda^2 \epsilon_{a1} = v_{a1} \cdot \epsilon_{a1} \\ \lambda^2 v_{a1} \cdot \lambda \epsilon_{a2} = \lambda v_{a1} \cdot \epsilon_{a2} \end{array} \right]$$

Proof = $3v_0 \epsilon_{a0} + 3v_{a2} \epsilon_{a2} + 3v_{a1} \epsilon_{a1} + v_{a1} \epsilon_{a2} (1 + \lambda + \lambda^2) + v_{a1} \epsilon_{a0} (1 + \lambda + \lambda^2)$

$$\begin{aligned}
 & + V_{a2} \Gamma_{a1} (1 + \lambda + \lambda^2) \\
 & + V_{a2} \Gamma_{a0} (1 + \lambda + \lambda^2) + V_{a0} \Gamma_{a1} (1 + \lambda + \lambda^2) \\
 & + V_{a0} \Gamma_{a0} (1 + \lambda + \lambda^2) \\
 & = 3 (V_{a1} \Gamma_{a1} + V_{a2} \Gamma_{a2} + V_{a0} \Gamma_{a0}) \\
 & = 3 \left[|V_{a1}| |\Gamma_{a1}| \cos \theta_1 + |V_{a2}| |\Gamma_{a2}| \cos \theta_2 + V_{a0} \Gamma_{a0} \cos \theta_0 \right]
 \end{aligned}$$

$$P + jQ = V_a \Gamma_a^* + V_b \Gamma_b^* + V_c \Gamma_c^*$$

$$= \begin{bmatrix} V_a & V_b & V_c \end{bmatrix} \begin{bmatrix} \Gamma_a \\ \Gamma_b \\ \Gamma_c \end{bmatrix}^*$$

$$= \begin{bmatrix} V_a \\ V_b \\ V_c \end{bmatrix}^T \begin{bmatrix} \Gamma_a \\ \Gamma_b \\ \Gamma_c \end{bmatrix}^*$$

$$\begin{bmatrix} V_a \\ V_b \\ V_c \end{bmatrix} = \begin{bmatrix} 1 & -1 & 1 \\ 1 & \lambda^2 & \lambda \\ 1 & \lambda & \lambda^2 \end{bmatrix} \begin{bmatrix} V_{a0} \\ V_{a1} \\ V_{a2} \end{bmatrix} = AV$$

$$\begin{bmatrix} V_a \\ V_b \\ V_c \end{bmatrix}^T = [AV]^T = V^T A^T$$

$$(P + jQ) = \begin{bmatrix} V_a \\ V_b \\ V_c \end{bmatrix}^T \begin{bmatrix} \Gamma_a \\ \Gamma_b \\ \Gamma_c \end{bmatrix}^*$$

$$= \begin{bmatrix} V_{a0} & V_{a1} & V_{a2} \end{bmatrix} \begin{bmatrix} 1 & 1 & 1 \\ 1 & \lambda^2 & \lambda \\ 1 & \lambda & \lambda^2 \end{bmatrix} \begin{bmatrix} \Gamma_a \\ \Gamma_b \\ \Gamma_c \end{bmatrix}^*$$

$$I_{a0} \begin{bmatrix} 1 \\ \lambda \\ \lambda^2 \end{bmatrix} = \begin{bmatrix} 1 & 1 & 1 \\ 1 & \lambda & \lambda^2 \\ 1 & \lambda^2 & \lambda \end{bmatrix} \begin{bmatrix} I_{a0} \\ I_{a1} \\ I_{a2} \end{bmatrix}$$

(3.14) (3.15)

$$= \begin{bmatrix} 1 & 1 & 1 \\ 1 & \lambda & \lambda^2 \\ 1 & \lambda^2 & \lambda \end{bmatrix} \begin{bmatrix} I_{a0} \\ I_{a1} \\ I_{a2} \end{bmatrix}$$

$$(P + jQ) = \begin{bmatrix} V_{a0} & V_{a1} & V_{a2} \end{bmatrix} \begin{bmatrix} 1 & 1 & 1 \\ 1 & \lambda^2 & \lambda \\ 1 & \lambda & \lambda^2 \end{bmatrix} \begin{bmatrix} I_{a0} \\ I_{a1} \\ I_{a2} \end{bmatrix}$$

$$= \begin{bmatrix} V_{a0} & V_{a1} & V_{a2} \end{bmatrix} \begin{bmatrix} 3 & 0 & 0 \\ 0 & 3 & 0 \\ 0 & 0 & 3 \end{bmatrix} \begin{bmatrix} I_{a0} \\ I_{a1} \\ I_{a2} \end{bmatrix}$$

$$= 3 \begin{bmatrix} V_{a0} & V_{a1} & V_{a2} \end{bmatrix} \begin{bmatrix} I_{a0} \\ I_{a1} \\ I_{a2} \end{bmatrix}$$

$$= 3 \left[V_{a0} I_{a0} + V_{a1} I_{a1} + V_{a2} I_{a2} \right]$$

$$P = 3 \left[V_{a0} I_{a0} \cos \theta_0 + V_{a1} I_{a1} \cos \theta_1 + V_{a2} I_{a2} \cos \theta_2 \right]$$

The potential of the neutral $V_n = -I_n Z_n$ where Z_n is the neutral grounding impedance and I_n is the neutral current. The negative sign is used as the current flows from the ground to the neutral and potential of the neutral is lower than the ground.

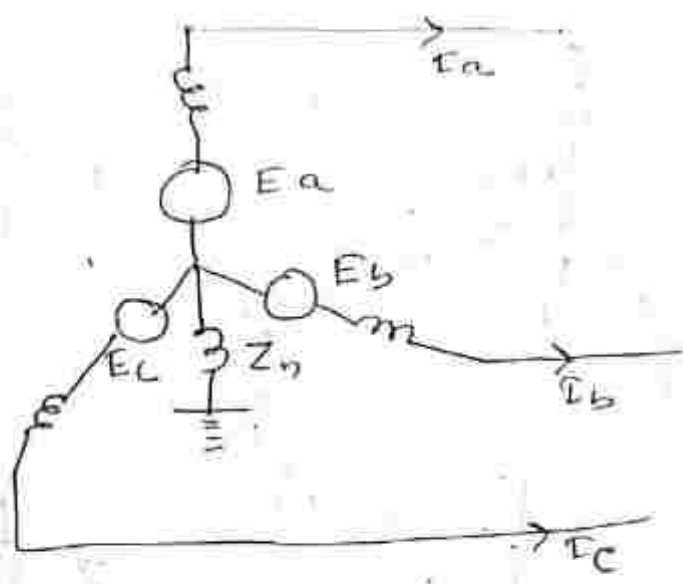
$$I_n = I_a + I_b + I_c = (I_{a1} + I_{a2} + I_{a0}) + (\lambda^2 I_{a1} + \lambda I_{a2} + \lambda I_{a1})$$

$$+ (\lambda I_{a1} + \lambda^2 I_{a2} + I_{a0})$$

$$\Rightarrow I_a (1 + \lambda + \lambda^2) + I_{a2} (1 + \lambda + \lambda^2) + 3 I_{a0}$$

$$= 3 I_{a0} \quad \text{And } V_n = -3 I_{a0} Z_n$$

Sequence Network Equation



→ These equations will be derived for an unloaded alternator with neutral solidly grounded, assuming that the system is balanced. The positive sequence component of voltage at the fault point is the positive sequence generated voltage minus the drop due to positive sequence current

$$V_{a1} = E_a - I_{a1} Z_1$$

The negative sequence component of voltage at the fault point is the generated sequence voltage minus the drop due to negative sequence current.

$$V_{a2} = E_{a2} - I_{a2} Z_2$$

$$E_{a2} = 0$$

$$V_{a2} = -I_{a2} Z_2$$

For zero sequence voltage, $E_{a0} = 0$

$$V_{a0} = V_n - I_{a0} Z_{g0}$$

$$= -3 I_{a0} Z_n - I_{a0} Z_{g0}$$

$$= -I_{a0} (3Z_n + Z_{g0})$$

Z_{g0} is the zero sequence impedance

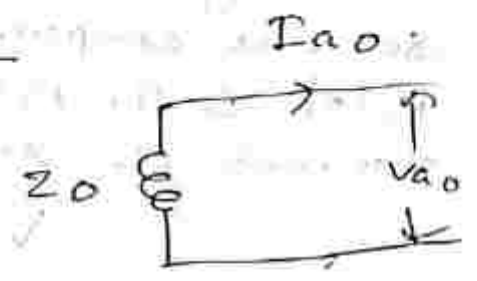
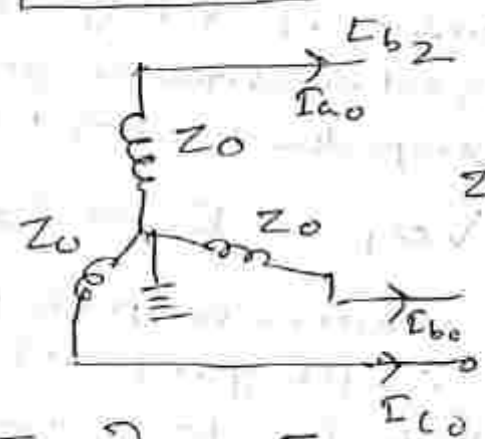
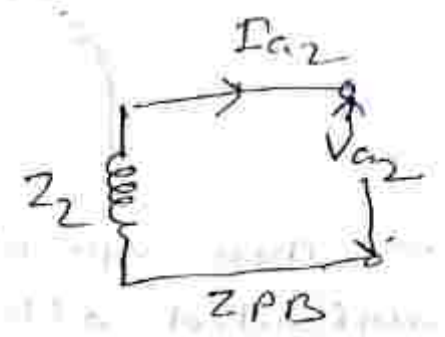
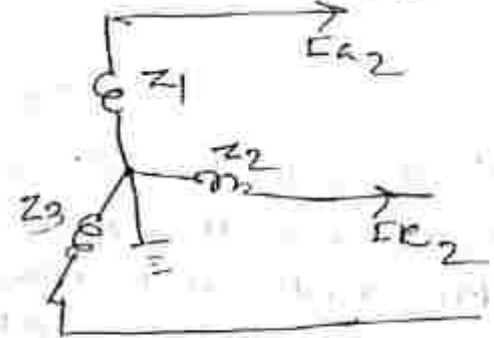
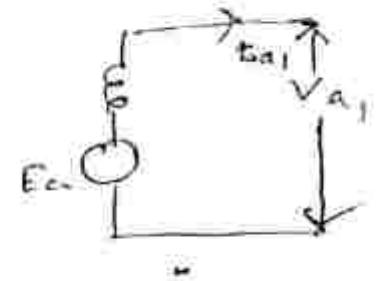
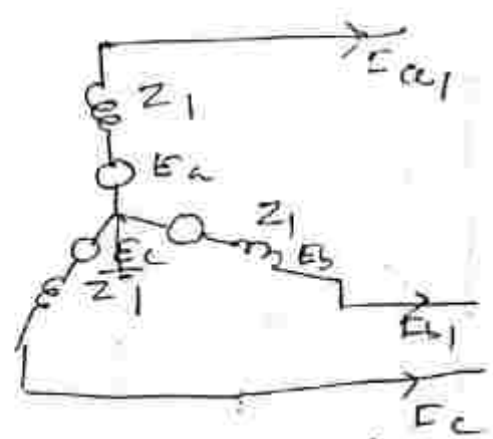
Z_n is the neutral impedance

$$V_{a1} = E_a - I_{a1} Z_1$$

$$V_{a2} = -I_{a2} Z_2$$

$$V_{a0} = -I_{a0} Z_0$$

$$Z_0 = Z_{g0} + 3Z_n$$



$$\begin{bmatrix} V_{a0} \\ V_{a1} \\ V_{a2} \end{bmatrix} = \begin{bmatrix} 0 \\ E_a \\ 0 \end{bmatrix} - \begin{bmatrix} Z_0 & 0 & 0 \\ 0 & Z_1 & 0 \\ 0 & 0 & Z_2 \end{bmatrix} \begin{bmatrix} I_{a0} \\ I_{a1} \\ I_{a2} \end{bmatrix}$$

Single line to ground fault: -

The boundary conditions are

$$V_a = 0$$

$$I_b = 0$$

$$I_c = 0$$

$$V_{a0} = -I_{a0}Z_0$$

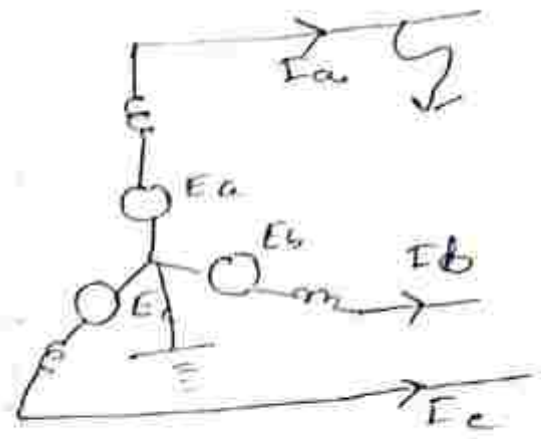
$$V_{a1} = E_a - I_{a1}Z_1$$

$$V_{a2} = -I_{a2}Z_2$$

$$I_{a1} = \frac{1}{3} (I_a + \lambda I_b + \lambda^2 I_c)$$

$$I_{a2} = \frac{1}{3} (I_a + \lambda^2 I_b + \lambda I_c)$$

$$I_{a0} = \frac{1}{3} (I_a + I_b + I_c)$$



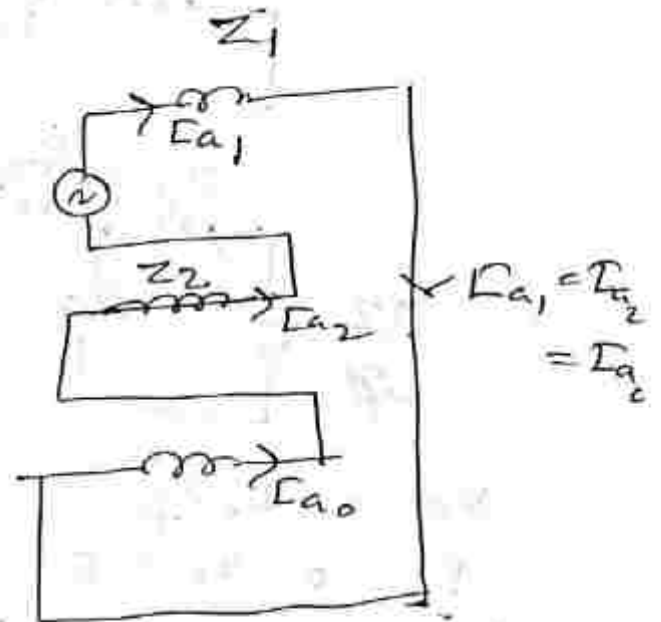
$$I_{a1} = I_{a2} = I_{a0} = I_a/3$$

$$V_a = 0 = V_{a1} + V_{a2} + V_{a0}$$

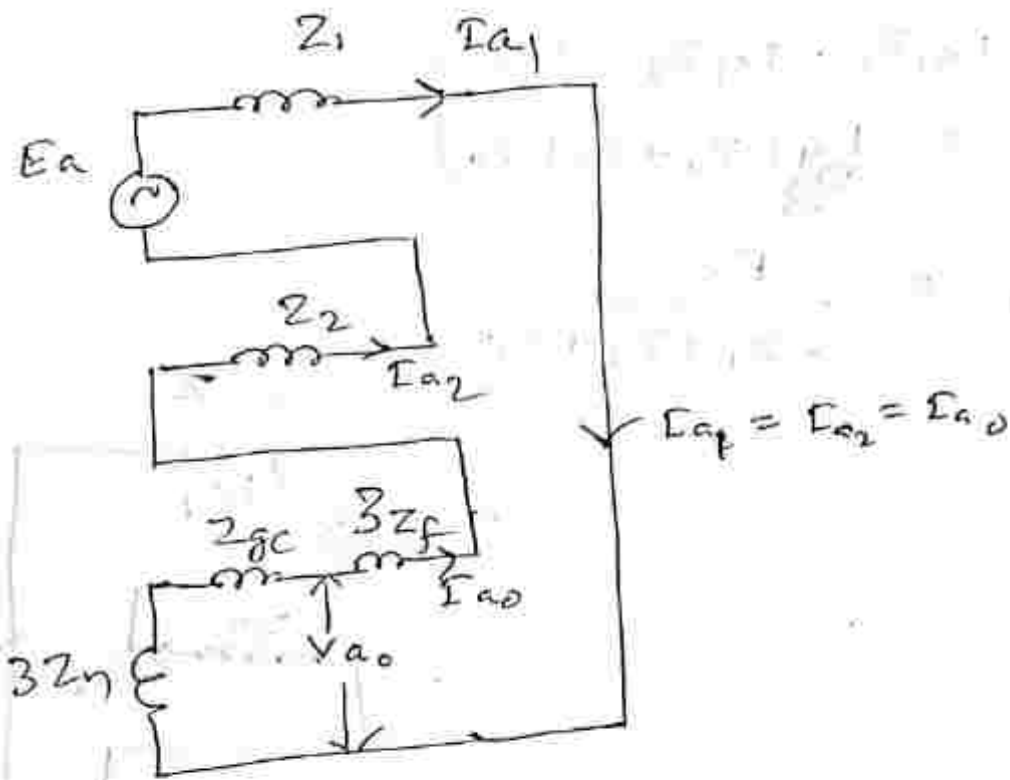
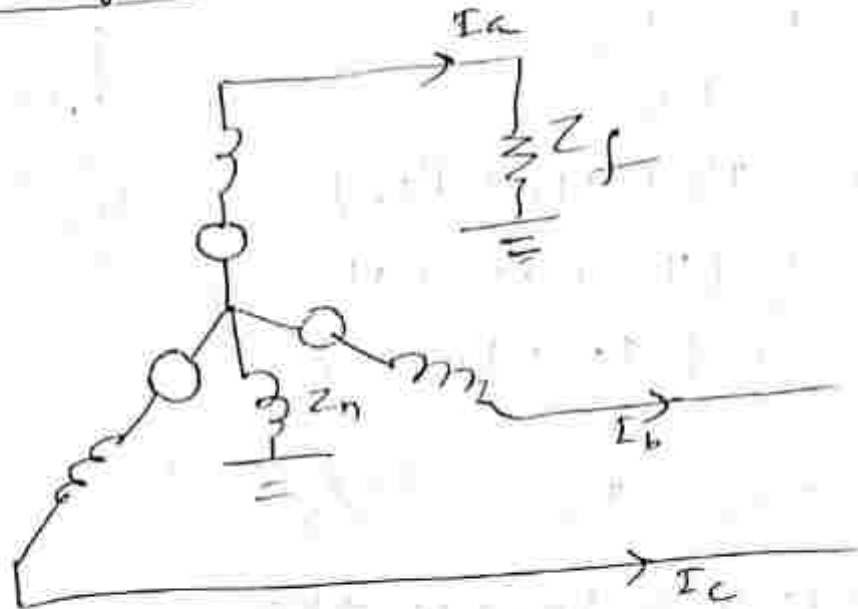
$$E_a - I_{a1}Z_1 - I_{a2}Z_2 - I_{a0}Z_0 = 0$$

$$E_a = \frac{I_{a1}}{3} (Z_1 + Z_2 + Z_0)$$

$$I_{a1} = \frac{E_a}{Z_1 + Z_2 + Z_0}$$



Line to ground fault with Z_f



$$V_a = I_a Z_f$$

$$I_b = 0 \quad I_c = 0$$

$$V_{a0} = -I_{a0} (Z_{g0} + 3Z_n)$$

$$V_{a1} = E_a - I_{a1} Z_n, \quad V_{a2} = -I_{a2} Z_2$$

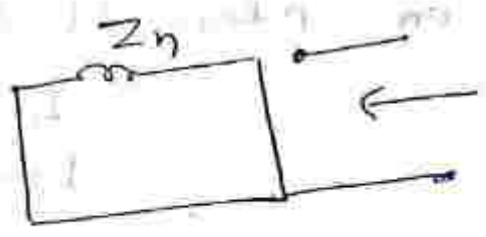
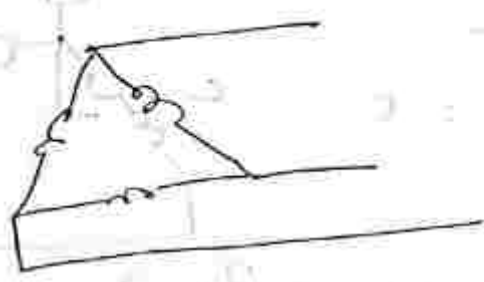
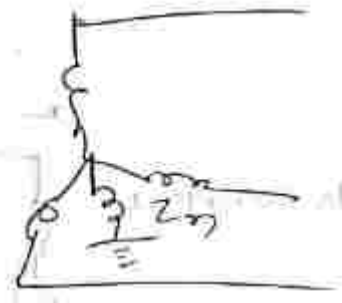
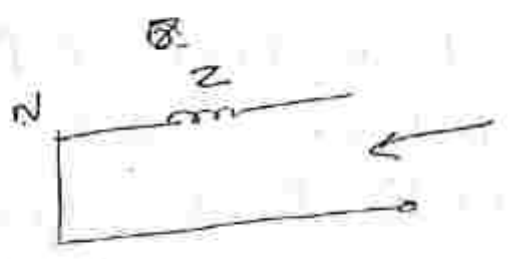
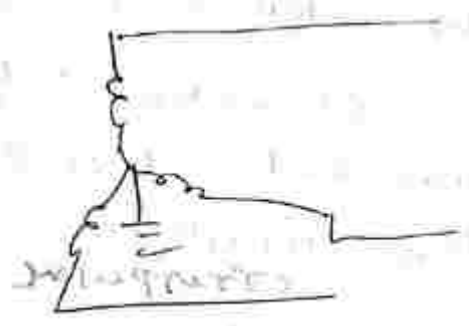
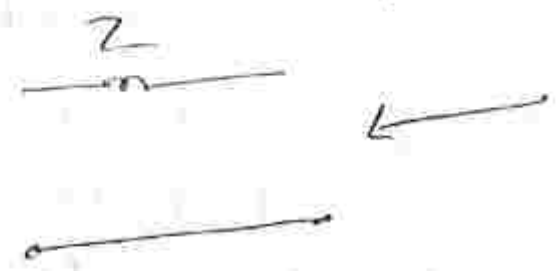
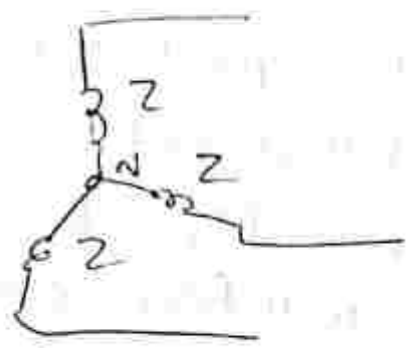
$$I_{a1} = I_{a2} = I_{a0} = I_a / 3$$

$$V_{a1} + V_{a2} + V_{a0} = V_a = 3 I_{a1} Z_f$$

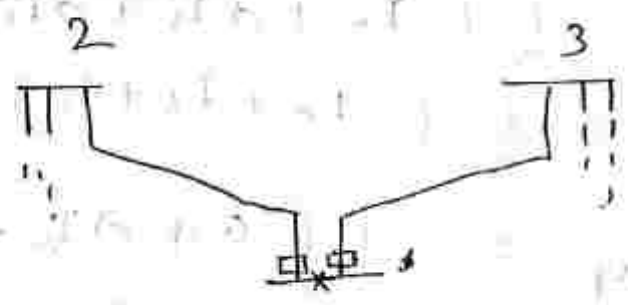
$$E_a - I_{a1}Z_1 - I_{a2}Z_2 = I_{a1}(Z_0 + 3Z_n)$$

$$= 3I_{a1}Z_f$$

$$\therefore I_{a1} = \frac{E_a}{Z_1 + Z_2 + (Z_0 + 3Z_n) + 3Z_f}$$



Short circuit capacity of a bus



1 short circuit

→ Let us consider symmetrical fault occurring at bus 1. The pre-fault voltage of bus is 1 pu. When fault occurs the voltage is zero. The voltage of the other buses ~~is zero~~ will sag during short circuits. The short-circuit capacity is defined as the product of the magnitude of pre-fault voltage and post-fault current. For a bus which has infinite short circuit capacity will have zero equivalent impedance. This bus is known as infinite bus. Such a bus is characterized by a zero equivalent impedance and it is able to maintain constant voltage irrespective of short circuit takes place.

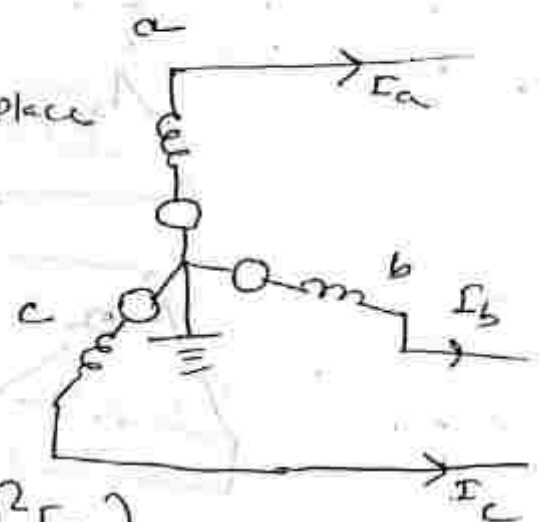
Line to line fault

Line to line fault takes place on phase - b & c

$$I_a = 0$$

$$I_b + I_c = 0$$

$$V_b = V_c$$



$$I_{a1} = \frac{1}{3} (I_a + \alpha I_b + \alpha^2 I_c)$$

$$I_{a2} = \frac{1}{3} (I_a + \alpha^2 I_b + \alpha I_c)$$

$$I_{a0} = \frac{1}{3} (I_a + I_b + I_c)$$

$$\begin{aligned}
 I_{a1} &= \frac{1}{3} (0 + \alpha I_b - \alpha^2 I_b) \\
 &= \frac{1}{3} (\alpha - \alpha^2) I_b
 \end{aligned}$$

$$I_{a2} = \frac{1}{3} (0 + \lambda^2 I_b - \lambda I_b)$$

$$= \frac{I_b}{3} (\lambda^2 - \lambda)$$

$$I_{a0} = \frac{1}{3} (0 + 0) = 0$$

In a line to line fault zero sequence component is absent. The positive sequence component of current is equal in magnitude but opposite in phase to negative sequence component of current.

$$I_{a1} = -I_{a2}$$

$$V_b = V_{a0} + \lambda^2 V_{a1} + \lambda V_{a2}$$

$$V_c = V_{a0} + \lambda V_{a1} + \lambda^2 V_{a2}$$

$$V_{a0} + \lambda^2 V_{a1} + \lambda V_{a2} = V_{a0} + \lambda V_{a1} + \lambda^2 V_{a2}$$

$$(\lambda^2 - \lambda) V_{a1} = (\lambda^2 - \lambda) V_{a2}$$

$$V_{a1} = V_{a2}$$

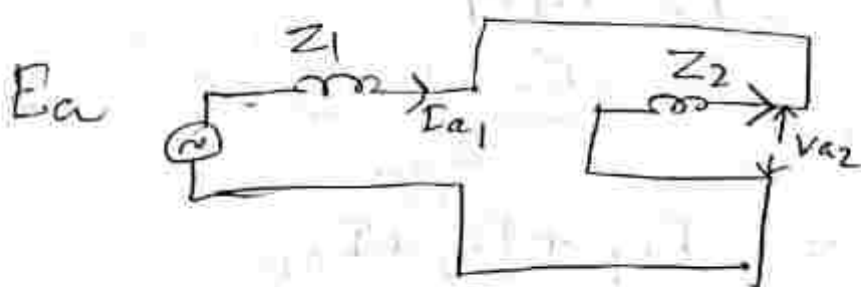
$$E_a - I_{a1} Z_1 = -I_{a2} Z_2$$

$$E_a - I_{a1} Z_1 = I_{a1} Z_1$$

$$E_a = I_{a1} Z_1 + I_{a1} Z_1$$

$$= I_{a1} (Z_1 + Z_2)$$

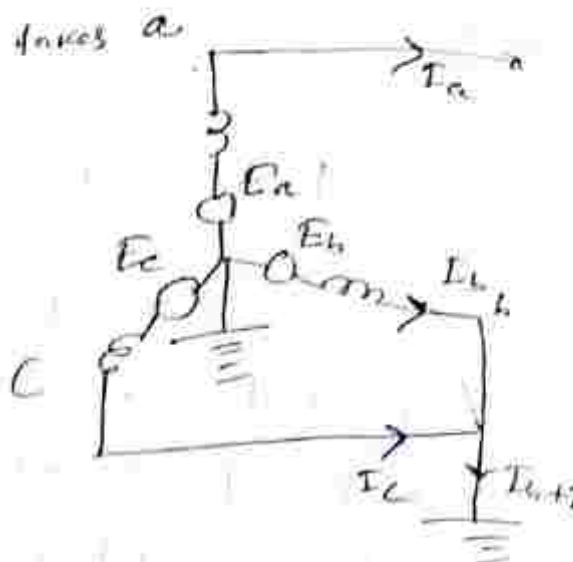
$$I_{a1} = \frac{E_a}{Z_1 + Z_2}$$



Double Line to ground fault

Double line to ground fault takes a
Place on phase b and c

$$\left. \begin{aligned} I_a &= 0 \\ V_b &= 0 \\ V_c &= 0 \end{aligned} \right\}$$



$$V_{a0} = \frac{1}{3} (V_a + V_b + V_c)$$

$$= \frac{V_a}{3}$$

$$V_{a1} = \frac{1}{3} (V_a + \lambda V_b + \lambda^2 V_c)$$

$$= \frac{V_a}{3}$$

$$V_{a2} = \frac{1}{3} (V_a + \lambda^2 V_b + \lambda V_c)$$

$$= \frac{V_a}{3}$$

$$\underline{V_{a0} = V_{a1} = V_{a2}} \quad (1)$$

$$V_{a0} = V_{a1}$$

$$-I_{a0} Z_0 = E_a - I_{a1} Z_1$$

$$I_{a0} = - \frac{E_a - I_{a1} Z_1}{Z_0}$$

$$V_{a2} = V_{a1} \quad (\text{2nd cond})$$

$$-I_{a2} Z_2 = E_a - I_{a1} Z_1$$

$$\therefore I_{a2} = - \frac{E_a - I_{a1} Z_1}{Z_2}$$

$$I_a = I_{a1} + I_{a2} + I_{a0}$$

$$0 = I_{a1} + I_{a2} + I_{a0}$$

$$I_{a_1} \neq - \frac{E_a - I_{a_1} z_1}{z_2} - \frac{E_a - I_{a_1} z_1}{z_0} = 0$$

$$I_{a_1} \left(z_1 - \frac{E_a - I_{a_1} z_1}{z_2} \right) -$$

$$I_{a_1} = \frac{E_a - I_{a_1} z_1}{z_2} + \frac{E_a - I_{a_1} z_1}{z_0}$$

$$= (E_a - I_{a_1} z_1) \left(\frac{1}{z_2} + \frac{1}{z_0} \right)$$

$$= (E_a - I_{a_1} z_1) \left(\frac{z_0 + z_2}{z_2 z_0} \right)$$

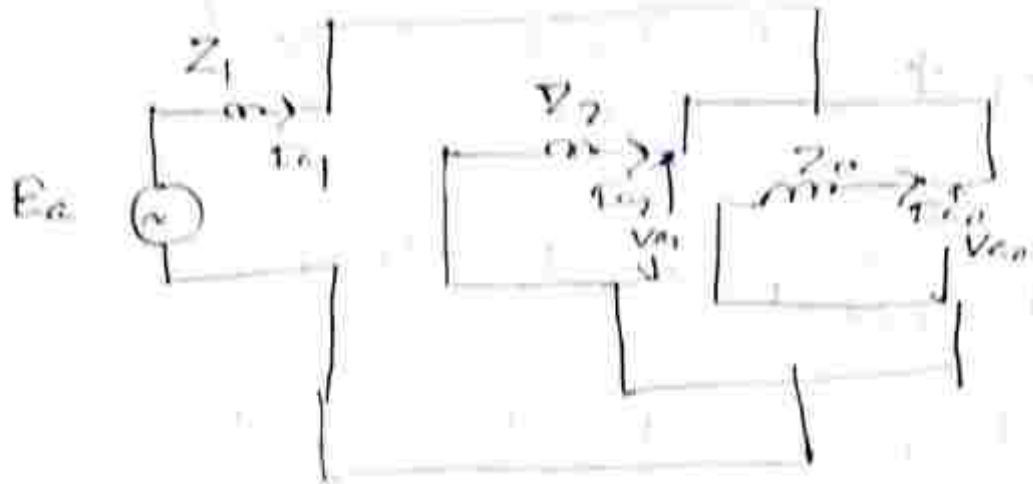
$$= \frac{E_a (z_0 + z_2)}{z_2 z_0} - \frac{I_{a_1} (z_0 + z_2) z_1}{z_2 z_0}$$

$$I_{a_1} \left(1 + \frac{z_1 (z_0 + z_2)}{z_2 z_0} \right) = \frac{E_a (z_0 + z_2)}{z_2 z_0}$$

$$I_{a_1} = \frac{E_a (z_0 + z_2)}{z_2 z_0 \left(1 + \frac{z_1 (z_0 + z_2)}{z_2 z_0} \right)}$$

$$= \frac{E_a (z_0 + z_2)}{z_2 z_0 + z_1 (z_0 + z_2)}$$

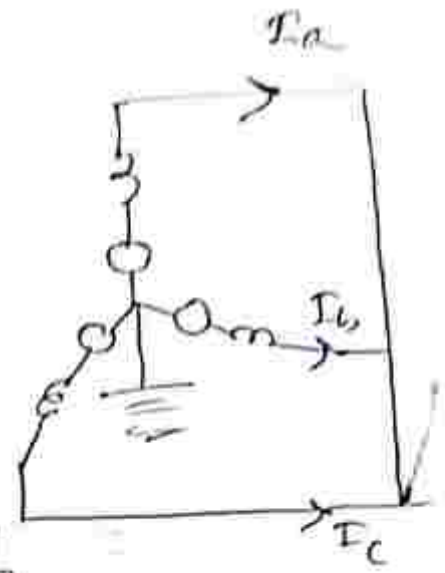
$$= \frac{E_a}{z_1 + \frac{z_0 z_2}{z_0 + z_2}}$$



3 p # Janet

$$\left. \begin{aligned} I_a + I_b + I_c &= 0 \\ V_a = V_b = V_c \end{aligned} \right\}$$

Since $|I_a| = |I_b| = |I_c|$ and if I_a taken as reference



$$I_b = \lambda^2 I_a \quad I_c = \lambda I_a$$

$$\begin{aligned} I_{a1} &= \frac{1}{3} (I_a + \lambda I_b + \lambda^2 I_c) \\ &= \frac{1}{3} (I_a + \lambda^3 I_a + \lambda^3 I_a) \\ &= I_a \end{aligned}$$

$$\begin{aligned} I_{a2} &= \frac{1}{3} (I_a + \lambda^2 I_b + \lambda I_c) \\ &= \frac{1}{3} (I_a + \lambda^4 I_a + \lambda^2 I_a) \\ &= \frac{1}{3} (I_a + \lambda I_a + \lambda^2 I_a) \\ &= \frac{1}{3} I_a (1 + \lambda + \lambda^2) \\ &= 0 \end{aligned}$$

$$I_{a0} = \frac{1}{3} (I_a + I_b + I_c) = 0$$

In a 3 φ fault zero as well as negative sequence component of current are absent and positive sequence component current is equal to the phase current.

$$V_{a1} = \frac{1}{3} (V_a + \lambda V_b + \lambda^2 V_c)$$

$$= \frac{1}{3} (V_a + \lambda V_a + \lambda^2 V_a)$$

$$= \frac{1}{3} V_a (1 + \lambda + \lambda^2)$$

$$= 0$$

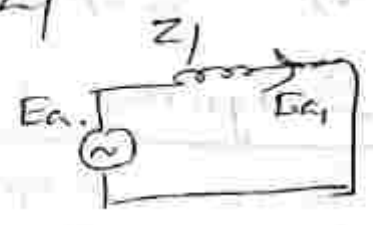
$$V_{a2} = \frac{1}{3} (V_a + \lambda^2 V_b + \lambda V_c)$$

$$= 0$$

$$V_{a0} = 0 \quad \frac{1}{3} (V_a + V_b + V_c)$$

$$V_{a1} = 0 = E_a - I_{a1} Z_1$$

$$I_{a1} = \frac{E_a}{Z_1}$$



... the faulted system is decomposed into its positive, negative and zero sequence components. The positive sequence component is a single-phase circuit with a voltage source E_a and impedance Z_1 . The negative and zero sequence components are represented by short circuits at the fault point, indicating that the voltage components V_{a2} and V_{a0} are zero.

Static Relays :-

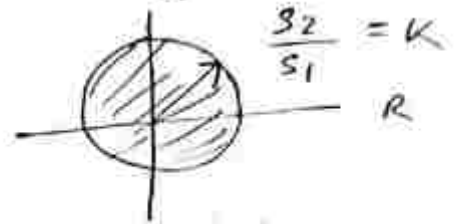
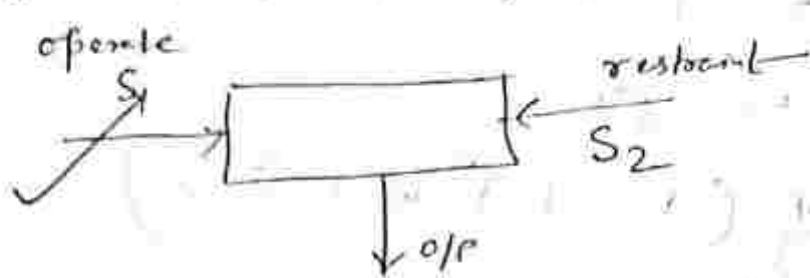
Amplitude comparator

If two input signals are S_1 and S_2 , the amplitude comparator gives the OP of $\left[\frac{S_2}{S_1} \leq K \right]$

S_1 = operating quantity

S_2 = restraining quantity

The function is represented by circles in a complex plane.

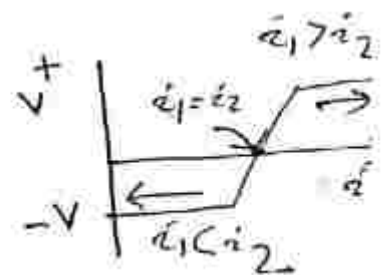
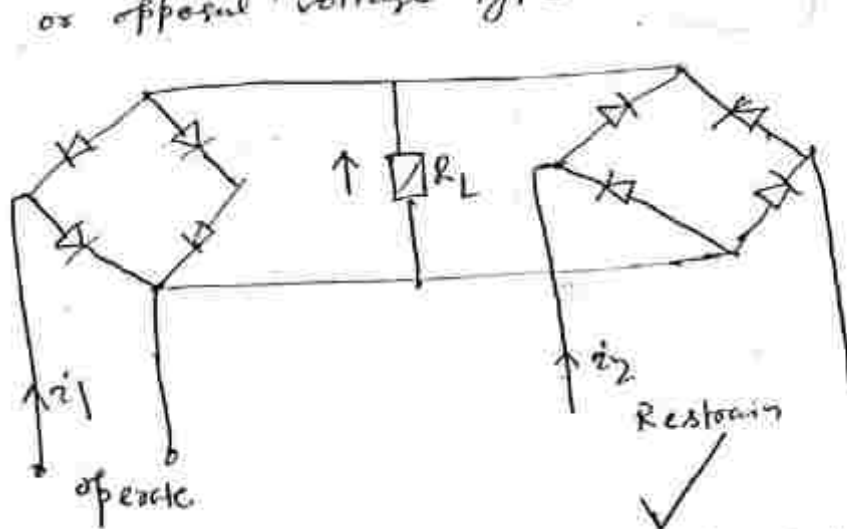


Static amplitude comparator can be classified

- (a) Integrating comparator
- (b) Instantaneous comparator
- (c) Sampling comparator.

Integrating Comparator :-

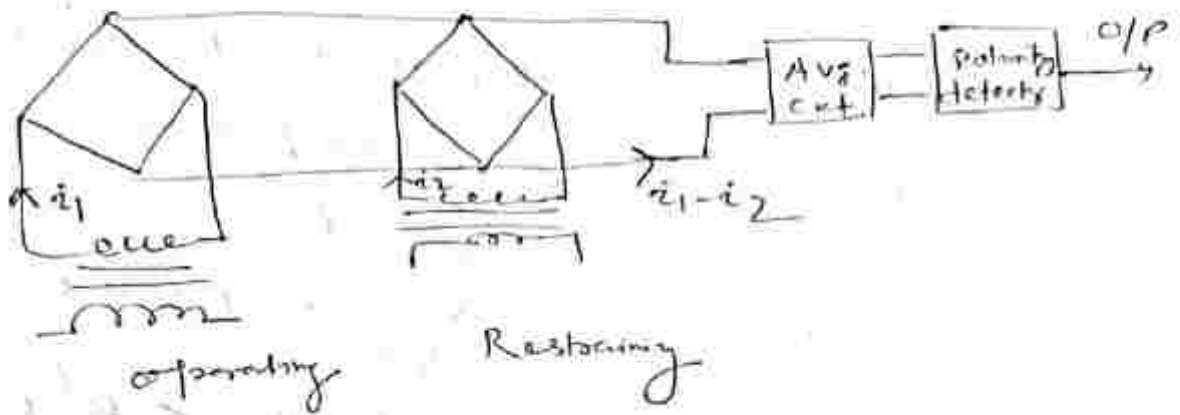
Rectifier bridge comparator can be either be circulating type or opposed voltage type.



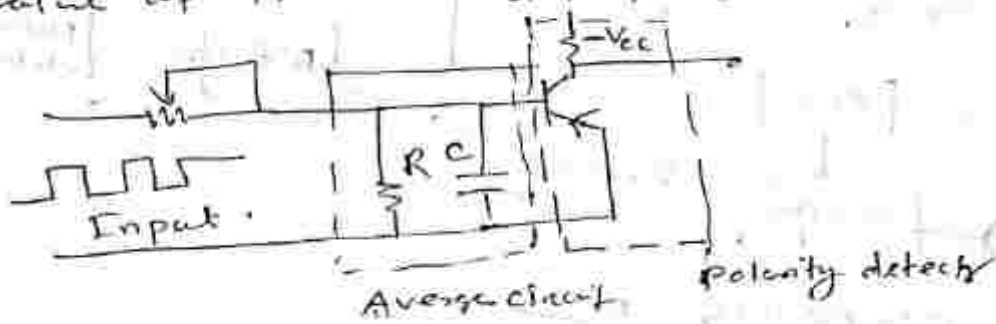
The polarized relay operates when $S_1 > S_2$ where $S_1 = K_1 i_1$ and $S_2 = K_2 i_2$. The voltage across the relay never exceeds twice the forward voltage drop of one of the rectifier.

A static integrator can be used instead of polarized relay.

which consist of averaging circuit and polarity detectors. The two current i_1 & i_2 rectified and their difference $(i_1 - i_2)$ is averaged. When average is positive the o/p is active.



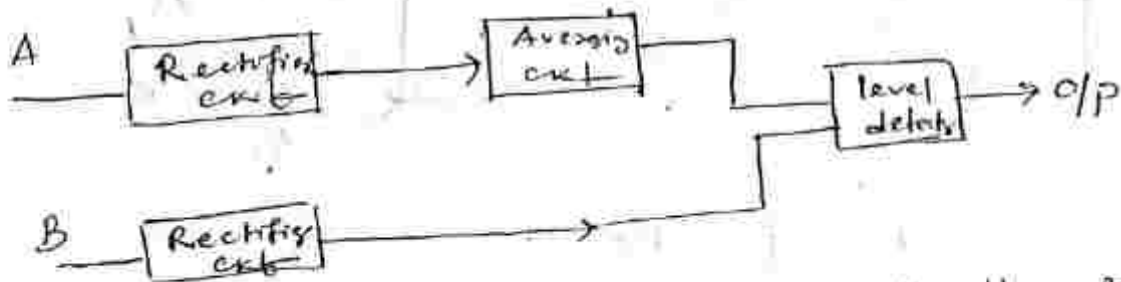
A triggering occurs when the capacitor voltage reaches the value of the level detector.



Instantaneous comparators

Instantaneous or direct comparators can be two types.

- (a) averaging type
- (b) phase splitting type

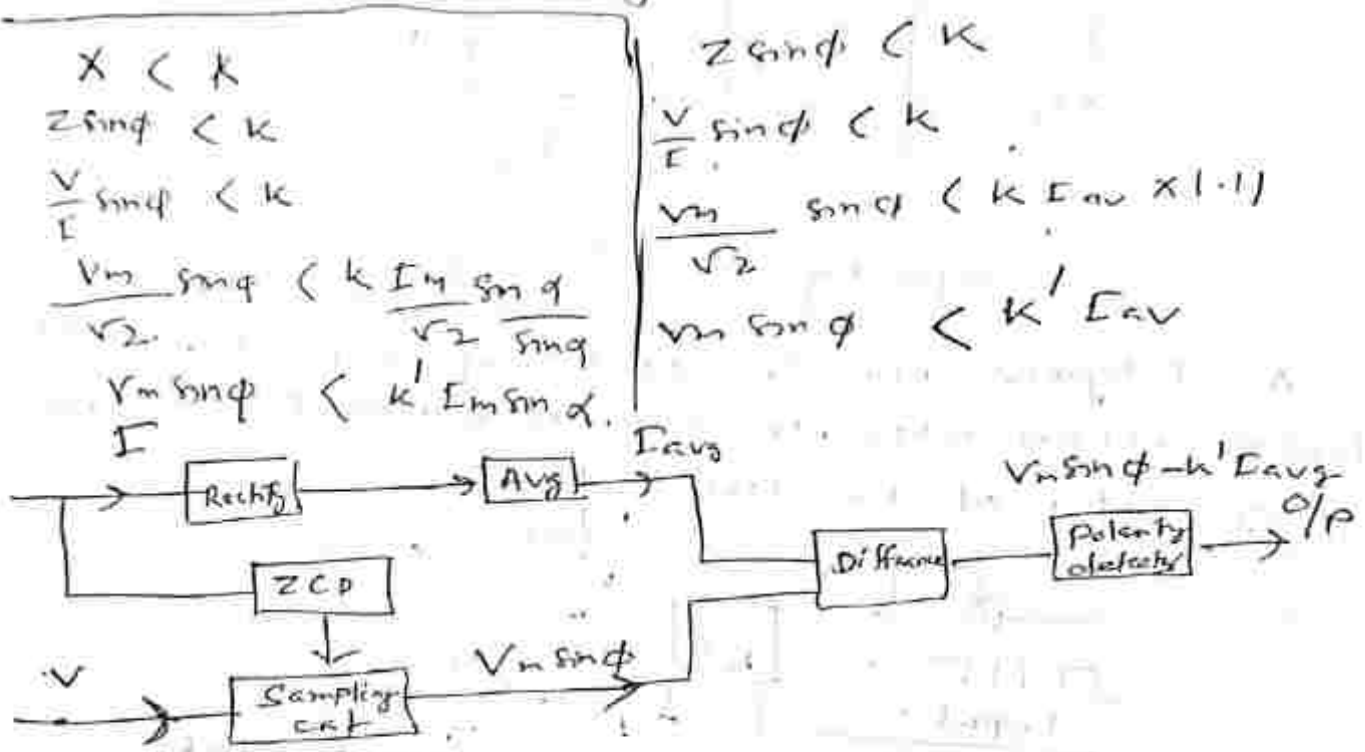


The restoring signal is rectified and then smoothing to obtain level constraints. This is compared with operating signal. The tripping signal occurs when operating signal exceeds the level constraints.

Sampling comparator

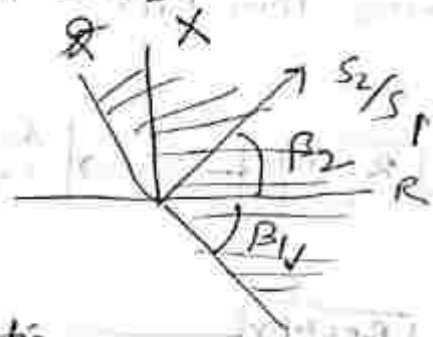
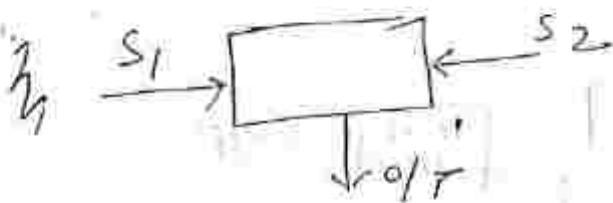
Reactance characteristics is obtained by comparing the rectified and smooth value of current. If I lags behind voltage V by an angle ϕ the value of voltage at current zero is $V_m \sin \phi$.

The reactance relay operates for $X < K$



Phase comparator

→ It is most useful in differential and carrier relays. The phase relationship lying within specific limit of input signal S_1 & S_2 .



The condition of operation

$$-\beta_1 \leq \theta \leq +\beta_2$$

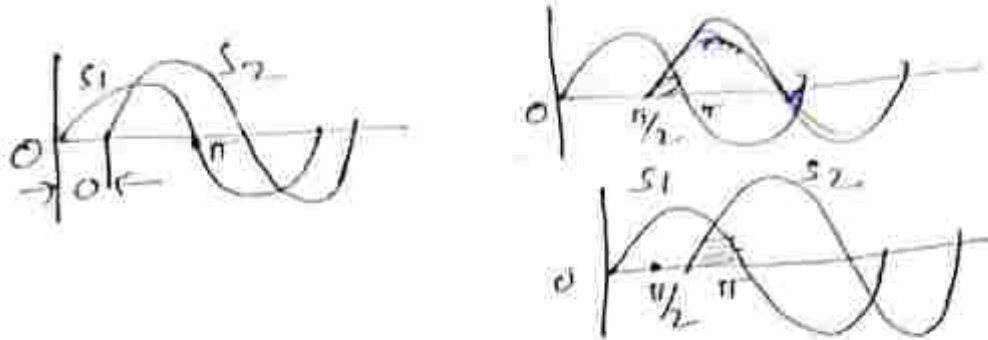
θ = angle by which S_2 leads S_1 , if $\beta_1 = \beta_2 = 90^\circ$

The comparator is known as cosine comparator

If $\beta_1 = 0$ $\beta_2 = 180^\circ$ sine comparator

Coincidence Comparator

The two input signals S_1 & S_2 , the period of coincidence of S_1 and S_2 will depend on the phase difference between S_1 and S_2 .



Period of coincidence is equal to the period of non-coincidence for a phase difference of $\pm 90^\circ$.

The period of coincidence is less than the period of non-coincidence and vice versa when the phase difference is less than $\pm 90^\circ$.

Basic Element of Static Relay

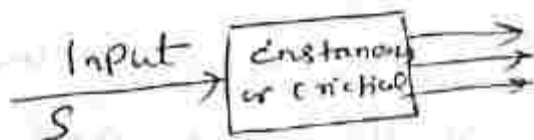
(1) Input element:-

- mixing circuit are required
- summing junction are required
- using OP-Amp as a summer or mixer

Measuring Element:-

- ① single input device
- ② two-input device
- ③ multi-input device.

Single input device are comparator.



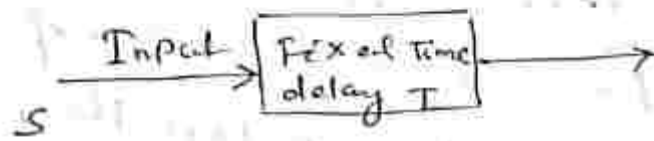
for obtaining contact pressure S is either zero or positive

then marginal operation level.

① To provision of β tripping signal to the CB and give some possible additional functioning of ~~interrupting~~ ^{interlocking} clear and indication.

(c) For operation $S \gg A$ (critical) ✓
for reset $S \leq kA \therefore k \leq 1$.

Fixed time delay: - (fixed definite time funct



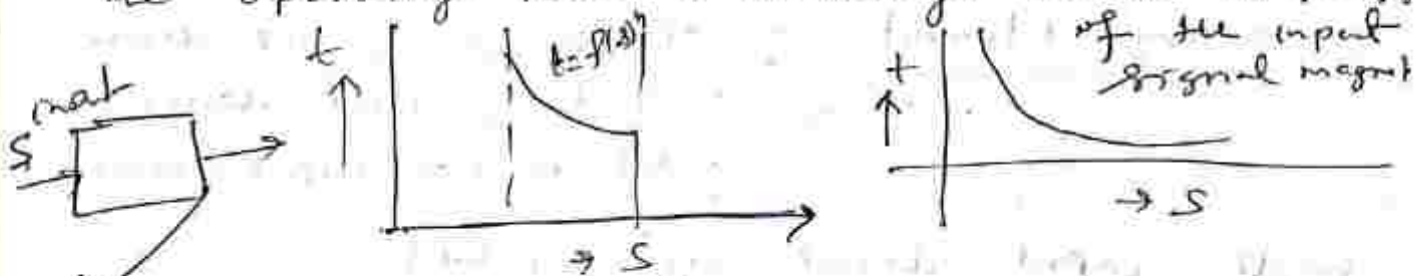
There must be fixed time delay between input and o/p. The time delay between the application of input and occurrence of o/p.

✓ Time function dependent input.

$$t = f(S^n) \checkmark$$

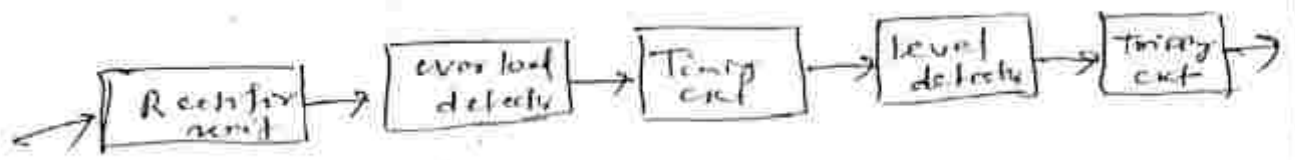
when n is negative. The relay for this category are inverse definite minimum time lag.

The essential features of such relay is that the operating time is inversely related to power of the input signal magnit



Over current relay

- ① Low burden CT, so that smaller CT is required
- ② Compactness of the unit and space reduction
- ③ Instantaneous reset possible
- ④ Low maintenance and long life
- ⑤ No overreaching tendency.



Principle The static overcurrent relay consists of a rectifier unit which converts the a.c. signal to d.c. signal followed by overload detector timing circuit, level detector and tripping ckt.

Time current characteristic

A general expression for the operating time of a time-current relay is

$$t = \frac{K M}{I^n - I_p^n}$$

t = time of operation in second ✓

K = design constant ✓

M = time multiplier setting ✓

I = multiple of tap setting current ✓

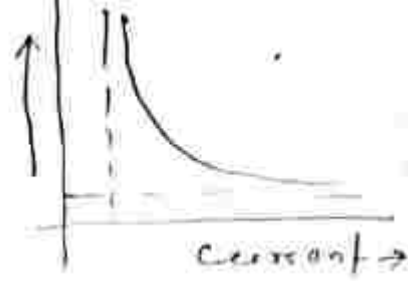
I_p = multiple of tap current at which pick up occurs. ✓

n = index number, which is empirical.

$$IDMT \Rightarrow t = \frac{0.14}{I^{0.02} - I}$$

Very inverse $t = \frac{13.5}{I - 1}$

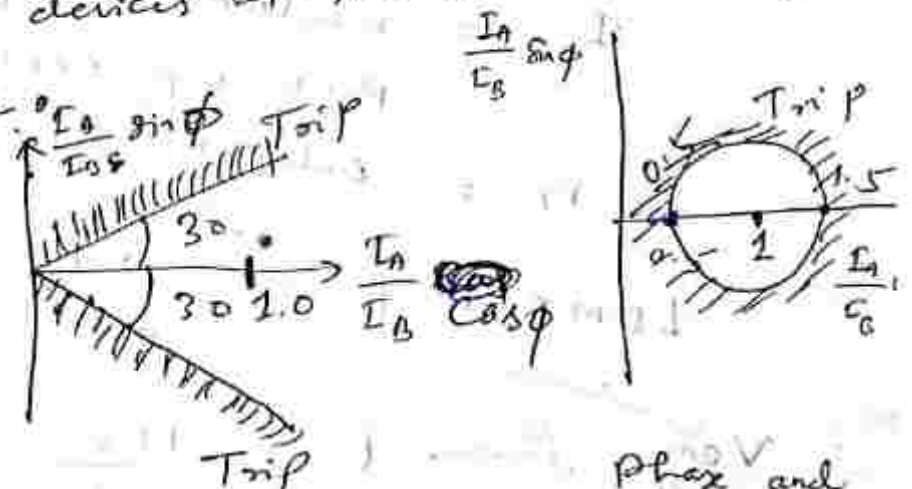
extremely inverse $t = \frac{80}{I^2 - 1}$



Differential protection

A differential protection scheme compares quantity derived from the input and output currents of the protected circuit in such a manner that for all healthy system and through fault conditions the quantities balance and protection is inoperative, while the internal fault condition the balance is disturbed and the protection operates.

The relaying quantities at both ends of the transmission circuit will be identical in magnitude and phase, so that their phasor ratio $\alpha = \frac{I_A}{I_B} = 1 + j0 = 1 \angle 0^\circ$. Two types of characteristics are plotted showing the threshold boundaries in terms of the effective ratio of outputs from the summation devices at two ends A & B of the protected line.



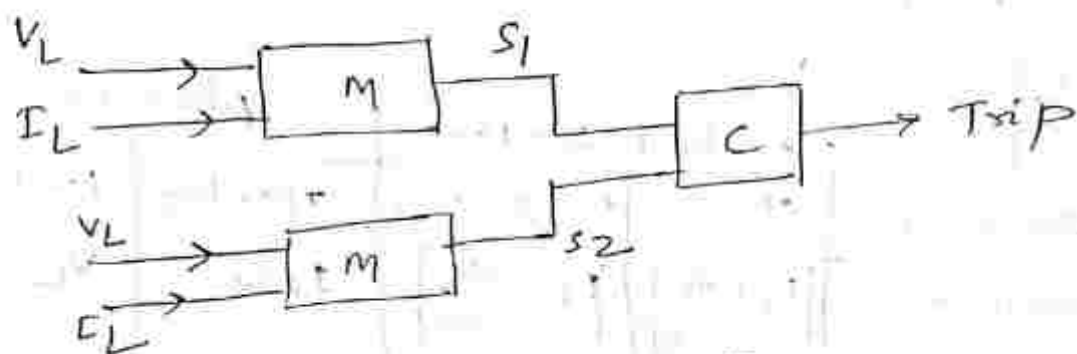
Phase comparison Amplitude

In practice, the pilot wire protection system comparison characteristics tend to be variable because a relay having closed - threshold characteristic under

Pilot wire systems may employ either of the above characteristics while carrying current of system employ pure phase comparison.

Static distance protection :-

Distance relays are characterized by having two input quantities respectively proportional to the voltage and current at a particular point in the power system.



$$S_1 = K_1 V_L + K_2 I_L$$

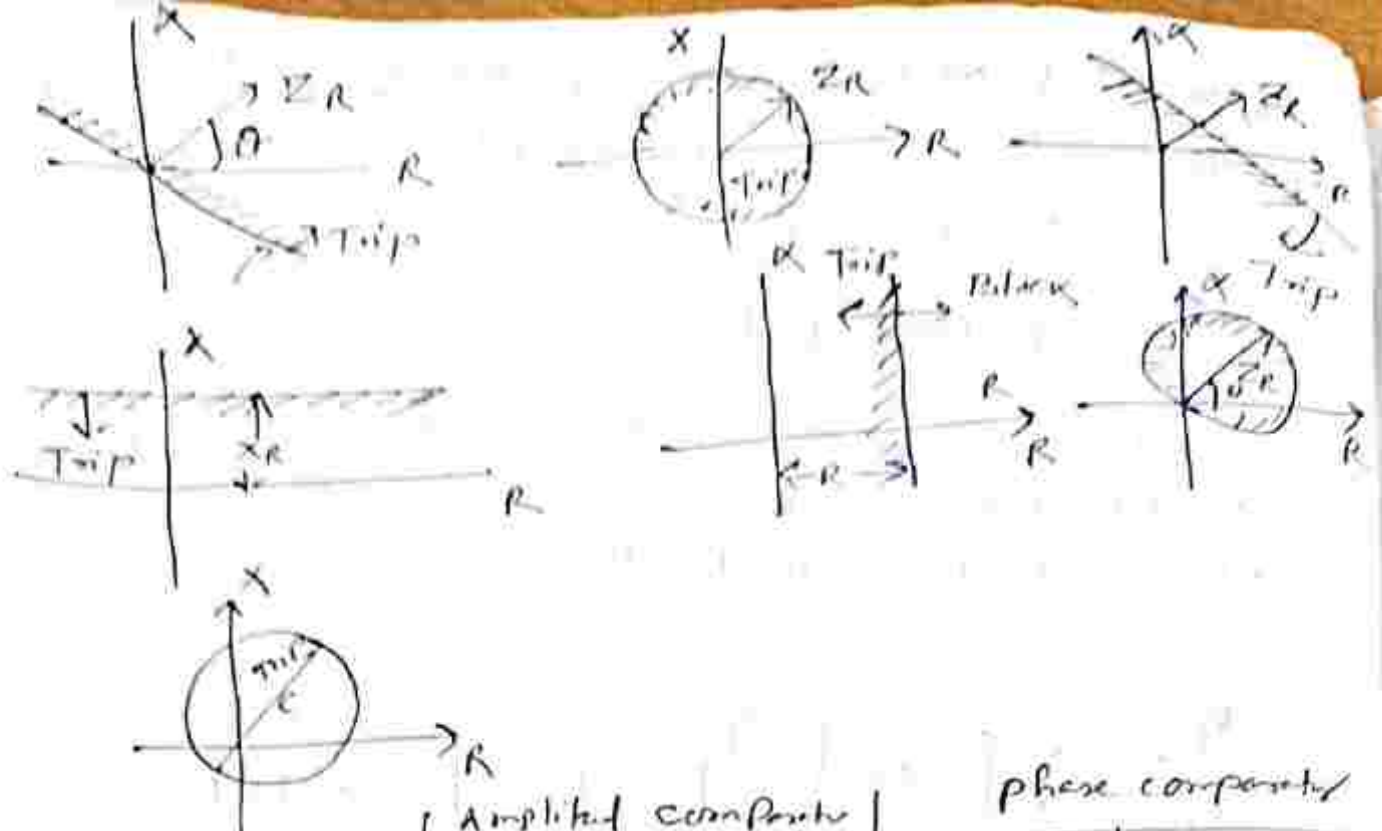
$$S_2 = K_3 V_L + K_4 I_L$$

Voltage V_L and current I_L are fed into measuring circuit M which produce voltages

$$S_1 = K_1 V_L + K_2 I_L$$

$$S_2 = K_3 V_L + K_4 I_L$$

These voltages are fed to the comparator C so as to produce a desired pickup characteristics, the constants of K_1 through K_4 are being selected accordingly. The polar characteristics of a distance relay defines the range of impedance values of the protected primary circuit for which the relay gives circuit breaker tripping. In this way polar characteristic of the relay provides its main characteristics of the relay provides its main discriminative features.



① Directional	Amplitude comparison		Phase comparison	
	operating	Restraining	operating	Restraining
Directional	$ I_L + \frac{V_L}{Z_R} $	$ I_L - \frac{V_L}{Z_R} $	$I_L Z_R$	V_L
Plain impedance	$ I_L $	$ \frac{V_L}{Z_R} $	$I_L Z_R - V_L$	$I_L Z_R + V_L$
Angle - impedance	$ I_L - \frac{V_L}{Z_R} $	$\frac{V_L}{Z_R}$	$(I_L Z_R - V_L)$	$I_L Z_R$
Reactance	$ I_L - \frac{V_L}{X_R} $	$ \frac{V_L}{X_R} $	$(I_L Z_R - V_L \sin \theta)$	$I_L Z_R$
Conductance	$ I_L - \frac{V_L}{R} $	$ \frac{V_L}{R} $	$I_L Z_R - V_L \cos \theta$	$I_L Z_R$
Mho	$ I_L $	$ I_L - \frac{V_L}{Z_R} $	$I_L Z_R - V_L$	V_L
offset mho	$ I_L $	$ \frac{V_L}{Z_R} - n I_L $	$(I_L Z_R - V_L) \cos(\phi - \theta)$	$V_L + n I_L Z_R$

MODULE- IV

The transient faults are more frequent in nature, but they have not doing any damage of the device. For a certain time, the line disconnected from the system momentarily. If the arc is deionized, the line can be reclosed to restore the normal value. In present day power system, automatic reclosing finds wide application. It has been used to effect fault clearance and subsequent reclosure.

Definition & available features:-

- (a) operating time of protective relay:- Time from the inception of the fault to the closing of the tripping contact.
- (b) operating time of circuit breaker:- Time from the energizing of the trip coil until the fault arc is extinguished.
- (c) Dead time of the circuit breaker or system:-

(1) Depending upon the time, fault existing on the system. (a) Transient fault (b) semi-permanent fault (c) permanent fault. It is found that 80% are permanent faults, 12% of semi-permanent and 8% are permanent faults. Reclosing could be resisted some delay so that cause of fault could be burnt away during the time delay.

Auto reclosing could be single phase or three phase. Single phase auto reclosing is restarted when a line to ground fault takes place and reclosed after a predetermined time.

Circuit breaker

→ The basic requirement of any circuit breaker requires the separation of contact in an insulating fluid which serves two functions:

- (a) It extinguishes the arc.
- (b) It provides adequate insulation between the contact.

Basic fluid requirement

- ① Air at atmospheric pressure
- ② Compressed air
- ③ Oil which produce hydrogen for arc extinction
- ④ Ultra high vacuum.
- ⑤ Sulphur hexafluoride.

properties of CB :-

- ① High dielectric strength.
- ② Thermal and chemical stability
- ③ Non-inflammability
- ④ High thermal conductivity.

Initiation of arc

→ The separation of CB contact which are carrying gives rise to an arc without changing the current waveform. At the separation, magnitude of current is very high and resistance

→ The distance of separation is very small, large voltage gradient is set up which cause ionization the particles. When current is high the discharge attains the form of an arc having a temperature high enough to be thermal ionization.

→ The arc is initiated due to field effect and then maintained due to thermal ionization.

Deionization :- The process of deionization is possible in the following ways.

- (i) high pressure
- (ii) forced convection and turbulence
- (iii) arc splitting.

There are two methods by which arc interruption is done. (i) High resistance method (ii) Low resistance or current zero interruption method.

High resistance method :-

ⓐ In this method, ~~arc~~ arc resistance is increased in time to such a high value that the current to zero without arcing thereafter. There will be induced harmful voltage. This is the disadvantage because large energy received by CB.

Low resistance or current zero interruption

This method is used only in ac circuit interruption because there is natural zero of current present in such system. In case of a 50 Hz supply there are 100 zeros per second.

This property of ac circuit is exploited for extinction purpose and the current is not allowed to rise again after a zero occurs.

The arc extinction is explained by two theories.

- (i) Energy balance theory
- (ii) voltage rise theories.

Energy balance theory

If the rate at which the heat generated between the contact is lower than the rate at which heat between the contact dissipated the arcs will be extinguished, otherwise it will restrike.

- (1) Initially when the contact are open, the restriking voltage is zero, heat generated is zero.
- (2) When the contact is fully opened, the resistance is infinite, heat generated zero.

Voltage rise theory :-

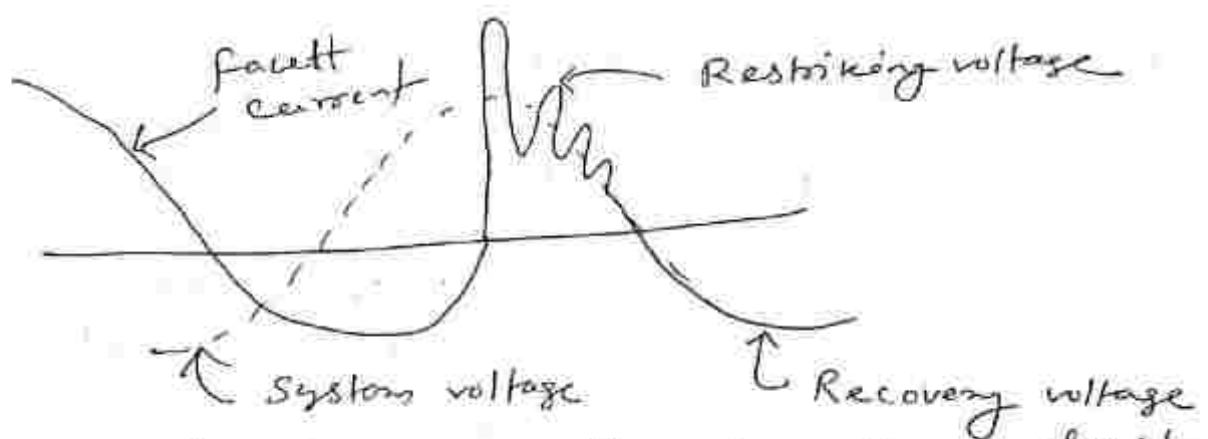
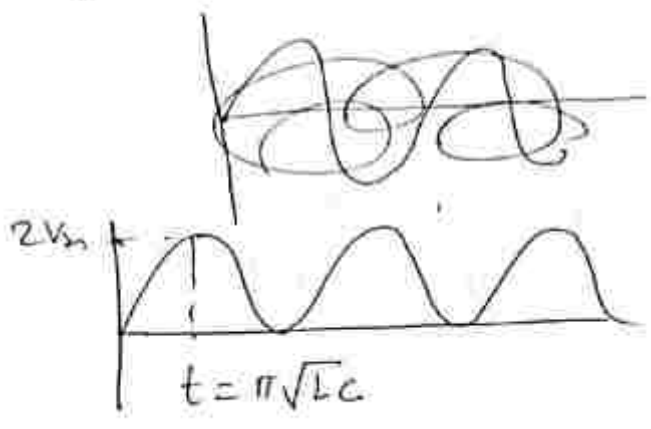
In the initial stage, the resistance is small and contact separates resistance increasing. Immediately after current zero, the electron & hole will be removed from the surface of contact. The ionization at current zero depends upon the power factor and other factors of the circuit like inductance and capacitance.

$$V = V \left(1 - \cos \frac{t}{\sqrt{LC}} \right)$$

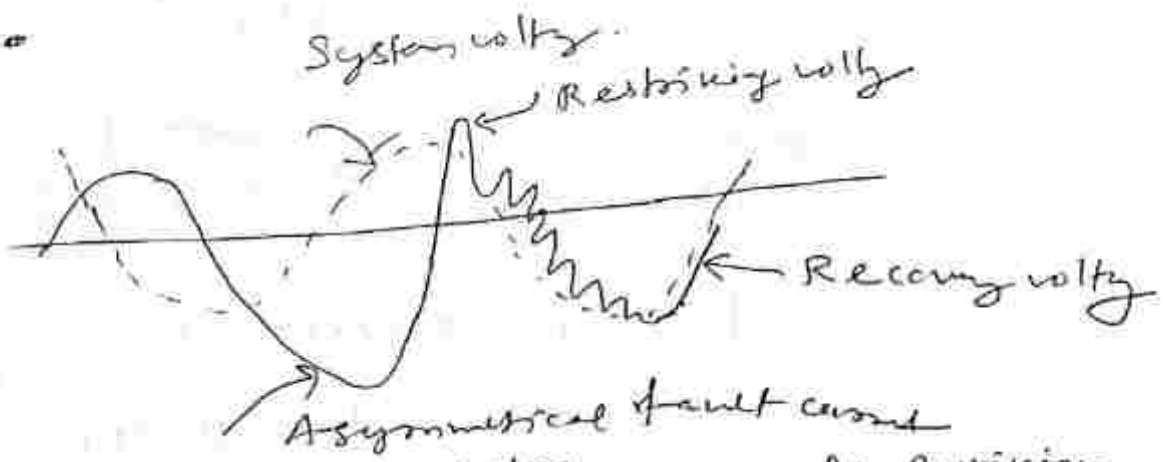
$V =$ restriking the voltage

V = voltage at the instant of interruption
 L & C = series inductance & capacitance

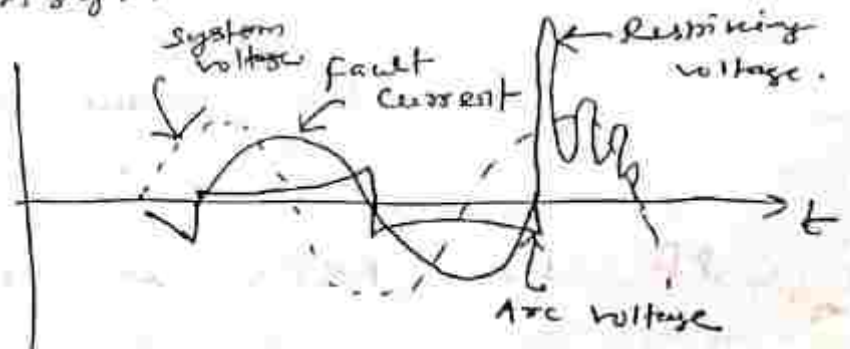
→ Lower the value of inductance & capacitance, higher the natural frequency, sever the effect of restriking voltage.



→ current lags the voltage by 90° . A fault current can have degree of asymmetry depending upon the time in the cycle at which the fault occurs.



~~Other effect~~



Restriking voltage: - The instant transient voltage which appears across the breaker contact at the instant of arc extinction is known as the restriking voltage.

Recovery voltage: - The power frequency r.m.s. voltage that appears across the breaker contact after transient oscillation die out

Active recovery voltage: - It is defined as the instantaneous recovery voltage at the instant of arc extinction

$$V_{or} = k V_m \sin \phi$$

Rate of rise of restriking voltage (RRRV)

Average RRRV = $\frac{\text{Peak value of restriking voltage}}{\text{Time taken to reach to peak value.}}$

$$= \frac{2 V_m}{\pi \sqrt{LC}}$$

$$v = V_m \left(1 - \cos \frac{t}{\sqrt{LC}} \right)$$

$$\frac{dv}{dt} = \frac{V_m}{\sqrt{LC}} \sin \frac{t}{\sqrt{LC}}$$

This is maximum when $\frac{t}{\sqrt{LC}} = \pi/2$

$$t = \frac{\pi}{2} \sqrt{LC}$$

and the value is $\frac{V_m}{\sqrt{LC}}$

If the RRRV is smaller than the rate

of which the dielectric between the contact developed the arc will extinguish.

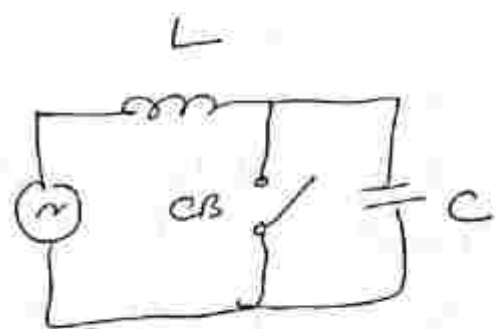
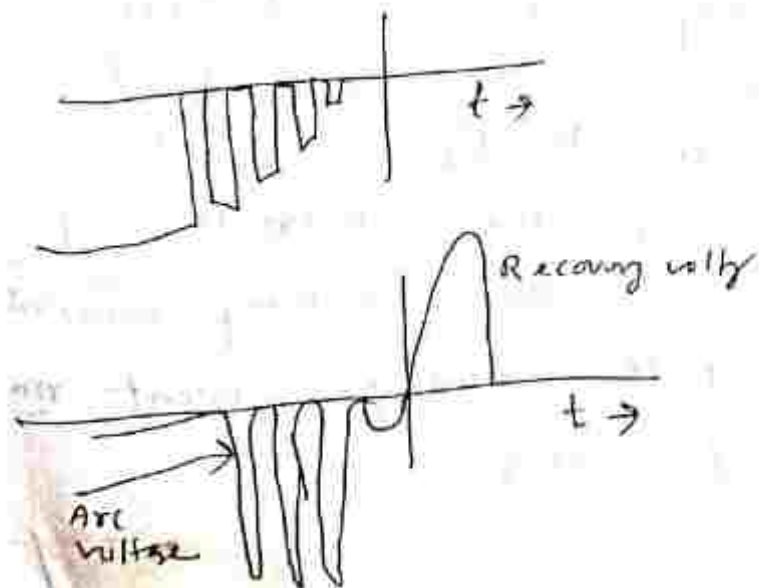
Current Chopping

$$V = \frac{L di}{dt}$$

→ When CB is interrupt low inductive current such as current due to no load magnetizing current of a transformer. The breaking of current before it passes through the natural zero is termed as current chopping. At a certain arc current, because of large deionizing force, the current suddenly reduces to zero. The current in arc was flowing from the source through the inductance and the CB contacts.

→ The conversion electromagnetic to electrostatic form of energy i.e. current is diverted to the capacitor from the arc. If i_a is the instantaneous value of arc current when chop takes place, the prospective value of voltage to which the capacitor will be charge.

$$V = i_a \sqrt{L/C}$$



Rating of Circuit Breaker :-

- ① Number of pole
- ② rated voltage & current
- ③ rated frequency
- ④ Rated making capacity
- ⑤ rated symmetrical and asymmetrical breaking capacity
- ⑥ operating duty.

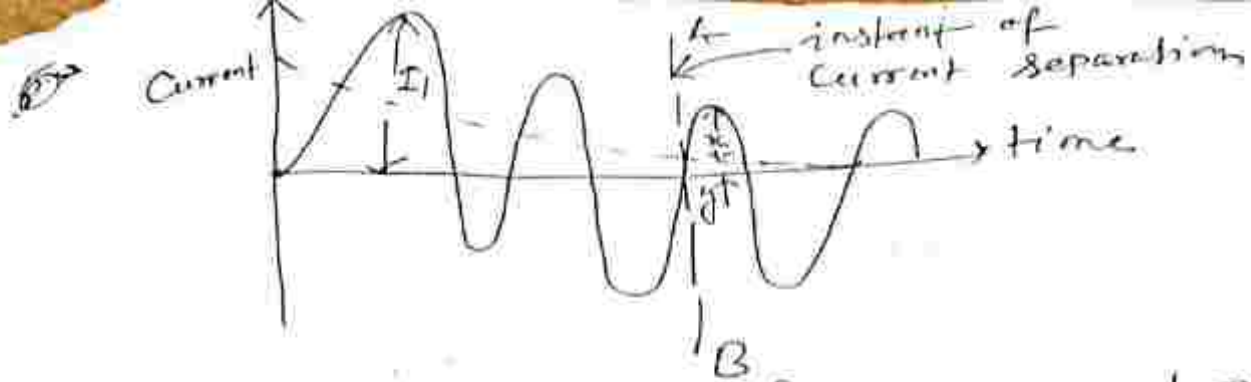
1 → The number of pole per phase of a breaker is a function of operating voltage.

2 → The breaker is expected to operate at a maximum voltage at which normally is higher than rated nominal voltage.

3 → The rated current of CB is the maximum value of current in amp. which it shall carry continuously without exceeding the temperature limits of the various parts of the CB.

3 → The rated frequency of a breaker is the frequency for which it is designed to operate.

4. making current is the peak value of the maximum current loop, including d.c component in any phase during first cycle of current when CB closes. The making current corresponds to the ordinate I_1 . The making current is the peak value rather than its rms value. The making ^{capacity} current is the product of the making current and instantaneous value of voltage.



59 The current in the first one or two cycle is known as subtransient current and 8 to 10 cycle is known as transient current.

The symmetrical breaking current is obtained by known, the making current can be obtained by multiplying this current by $\sqrt{2}$ and again by 1.8 times.

The symmetric breaking current is given by $x/\sqrt{2}$ and asymmetric breaking current is given by $\sqrt{\left(\frac{x}{\sqrt{2}}\right)^2 + y^2}$.

The breaking capacity of a breaker is the product of breaking current and recovery voltage.

Short time rated current is the current that can be safely applied, with the CB in its normal condition, for 3 seconds.

$$B - 3 - MB - 3 - MB$$

CB with autoreclose

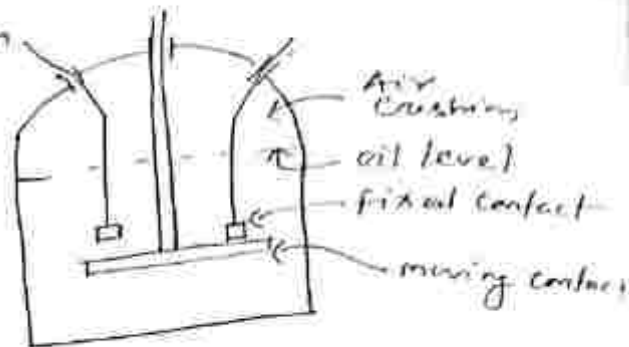
$$B - D_t - MB$$

D_t = Dead time

Plain oil circuit breaker:-

→ Air cushion is required between the oil surface and tank

→ The air cushion also serves to absorb the mechanical shock of the upward oil movement.



→ ~~And~~ The minimum oil head is required to provide substantial oil pressure. The gas generated from the arc to the oil surface is produced. The gas is partially ionized and low dielectric strength. So appreciable amount of oil depending upon the working voltage should always exist between the contact and the tank.

principle :- The final arc extinction process involves increasing the length of the arc. The length of the arc depends upon the arc current and recovery voltage. Initially, the separation is very small and high voltage gradient between the contact ionize the oil. The gas obtained mainly hydrogen gas and is dissociated in its atomic form, releasing lot of heat. The volume of oil increases. So the oil is therefore pushed away from the arc. Final arc extinction of the arc takes place at a current zero when the power input to the arc is less than that dissipated between the contact.

MOCB :- one of the most important characteristic of OCB is to reduce the oil needed.

- ① Reduction in tank size
- ② Reduction in total weight
- ③ Reduction in cost.

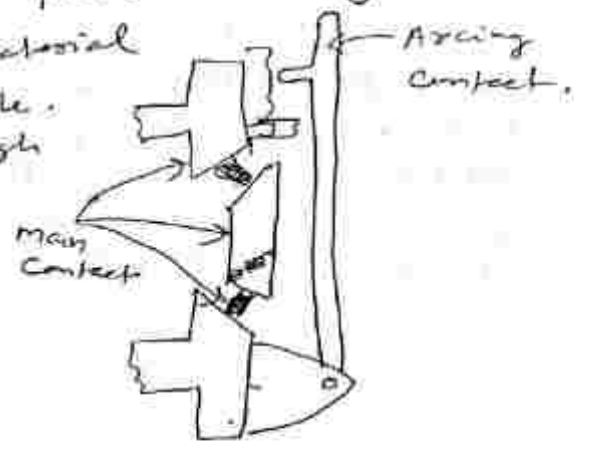
The minimum OCB ~~is~~ uses solid material for insulating purpose. The minimum oil CB can be self blast type, or external blast type. ✓

In case of self blast type, gas pressure developed depends upon current to be interrupted. Higher the current interrupted, larger the gas pressure and hence effective for arc quenching. The insulating material are glass fibre,

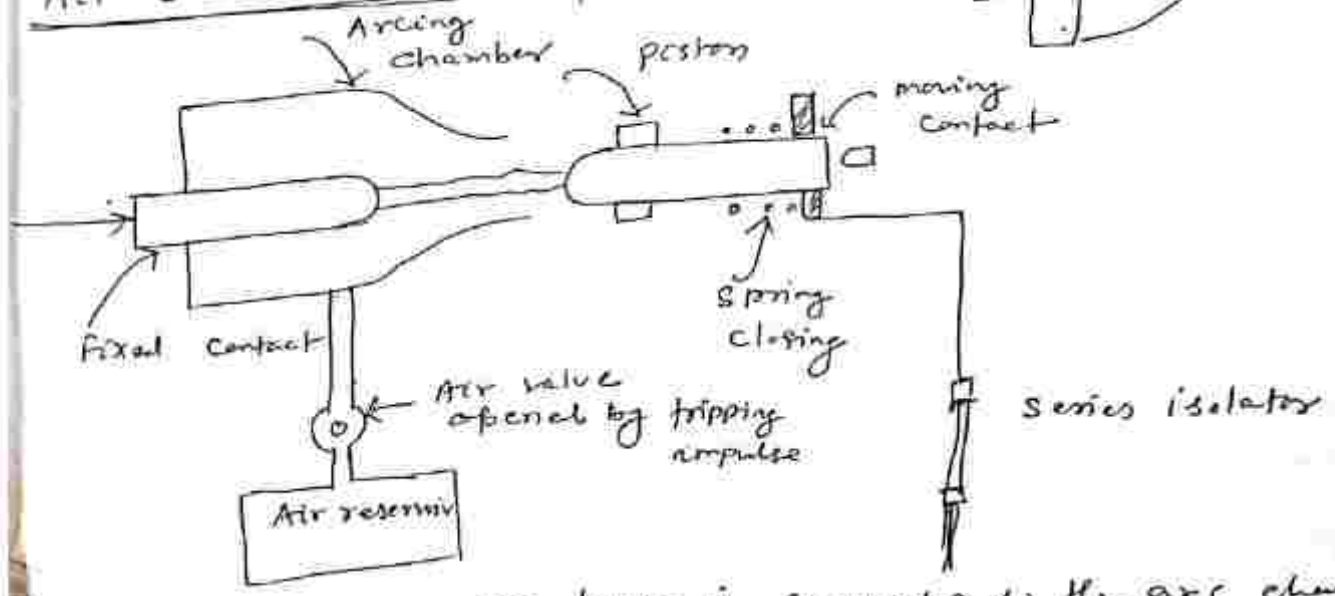
The arcing chamber is designed in terms of
 (a) axial venting (b) radial venting.
 In axial venting gas produced in longitudinal direction.
 In radial venting the arc is transverse direction.
 In axial venting, high gas pressure is generated with high dielectric strength. It is low current and high voltage. In radial venting is used heavy current and low voltage.
 This type of CB is used voltage upto 8000 MVA at 245 KV with a total break times 3 to 5 cycle.

Air CB (1) Fire risk and maintenance are eliminated.
 (2) Arcing produced in air completely removed.
 (3) Heavy mechanical stress are set up by gas pressure.
 Air CB is used for low voltage circuit as well as highest transmission voltage.

Principle :- It has two pairs of contacts per phase. The main pair made up copper and carries current under normal operating condn. The other pair is arcing electrodes which made up carbony. The material used for contact should be non volatile.
 The principle of operation is based on high resistance method.



Air blast CB (ABC)



→ The breaker reservoir tank is connected to the arc chamber.
 When a tripping impulse opens the air valve.
 → The air entering the arc chamber exerts a pressure on the moving contact

→ The air moves with high velocity through the nozzle. The diameter of the arc is reduced. The temperature gradient set up. When the current passes through the zero, the air blast is more effective. The total heat loss is proportional to arc diameter, whereas the total energy content of the arc is roughly proportional to the square of the diameter.

→ Most of the CBS upto 11kV are either ^{air} air break type or oil break type. Between 11kV and 66kV mainly oil CB, while 132kV and 275kV the market is shared by oil.

VCB In vacuum type discharge, the mean free path of particle is small and electron avalanche is formed. In VCB 10^{-5} torr (1 micron = 10^{-3} torr) (one mm of Hg is known as torr) mean free path is produced. When electrodes separated by a few mm an electron crosses the gap without any collision. Due to electron avalanche current growth can not takes. In vacuum arc is the neutral atom, ions and electrons do not come. Due to large mean free path, dielectric strength is thousand times more than the gas interrupted device.

→ A high vapour pressure and low conductivity metal is more desirable to limit the current chopping whereas low vapour pressure metal are more desirable from the arc extinction point of view.