

**SUBJECT-BASIC ELECTRONICS ENGINEERING**

**TOPIC-OPERATIONAL AMPLIFIER**

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## OPERATIONAL AMPLIFIER

### Operational Amplifier (OP-Amp)

An operational amplifier is a very high gain amplifier having very high input impedance (in  $M\Omega$  or more) and low output impedance (less than  $100\Omega$ ).

The operational amplifier amplifies the signal and also performs the mathematical operations like addition, subtraction, integration etc., that's why it is named as op-amp.

One basic op-amp circuit is shown in fig 1.

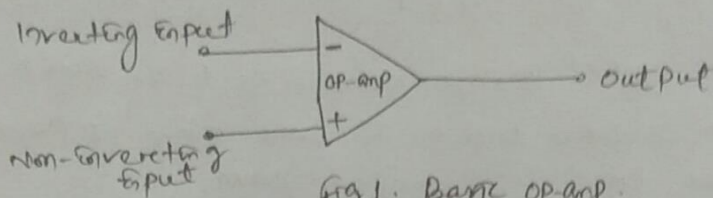


Fig 1. Basic op-amp.

It has two inputs: (i) Inverting (ii) Non-Inverting.

→ The (+) input produces an output that is in phase with the input signal applied, whereas the (-) input to the <sup>terminal</sup> results in an opposite-polarity output.

#### Ideal characteristics of op-amp :-

- 1) Voltage gain (AV) is infinite.
- 2) Input impedance is infinite.
- 3) Input offset voltage is zero.
- 4) Output voltage range is infinite.
- 5) Bandwidth is infinite.
- 6) Slew rate is infinite.
- 7) Output impedance is zero.
- 8) Common mode rejection ratio (CMRR) is infinite.

BASIC OP-AMP.

The basic ckt connection using op-amp is shown in fig 2.

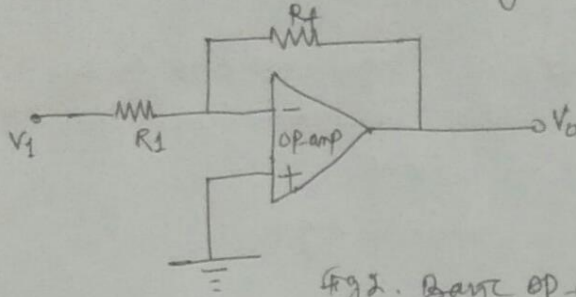
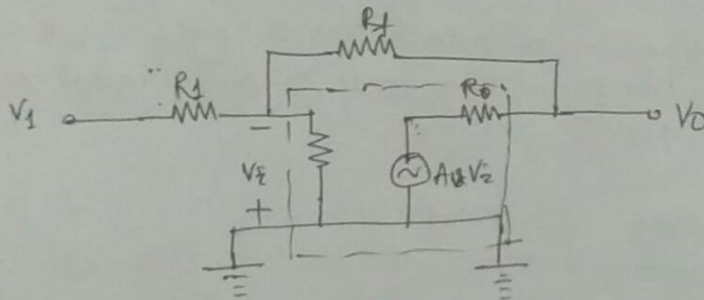


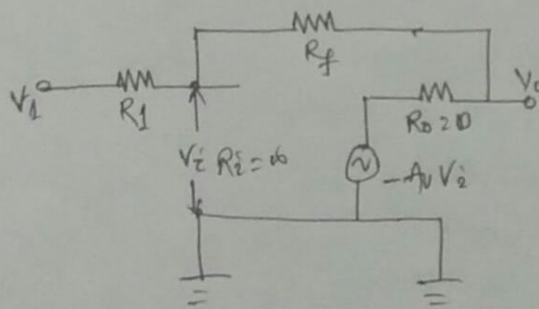
fig 2. Basic op-amp connection

An input signal  $V_1$  is applied through resistor  $R_1$  to the inverting input. The op-amp is then connected back to the same inverting input through resistor  $R_f$ . The plus input is connected to ground.

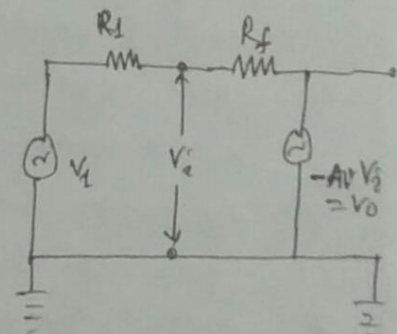
Now draw the <sup>ac</sup> equivalent ckt. (ideal condition)



(a)



(b)



(c)

fig(a). operation of op-amp as constant gain multiplier.

- (a) op-amp ac equivalent ckt,
- (b) ideal op-amp equivalent ckt
- (c) resultant equivalent ckt.

2.

Here, we consider the ideal op-amp equivalent ckt., hence we replace  $R_i = \infty$ ,  $R_o = 0 \Omega$ .

The ckt is redrawn as shown in fig 2c.

using superposition, we can solve for the voltage  $V_2$  in terms of the components due to each of the sources.

For the source  $V_1$  set  $-A_0 V_2 = 0$ ,

$$V_{21} = \frac{R_f}{R_1 + R_f} V_1$$

For the source  $-A_0 V_2$ , set  $V_1 = 0$ ,

$$V_{22} = \frac{R_1}{R_1 + R_f} (-A_0 V_2)$$

The total voltage  $V_2$  is then

$$V_2 = V_{21} + V_{22} = \frac{R_f}{R_1 + R_f} V_1 + \frac{R_1}{R_1 + R_f} (-A_0 V_2)$$

$$V_2 = \frac{R_f}{R_f + (1 + A_0) R_1} V_1$$

If  $A_0 \gg 1$  and  $A_0 R_1 \gg R_f$ , then

$$V_2 = \frac{R_f}{A_0 R_1} V_1$$

Solving for  $V_0/V_2$ , we get

$$\frac{V_0}{V_2} = \frac{-A_0 V_2}{V_2} = \frac{-A_0 R_f V_1}{V_2 A_0 R_1} = \frac{-R_f}{R_1} \frac{V_1}{V_2}$$

So that

$$\boxed{\frac{V_0}{V_1} = -\frac{R_f}{R_1}}$$

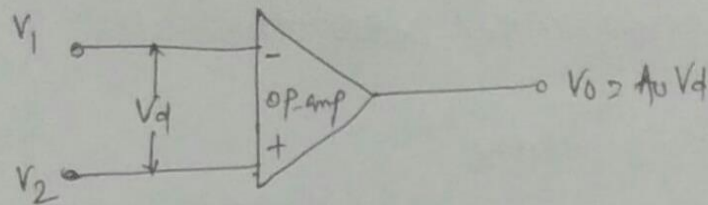
$$\boxed{A_V = -R_f/R_1}$$

Unity gain

If  $R_f = R_1$ , then the voltage gain  
voltage gain =  $-R_f/R_1 = -1$

### Virtual ground :-

In ideal condition, if one input is at zero potential, then the other terminal is also considered as at zero potential.



$V_1, V_2 \rightarrow$  Input voltages

$V_d \rightarrow$  difference voltage

$V_d = V_1 - V_2$ ,  $A_o \rightarrow$  voltage gain

The diff voltage  $(V_0) = A_o V_d$

$$\text{Now } A_o = \frac{V_0}{V_d}$$

$$= \frac{V_0}{V_1 - V_2}$$

We know that the voltage gain of the ideal op-amp is  $\infty$ .

$$\text{So, } \infty = \frac{V_0}{V_1 - V_2} = \frac{V_0}{0V}$$

$$\therefore \Rightarrow V_1 - V_2 = 0V$$

$$\text{and } \boxed{V_1 = V_2}$$

Inverting Amplifier

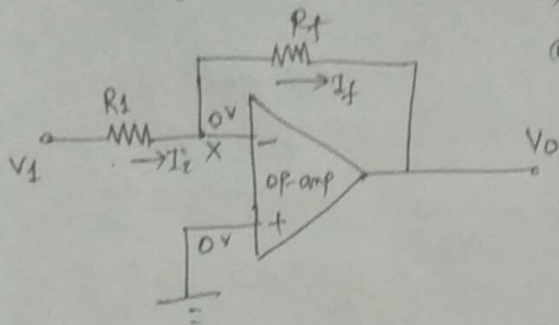


fig. Inverting op-amp configuration

In inverting amplifier, the input signal is applied to the (-) terminal. And the (+) terminal is connected to ground.

$I_i$  is the inp current &  $I_f$  is feedback current.

Applying KCL at Node X.

As it's virtual ground concept the voltage at X is zero.

$$I_i = I_f$$

$$\frac{V_1 - 0V}{R_1} = \frac{0V - V_0}{R_f}$$

$$\Rightarrow \frac{V_1}{R_1} = -\frac{V_0}{R_f}$$

$$\Rightarrow \boxed{\frac{V_0}{V_1} = -R_f/R_1}$$

Non Inverting Amplifier :-

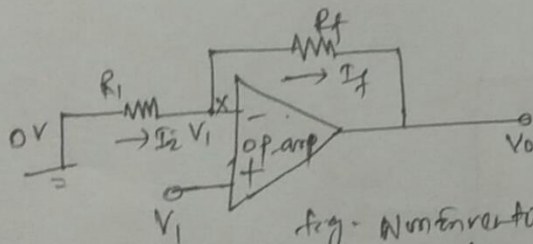


fig. Non Inverting Amplifier

In non-inverting amplifier, the input signal is applied to (+) terminal and (-) terminal is connected to ground.

Applying KCL at X, we get.

$$I_i = I_f$$

$$\Rightarrow \frac{0V - V_1}{R_1} = \frac{V_1 - V_0}{R_f}$$

$$\Rightarrow \frac{-V_1}{R_1} = \frac{V_1 - V_0}{R_f}$$

$$\Rightarrow \boxed{\frac{V_0}{V_1} = 1 + \frac{R_f}{R_1}}$$

Summing Amplifier :- It produces the sum of the input signals.

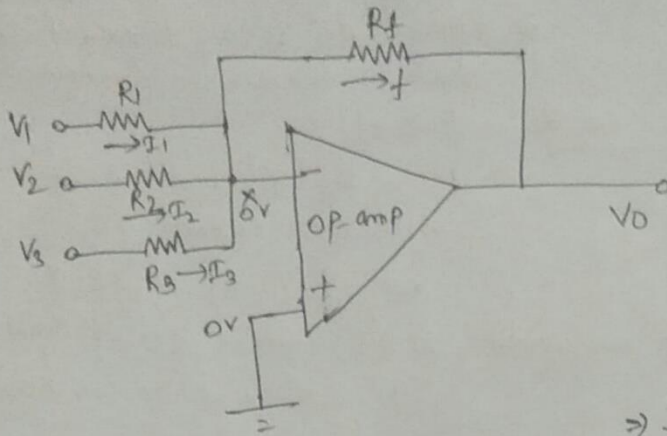


Fig. Summing amplifier

Applying KCL at X,  
we get

$$I_1 + I_2 + I_3 = I_f$$

$$\Rightarrow \frac{V_1 - 0V}{R_1} + \frac{V_2 - 0V}{R_2} + \frac{V_3 - 0V}{R_3} = \frac{0V - V_0}{R_f}$$

$$\Rightarrow \frac{V_1}{R_1} + \frac{V_2}{R_2} + \frac{V_3}{R_3} = \frac{-V_0}{R_f}$$

$$\Rightarrow V_0 = - \left( \frac{R_f}{R_1} V_1 + \frac{R_f}{R_2} V_2 + \frac{R_f}{R_3} V_3 \right)$$

If  $R_f = R_1 = R_2 = R_3$

$$V_0 = -(V_1 + V_2 + V_3)$$

The op of the summing amplifier is the summation of all the input signals.

Subtractor ~~is~~ is Differential amplifier :-

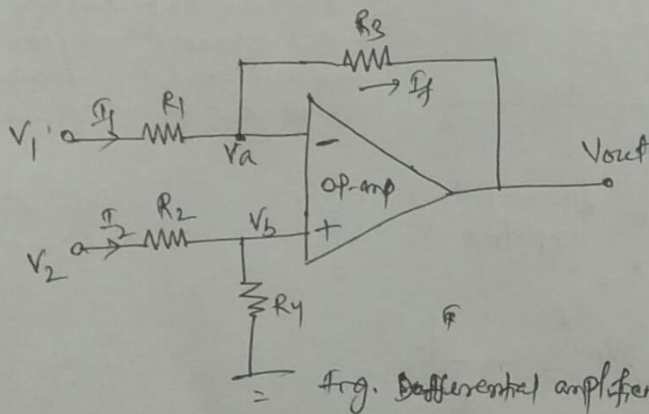


Fig. Differential amplifier

From the fig. we can find

$$I_1 = \frac{V_1 - V_a}{R_1},$$

$$I_2 = \frac{V_2 - V_b}{R_2},$$

$$I_3 = \frac{V_a - V_{out}}{R_3}$$

As per the virtual ground concept,  $V_a = V_b$ .

and  $V_b = V_2 \left( \frac{R_4}{R_2 + R_4} \right)$

If  $V_2 = 0$ ; then;  $V_{out(a)} = -V_1 \left( \frac{R_3}{R_1} \right)$

If  $V_1 = 0$ ; then,

$$V_{out(b)} = V_2 \left( \frac{R_4}{R_2 + R_4} \right) \left( 1 + \frac{R_3}{R_1} \right)$$

↑  
Using voltage division

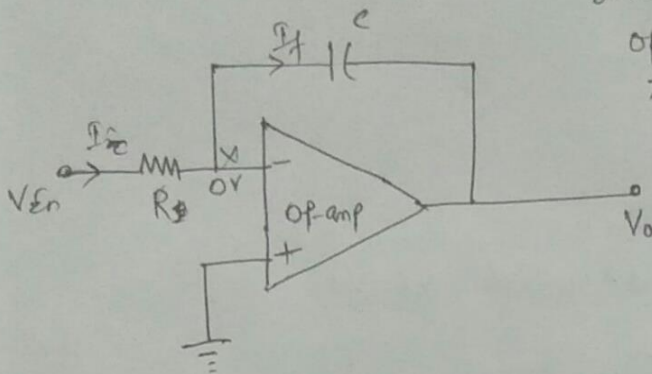
$$V_{out} = -V_{out(a)} + V_{out(b)}$$

$$\therefore V_{out} = -V_1 \left( \frac{R_3}{R_1} \right) + V_2 \left( \frac{R_4}{R_2 + R_4} \right) \left( 1 + \frac{R_3}{R_1} \right)$$

If  $R_1 = R_2 = R_3 = R_4$ , then we

$$\boxed{V_{out} = V_2 - V_1}$$

Integrator circuit



The op-amp integrator is an operational amplifier circuit that performs the mathematical operation of integration.

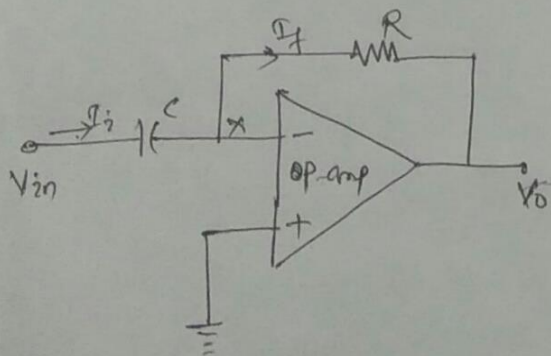
→ The integrator produces an output voltage which is proportional to the integral of the input voltage.

Fig. Integrator ckt

Applying KCL at X, we get

$$\begin{aligned}
 I_i &= I_f \\
 \Rightarrow \frac{V_{in} - 0V}{R_1} &= C \frac{d(V_{in} - V_o)}{dt} \\
 \Rightarrow \frac{V_{in}}{R_1} &= -C \frac{dV_o}{dt} \\
 \Rightarrow \boxed{V_o = -\frac{1}{RC} \int V_{in} dt}
 \end{aligned}$$

Differentiator amplifier



The op-amp differentiator is an operational amplifier circuit that performs the mathematical operation of differentiation.

The differentiator produces an output voltage which is directly proportional to the input voltage's rate-of-change with respect to time.

Applying KCL at X, we get

$$I_{in} = I_f$$

$$\Rightarrow \frac{C d(V_{in} - 0V)}{dt} = \frac{0V - V_o}{R}$$

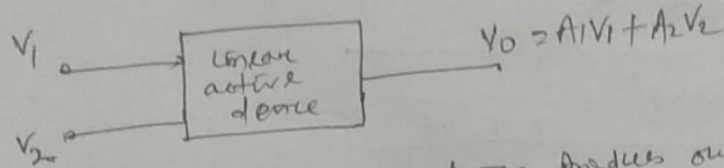
$$\Rightarrow \frac{C dV_{in}}{dt} = -\frac{V_o}{R}$$

$$\Rightarrow \boxed{V_o = -RC \frac{dV_{in}}{dt}}$$

CMRR (Common mode rejection ratio)

The CMRR is defined as, it is the ratio between differential gain ( $A_d$ ) to common mode gain ( $A_c$ ).

$$CMRR = \frac{A_d}{A_c}$$



Let us consider a linear active device produces output  $V_0$  is the linear combination of inputs.

The difference voltage is defined as

$$V_d = V_1 - V_2 \quad \text{--- (1)}$$

and the common mode voltage is defined as

$$V_c = \frac{V_1 + V_2}{2} \quad \text{--- (2)}$$

Subtract eqn (2) from eqn (1)

$$\begin{array}{r} V_d = V_1 - V_2 \\ 2V_c = V_1 + V_2 \\ \hline V_d - 2V_c = -2V_2 \end{array}$$

$$\Rightarrow V_2 = \frac{V_d - 2V_c}{-2}$$

Add eqn (1) with eqn (2)

$$\begin{array}{r} V_d = V_1 - V_2 \\ 2V_c = V_1 + V_2 \\ \hline V_d + 2V_c = 2V_1 \end{array}$$

$$\Rightarrow V_1 = V_c + \frac{V_d}{2}$$

Substitute the value of  $V_1$  and  $V_2$  in  $V_0 = A_1V_1 + A_2V_2$ .

$$\begin{aligned} \text{So, } V_0 &= A_1 \left( V_c + \frac{V_d}{2} \right) + A_2 \left( V_c - \frac{V_d}{2} \right) \\ &= A_1 V_c + \frac{A_1 V_d}{2} + A_2 V_c - \frac{A_2 V_d}{2} \\ &= (A_1 + A_2) V_c + \frac{(A_1 - A_2)}{2} V_d \end{aligned}$$

$$V_0 = A_c V_c + A_d V_d$$

where  $A_1 + A_2 = A_c$   
&  $\frac{A_1 - A_2}{2} = A_d$

$A_c \rightarrow$  common mode gain of the amplifier  
 $A_d \rightarrow$  differential gain of the amplifier.

$$\text{CMRR in dB} = 20 \log_{10} \frac{A_d}{A_c}$$

$$V_o = A_d V_d + A_c V_c$$

$$= A_d V_d \left( 1 + \frac{A_c V_c}{A_d V_d} \right)$$

$$V_o = A_d V_d \left( 1 + \frac{1}{\text{CMRR}} \frac{V_c}{V_d} \right)$$